

Impact of **Fecundity-Immunity** Trade-off on Emergent properties and Host Eco-Evolutionary Dynamics.

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Aussois
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What do we know about epidemics ?

Epidemics are known to reduce the host population size.



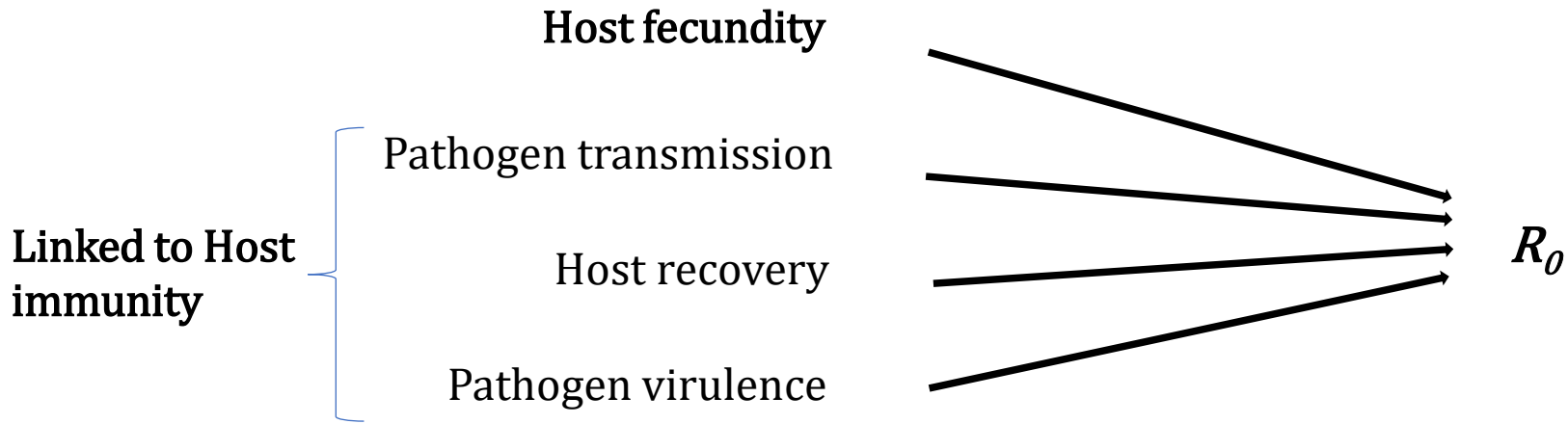
But what if the host is evolving /developing defense mechanisms ?

What do we know about epidemics ?

Epidemics propagate $\longrightarrow R_0$

The basic reproduction number R_0 \longrightarrow

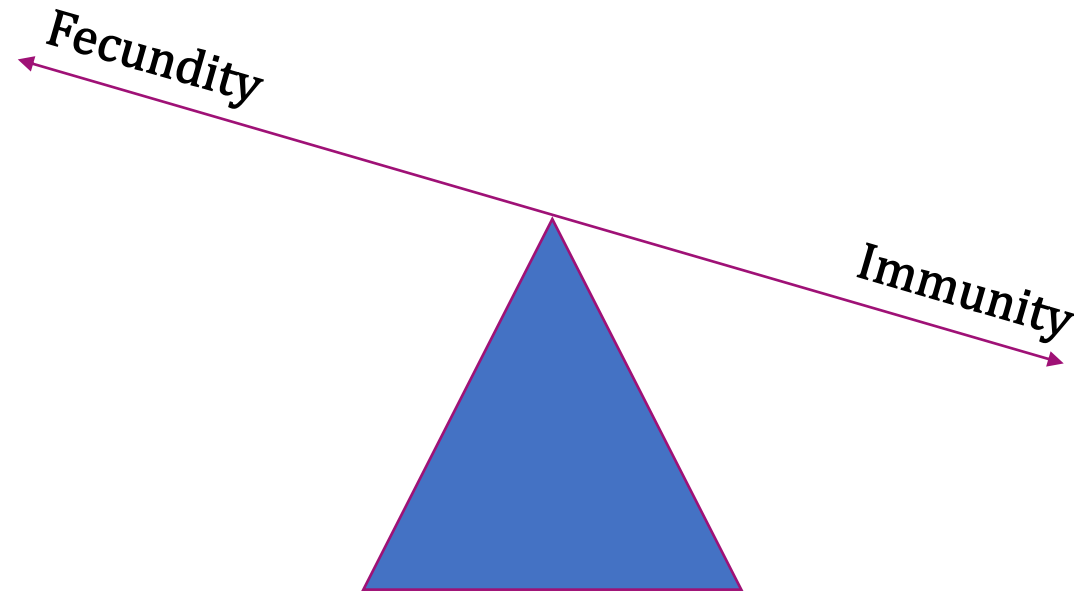
R_0 is the number of secondary infections of one infected host in a susceptible population. If $R_0 > 1$, the pathogen can invade and eventually become endemic in the host population.



But what if the host is evolving /enhancing immunity?

Fecundity - Immunity Trade-off

Empirical Evidences



Reproduction–Immunity Trade-Offs in Insects

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Functional Ecology



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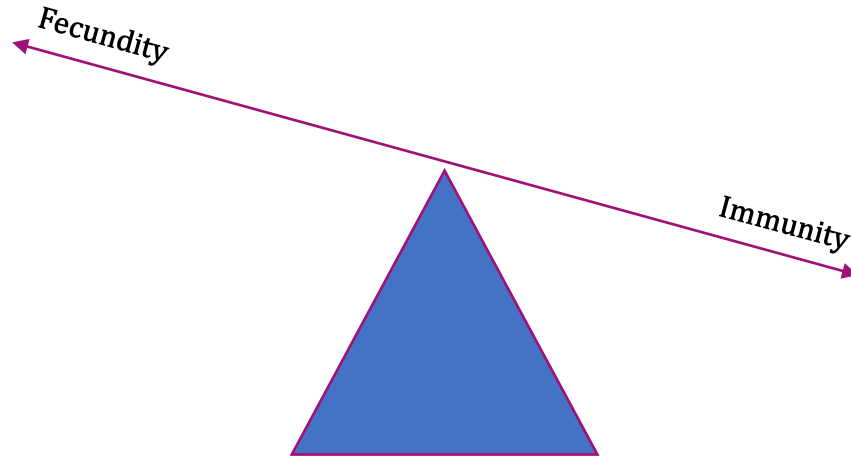
Trade-offs among locomotor performance, reproduction and immunity in lizards

Jerry F. Husak^{*,1}, Haley A. Ferguson¹ and Matthew B. Lovern²

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Fecundity - Immunity Trade-off

Theoretical Works



Host – Pathogen Diversification

Host – Pathogen Co – Existence

The Implications of Coevolutionary Dynamics to
Host-Parasite Interactions

Alex Best,^{1,*} Andy White,² and Mike Boots¹

The evolution of host resistance: Tolerance and control as
distinct strategies

M.R. Miller^{a,*}, A. White^b, M. Boots^a

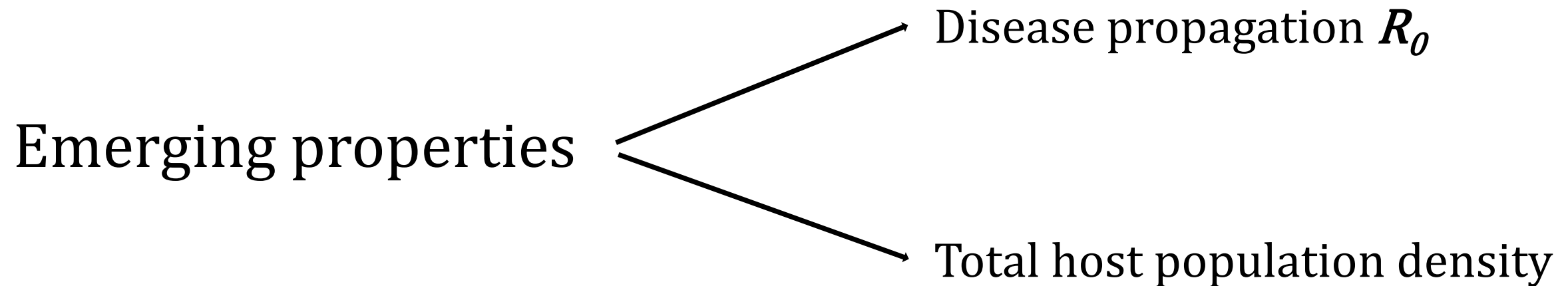
The Evolution of Host-Parasite Range

A. Best,^{1,*} A. White,² É. Kisdi,³ J. Antonovics,⁴ M. A. Brockhurst,⁵ and M. Boots¹

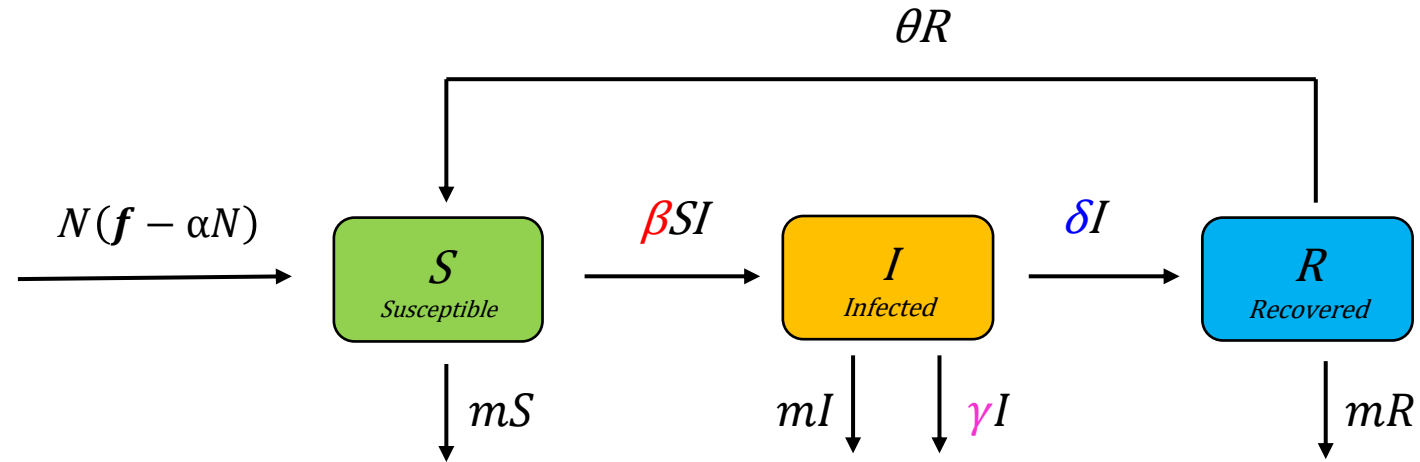
Three Mechanisms of Host Resistance to Microparasites—Avoidance,
Recovery and Tolerance—Show Different Evolutionary Dynamics

MICHAEL BOOTS^{*†} AND ROGER G. BOWERS[‡]

What are the consequences of a **fecundity-immunity** trade-off on emerging properties in the system and on host eco-evolutionary dynamics?



The epidemic model



$$\frac{dS}{dt} = N(f - \alpha N) - \beta SI - mS + \theta R$$

$$\frac{dI}{dt} = \beta SI - (\gamma + \delta + m)I$$

$$\frac{dR}{dt} = \delta I - (\theta + m)R$$

$$N = S + I + R$$

f : Fecundity of the species.

α : Inter – specific competition of the species.

β : Pathogen transmission

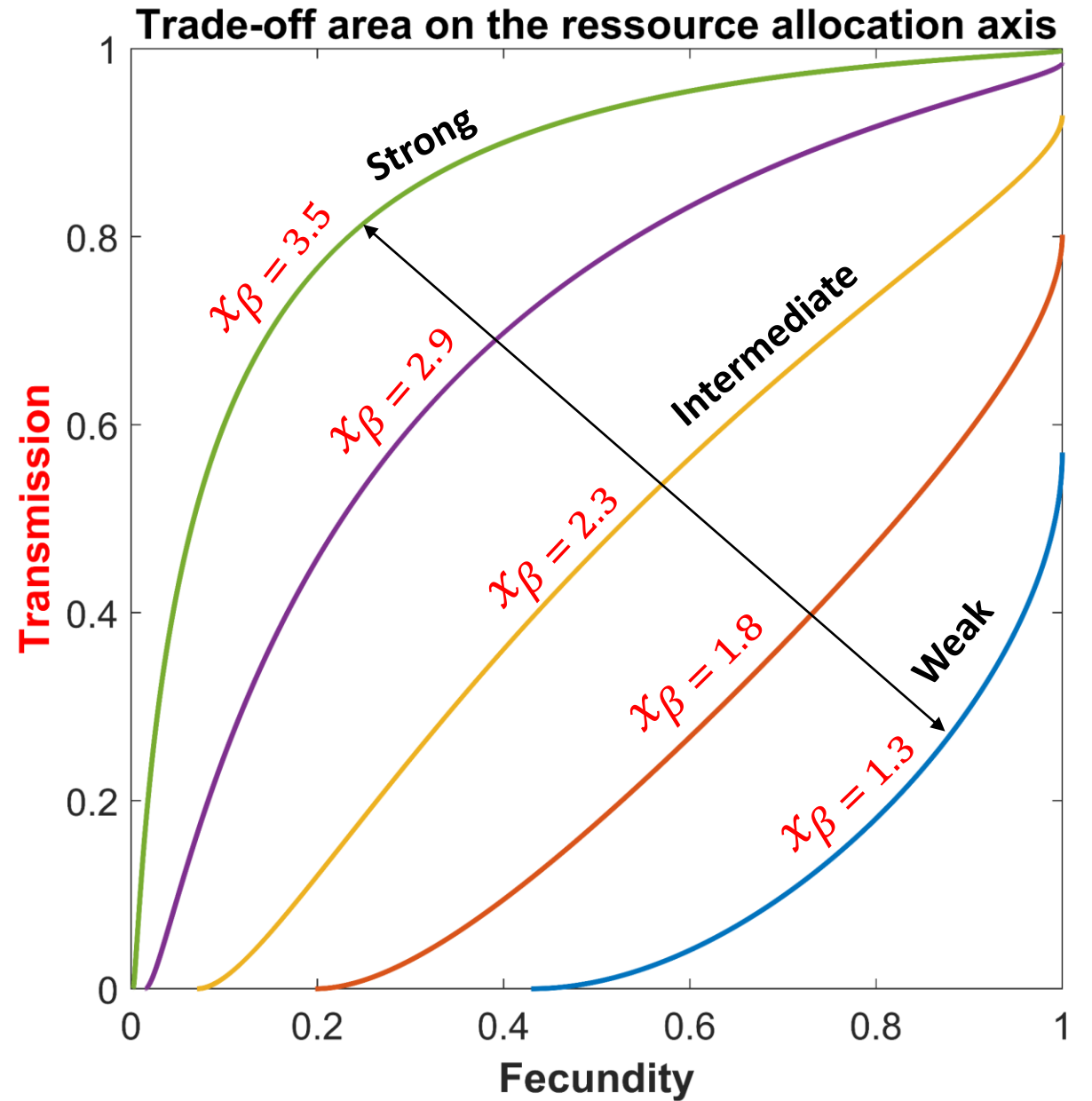
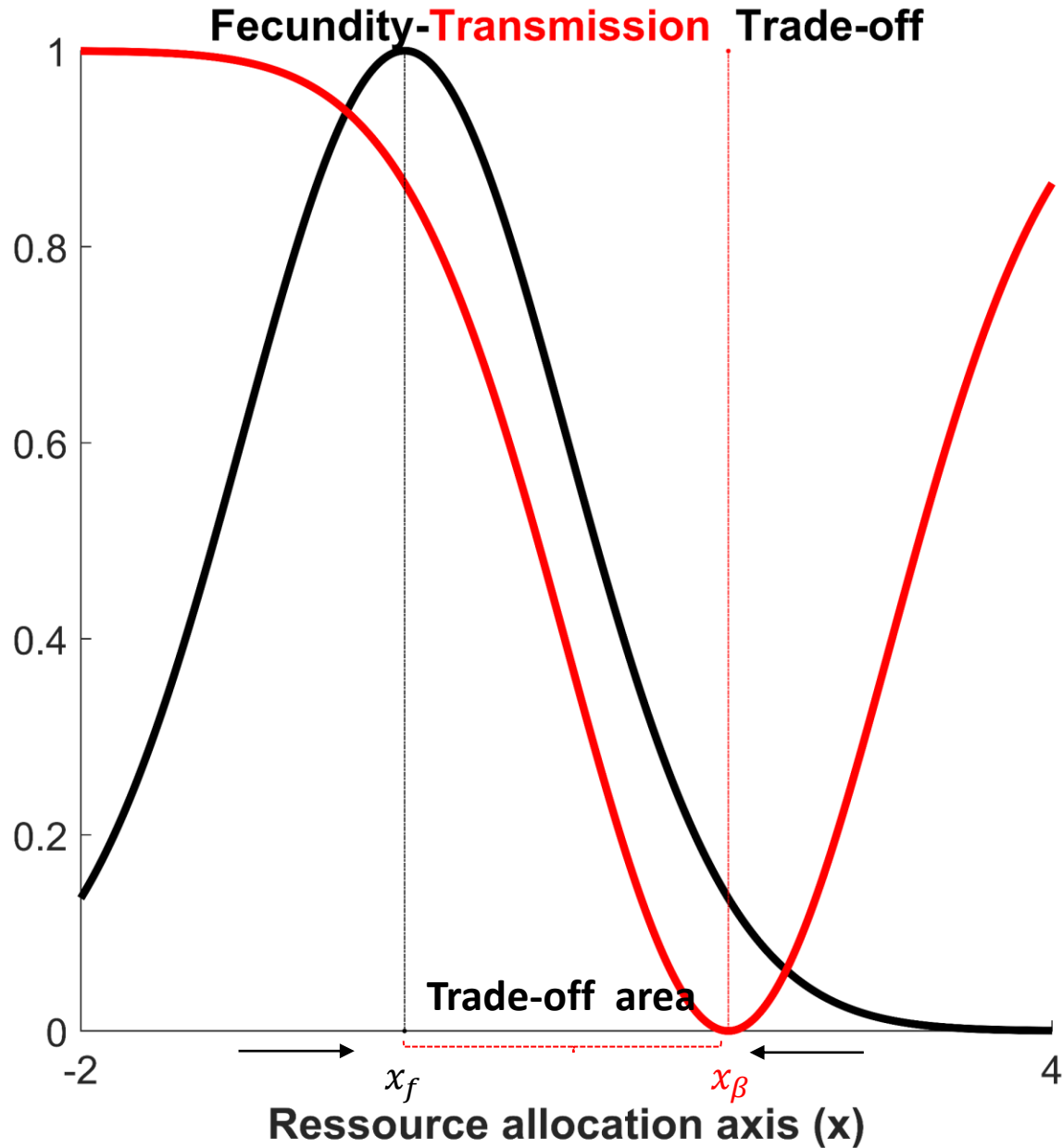
m : Natural mortality rate.

γ : Virulence (Pathogen – induced death rate).

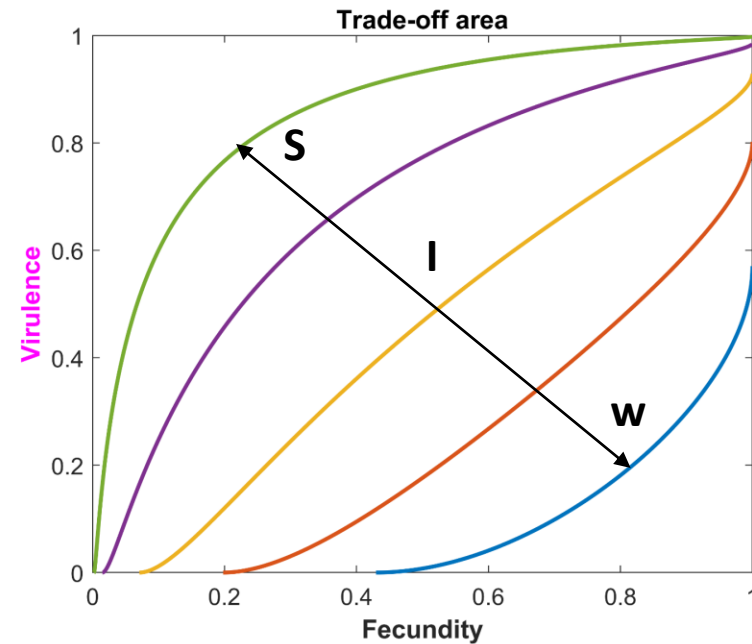
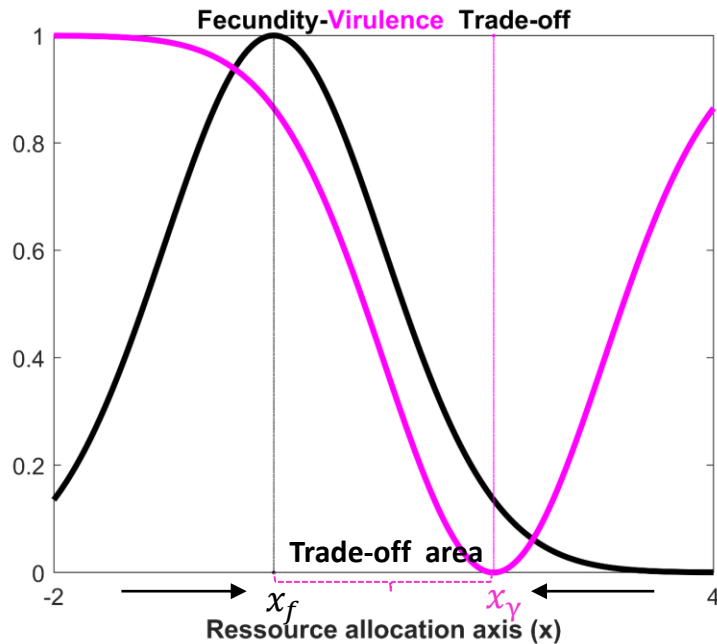
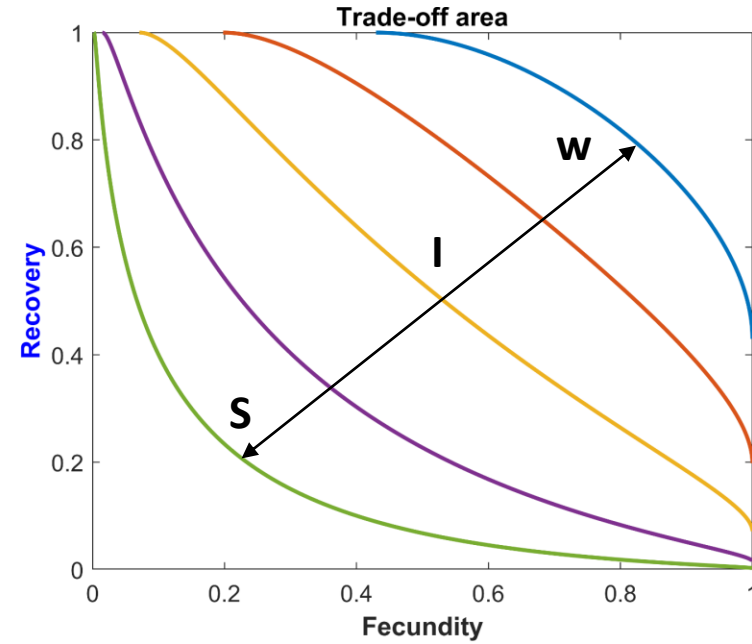
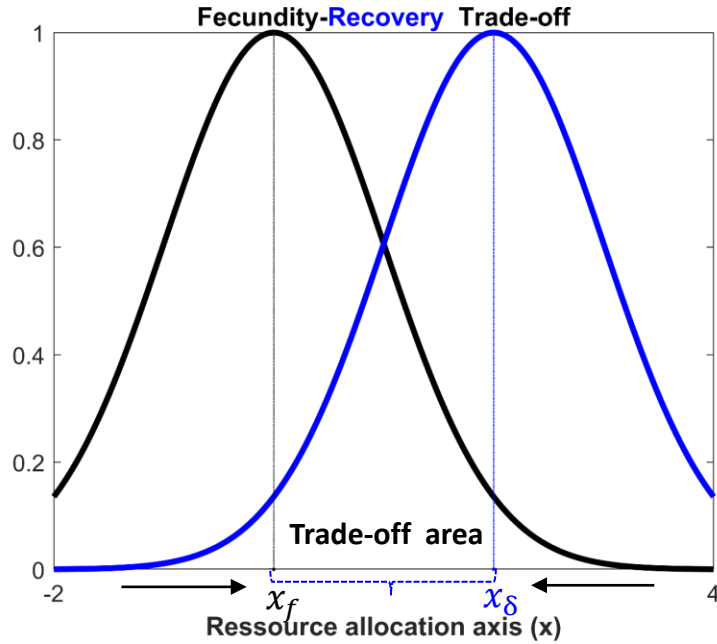
δ : Recovery rate.

θ : Rate of immunity loss

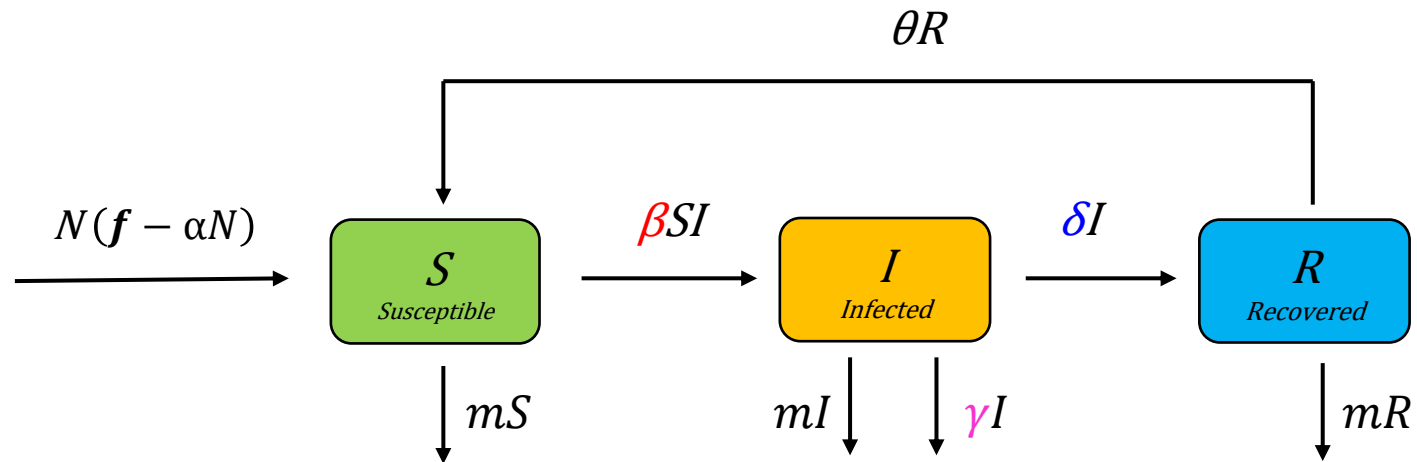
Fecundity - Immunity Trade-off



Fecundity - Immunity Trade-off



The epidemic model



$$\frac{dS}{dt} = N(f - \alpha N) - \beta SI - mS + \theta R$$

$$\frac{dI}{dt} = \beta SI - (\gamma + \delta + m)I$$

$$\frac{dR}{dt} = \delta I - (\theta + m)R$$

$$N = S + I + R$$

$$R_0 = \frac{\beta}{\gamma + \delta + m} * \frac{f - m}{\alpha}$$

f : Fecundity of the species.

α : Inter – specific competition of the species.

β : Pathogen transmission

m : Natural mortality rate.

γ : Virulence (Pathogen – induced death rate).

δ : Recovery rate.

θ : Rate of immunity loss

Eco – evolutionary dynamics

Adaptive Dynamics

Ecological dynamics – SIR model

$$\begin{aligned}\frac{dS}{dt} &= N(f(x) - \alpha N) - mS - \beta(x)SI + \theta R \\ \frac{dI}{dt} &= \beta(x)SI - (\gamma(x) + \delta(x) + m)I \\ \frac{dR}{dt} &= \delta(x)I - (\theta + m)R\end{aligned}$$

Invasion fitness of the rare mutant host
 x_m *in a resident population at*
Ecological Equilibrium x
 $\omega(x_m, x)$

Ecology *Eco – Evo*
Dynamics Evolution

Evolutionary dynamics

$$\frac{dx}{dt} = \frac{1}{2} \mu \sigma^2 N^*(x) \frac{\partial \omega(x_m, x)}{\partial x_m} \Bigg|_{x_m \rightarrow x}$$

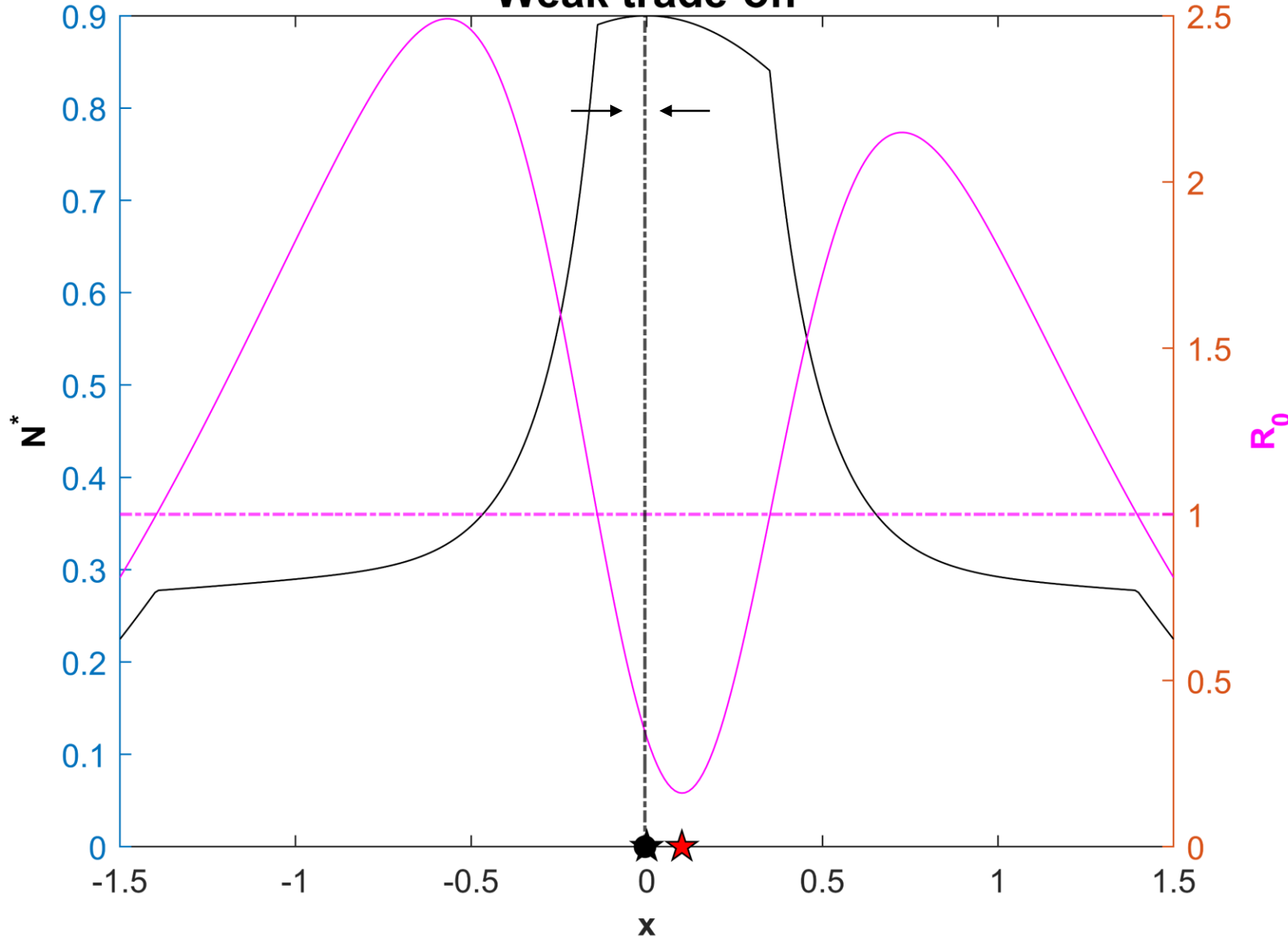
1 – Large population size

2 – Clonal reproduction

3 – Rareness, randomness, smoothness
and small effects of the mutations

Fecundity - **Transmission** Trade-off

Weak trade-off

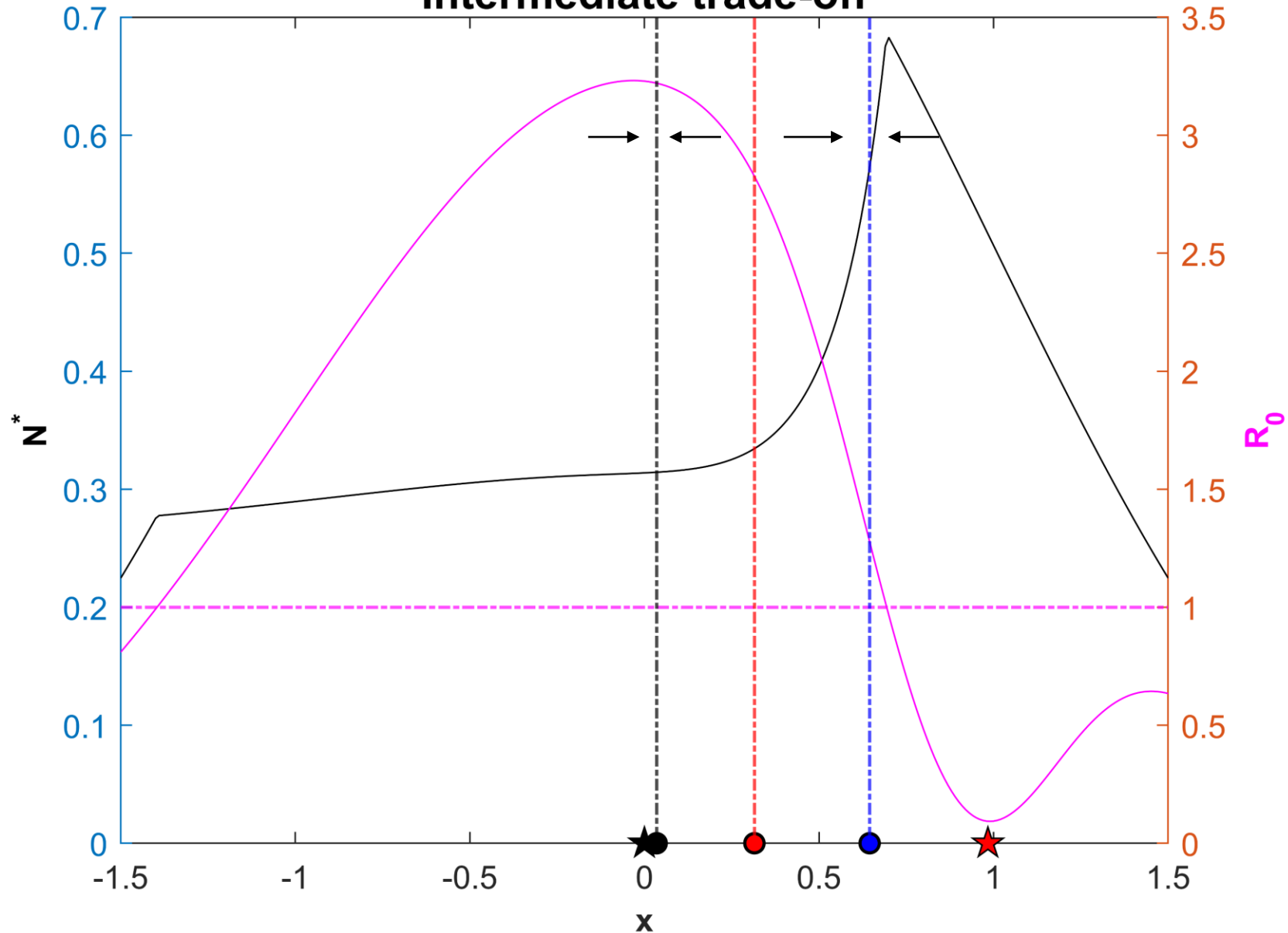


-Evolution maximizes fecundity.

-Pathogen will go extinct.

Fecundity - **Transmission** Trade-off

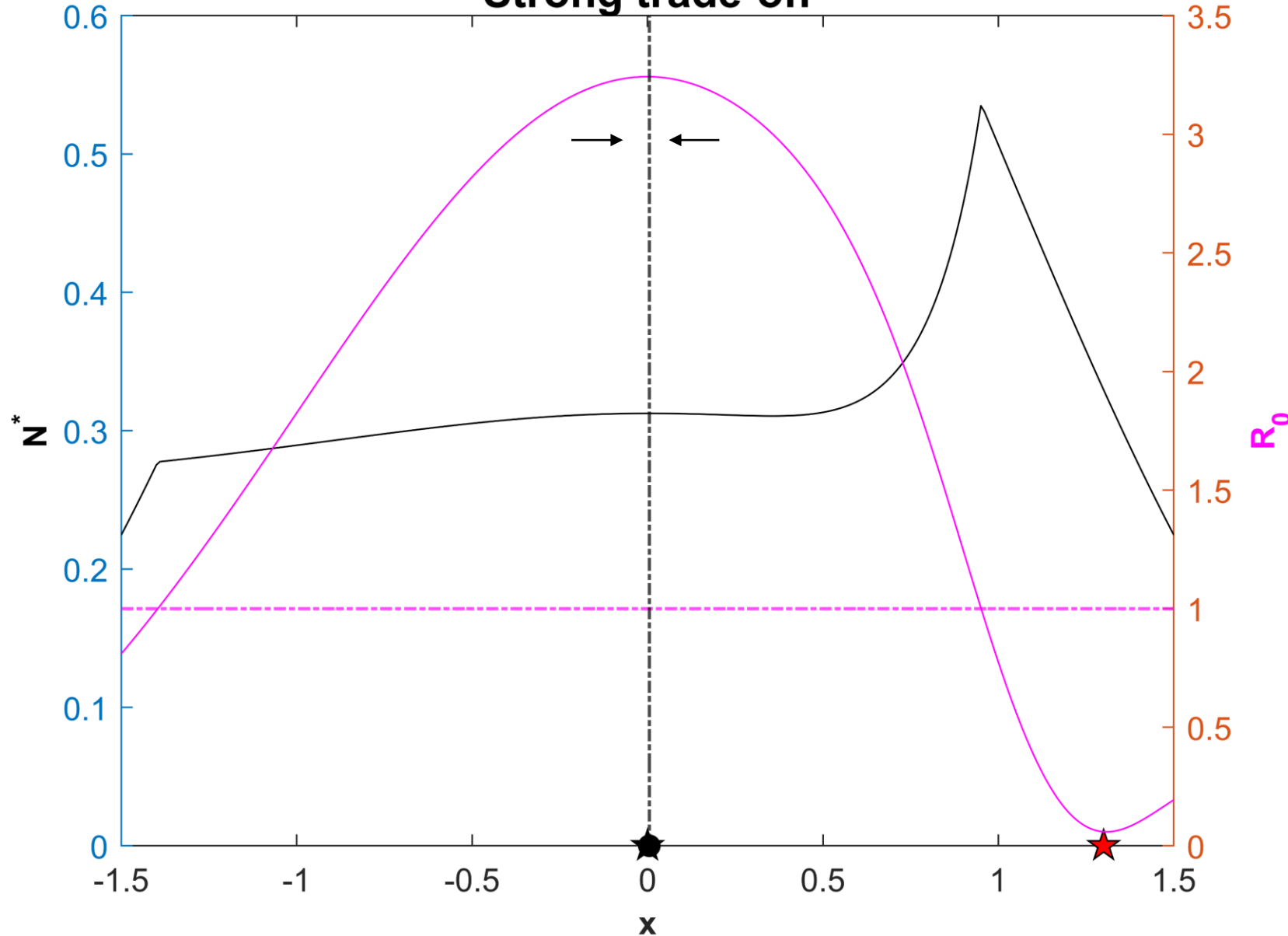
Intermediate trade-off



-2 alternative strategies (1 CSS and 1 branching)

Fecundity - **Transmission** Trade-off

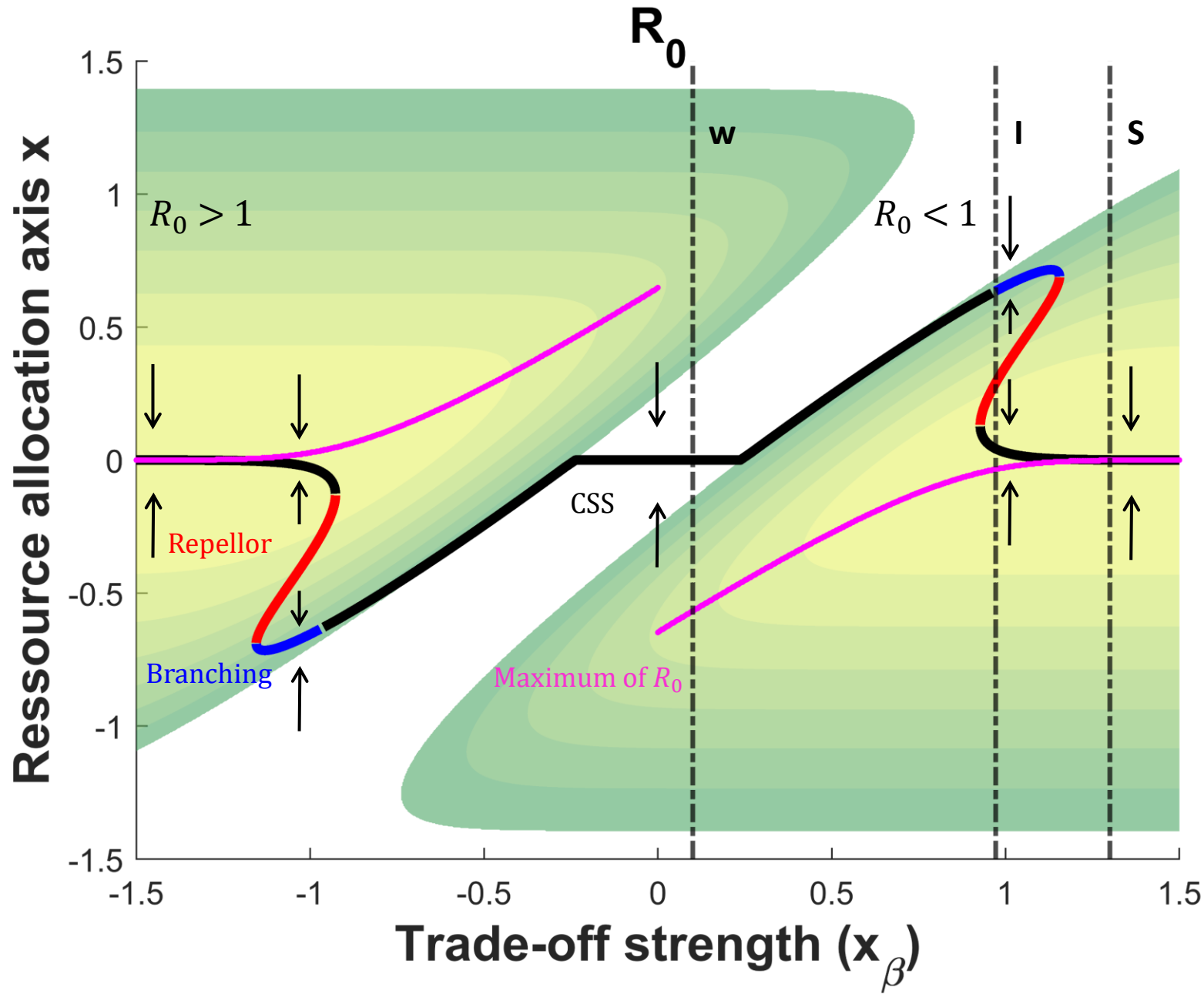
Strong trade-off



-Evolution maximizes fecundity.

-Disease propagation is the highest.

Fecundity - **Transmission** Trade-off (E3)



Weak trade-off

- Evolution maximizes fecundity.
- Pathogen goes extinct.

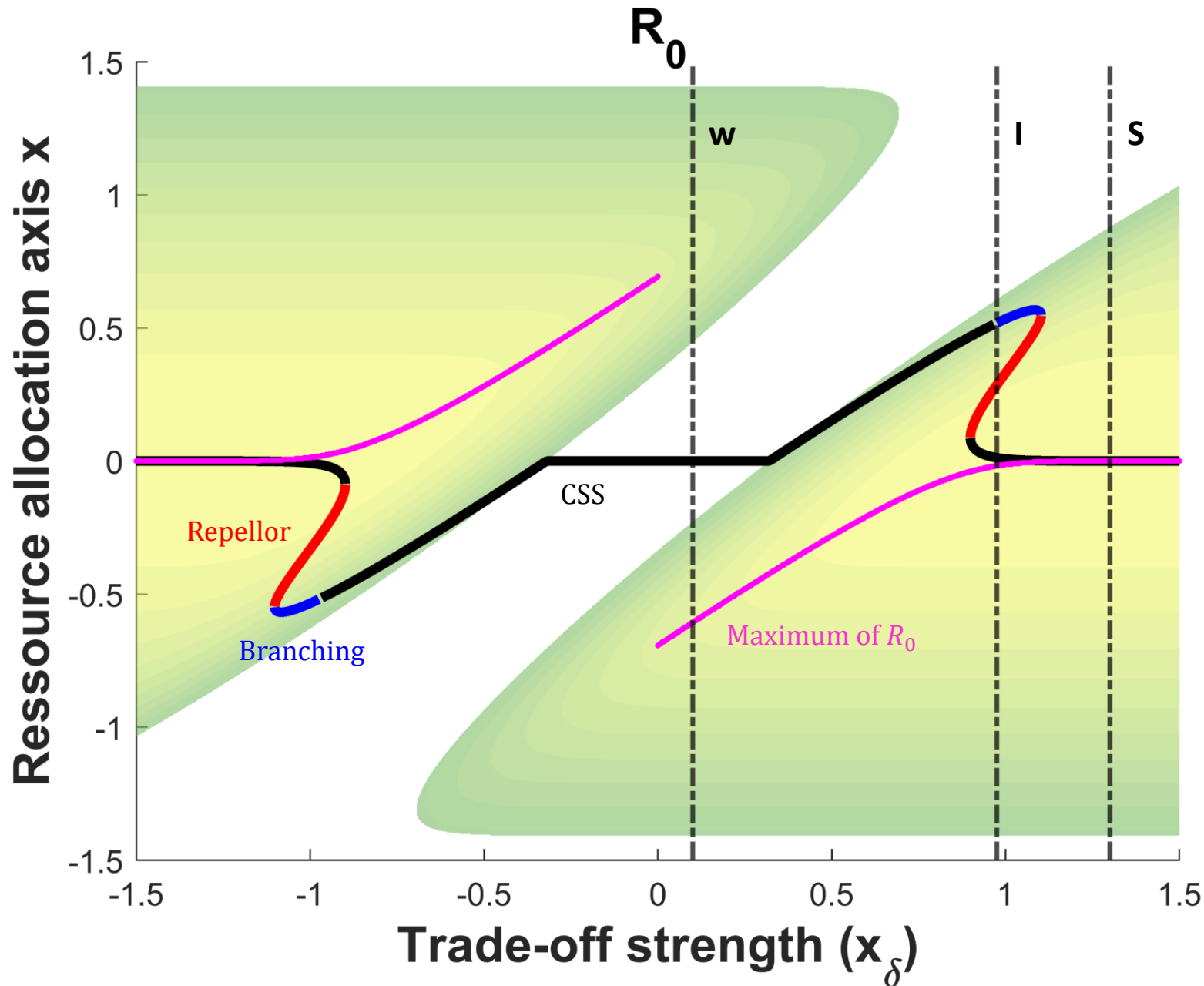
Intermediate trade-off

- 2 alternative strategies

Strong trade-off

- Evolution maximizes fecundity.

Fecundity - Recovery Trade-off



Weak trade-off

- Evolution maximizes fecundity.
- Pathogen goes extinct.

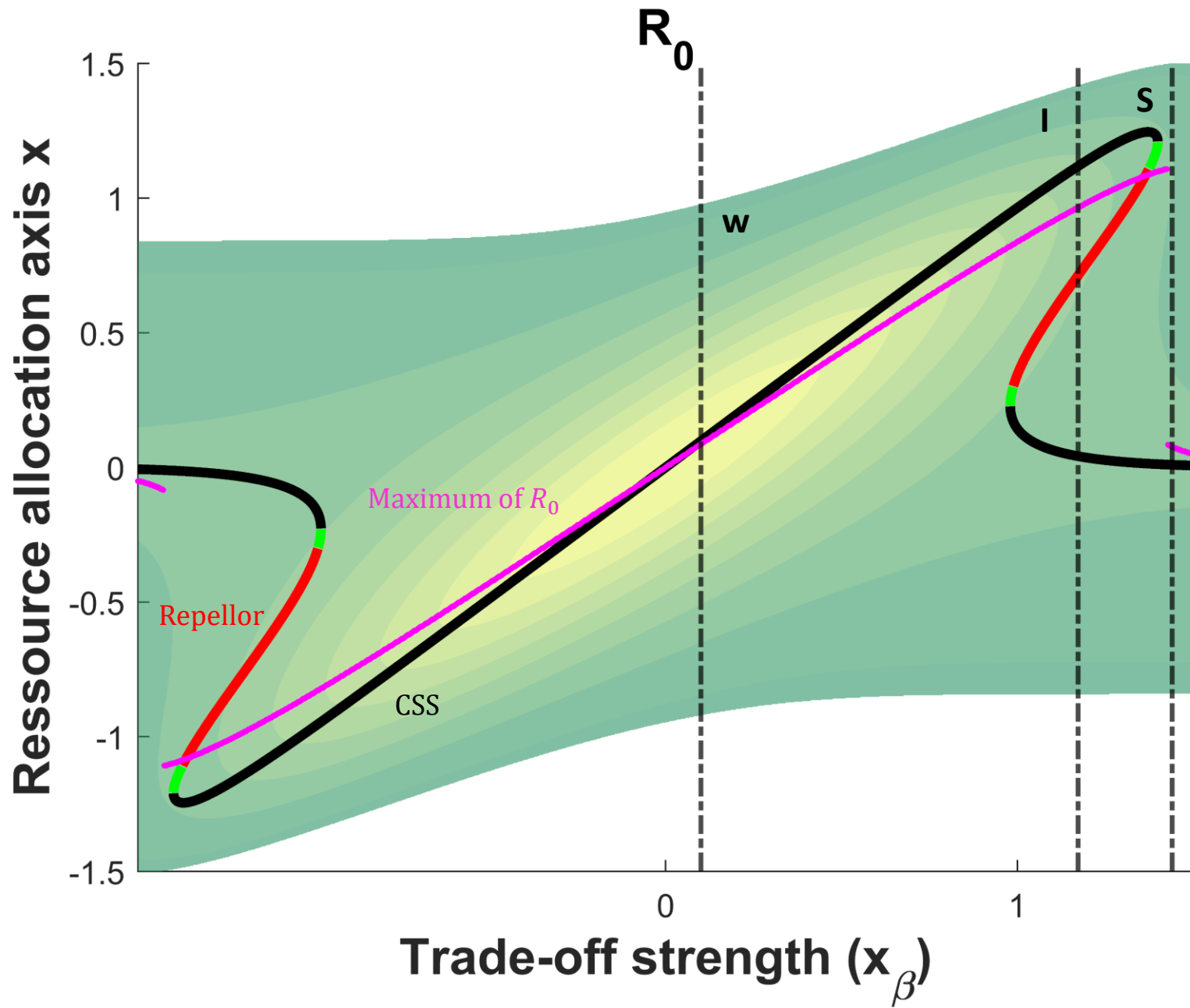
Intermediate trade-off

- 2 alternative strategies

Strong trade-off

- Evolution maximizes fecundity.

Fecundity - Virulence Trade-off



Weak trade-off

-Evolution maximizes fecundity.

Intermediate trade-off

-2 alternative strategies (2 CSS)

Strong trade-off

-Evolution maximizes fecundity.

Discussion

Fecundity - **Transmission**
Trade-off

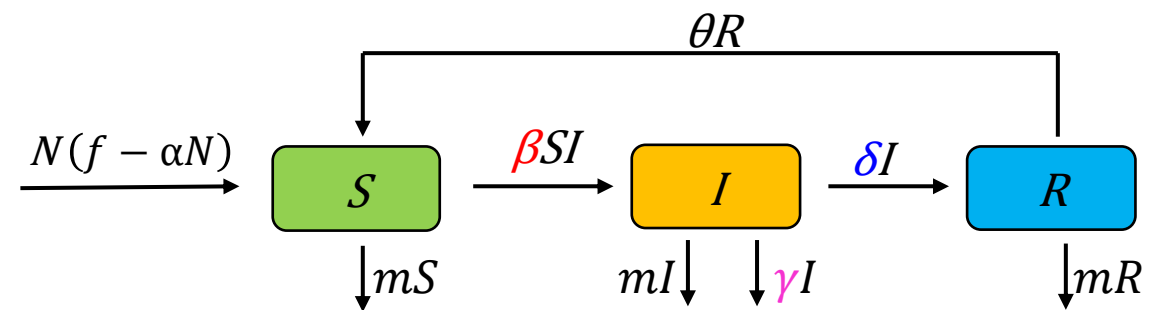
Fecundity - **Recovery**
Trade-off

Fecundity - **Virulence**
Trade-off

Resistance
mechanisms

Same
evolutionary
outcomes

Tolerance mechanism



Follow up questions

What are the conditions of diversification ?

Is diversity maintained in the system?

Is subsequent diversification events possible?

Thank you for your attention!

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