

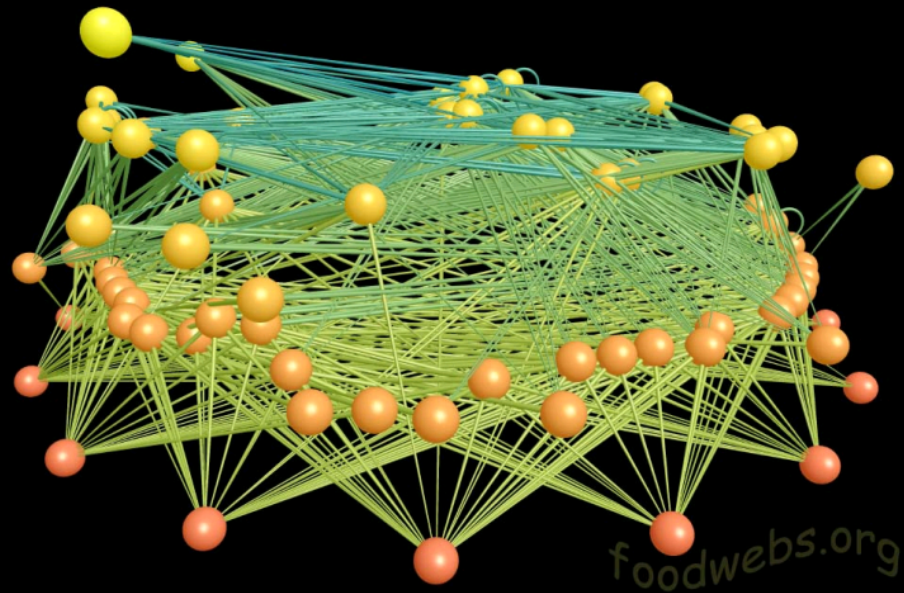
# The structure and stability of networks with antagonistic and mutualistic interactions

FONTAINE, Colin<sup>2</sup>  
THEBAULT, Elisa<sup>1</sup>  
SAUVE, Alix<sup>1,2</sup>

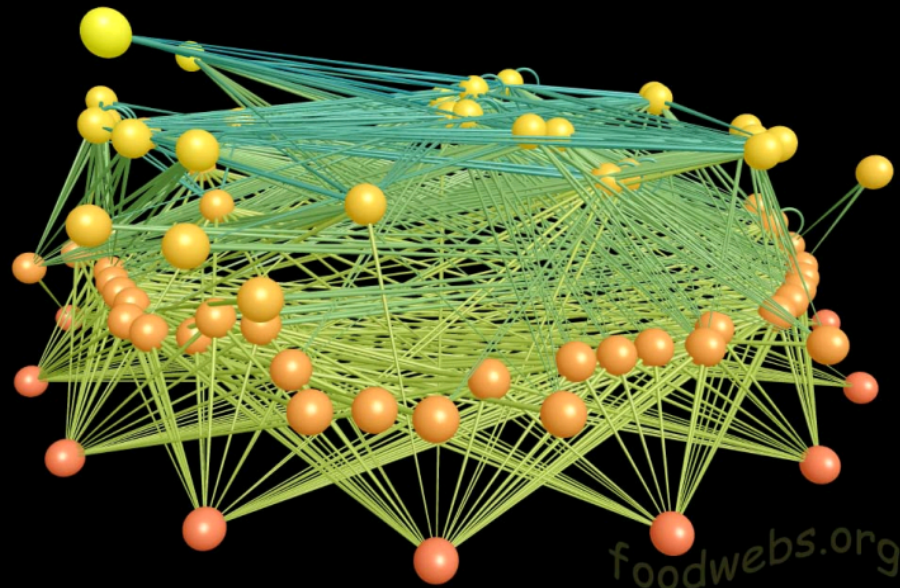
1 CNRS - Bioemco, Paris, France

2 Museum National d'Histoire Naturelle, Paris, France





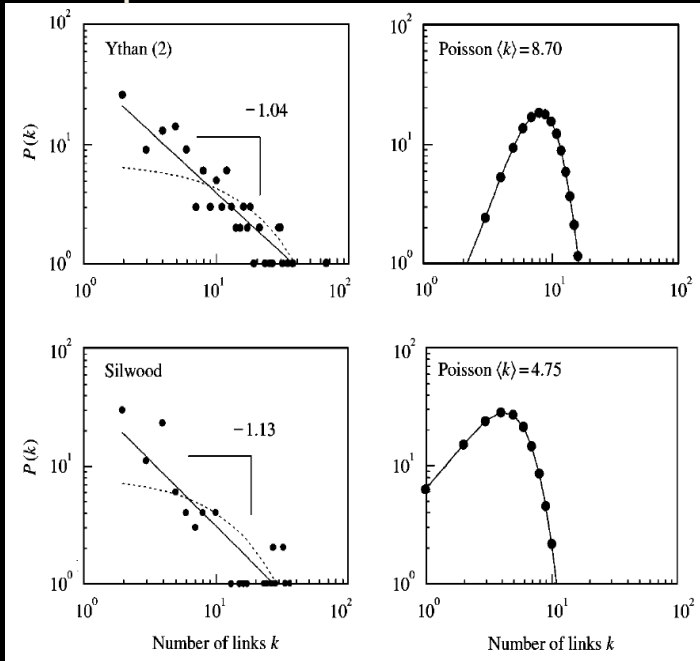
foodwebs.org

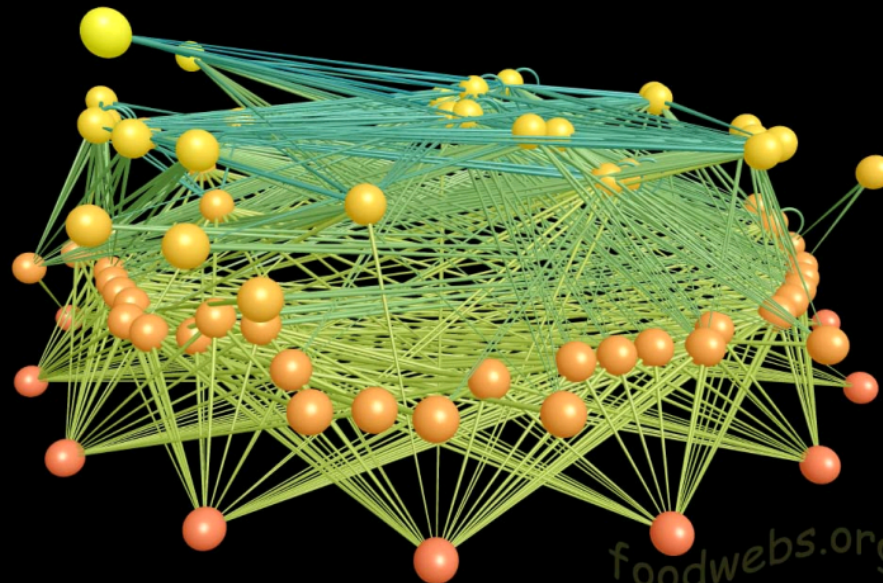


# Structure

Empirical data

Random data





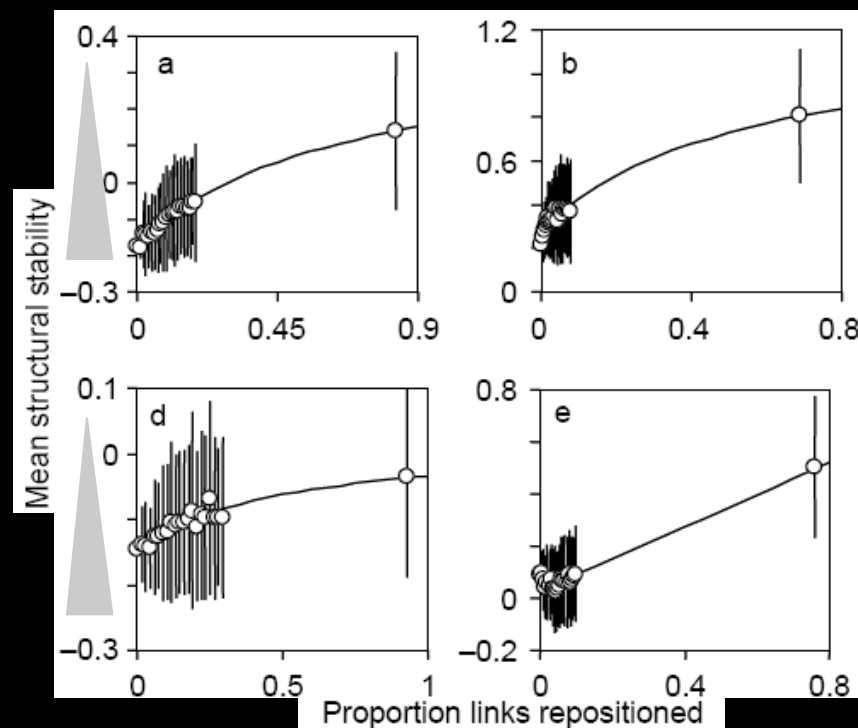
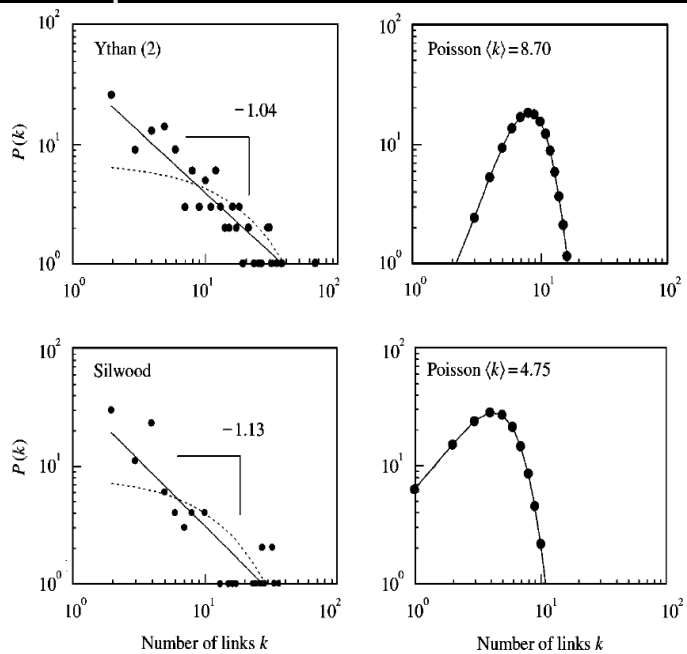
**Structure**



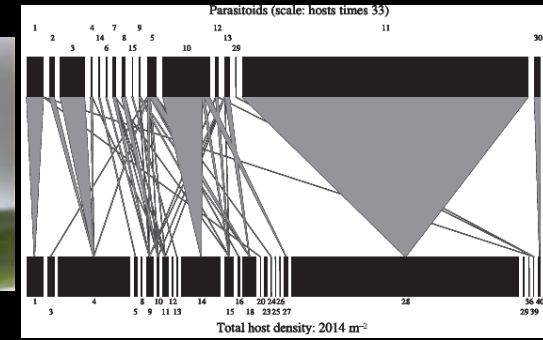
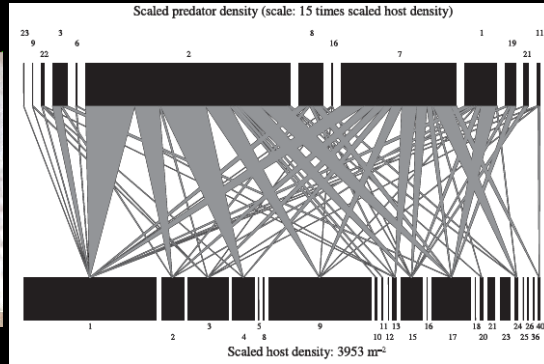
**Stability**

Empirical data

Random data



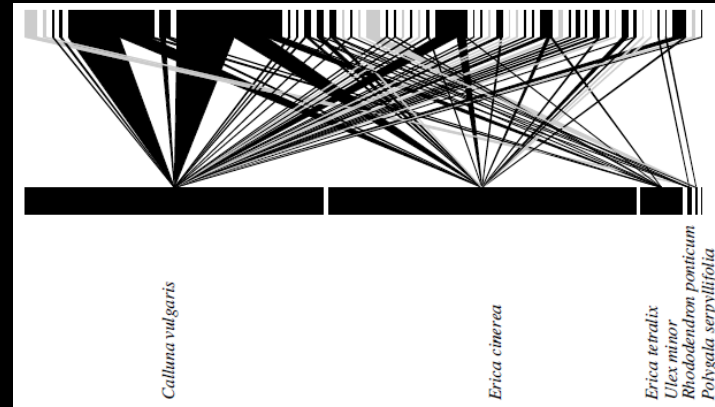
# Diversity of interaction types



Structure



Stability



# I. Comparing networks with mutualistic and antagonistic interactions

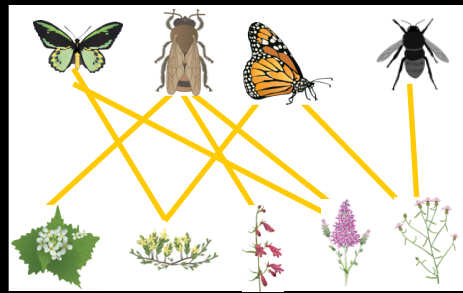
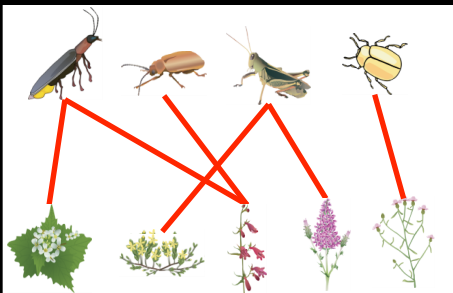
**Structure**



**Stability**

*Differences between  
herbivory & pollination  
networks?*

*Consequences  
on species coexistence  
and stability?*



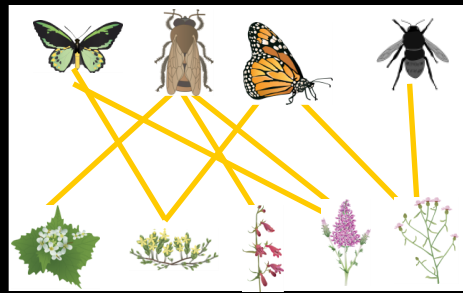
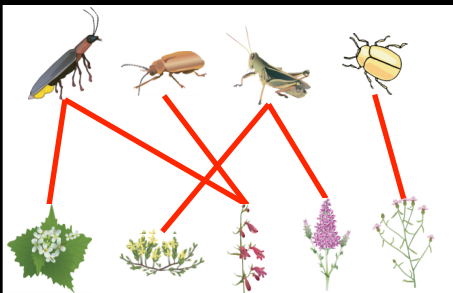
Bascompte et al. *PNAS* 2003

Lewinsohn et al. *Oikos* 2006

# I. Comparing networks with mutualistic and antagonistic interactions

## Structure

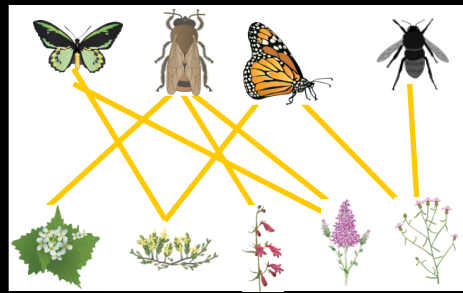
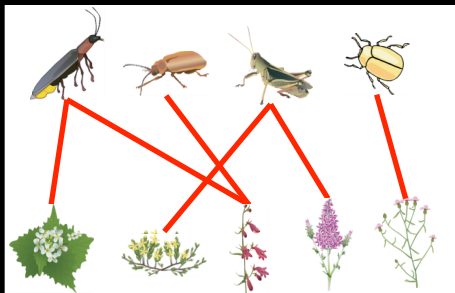
*Differences between  
herbivory & pollination  
networks?*



# I. Comparing networks with mutualistic and antagonistic interactions

## Structure

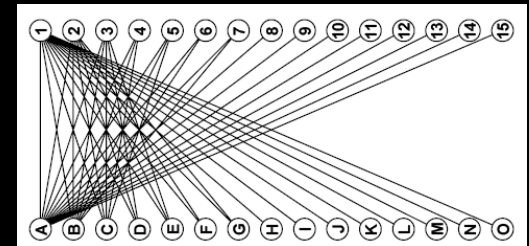
*Differences between herbivory & pollination networks?*



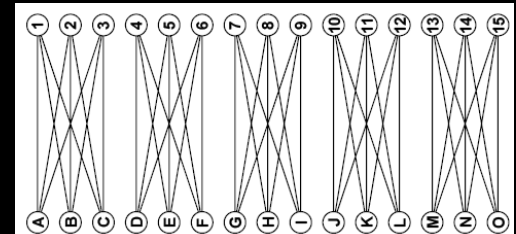
Diversity

Connectance

Nestedness

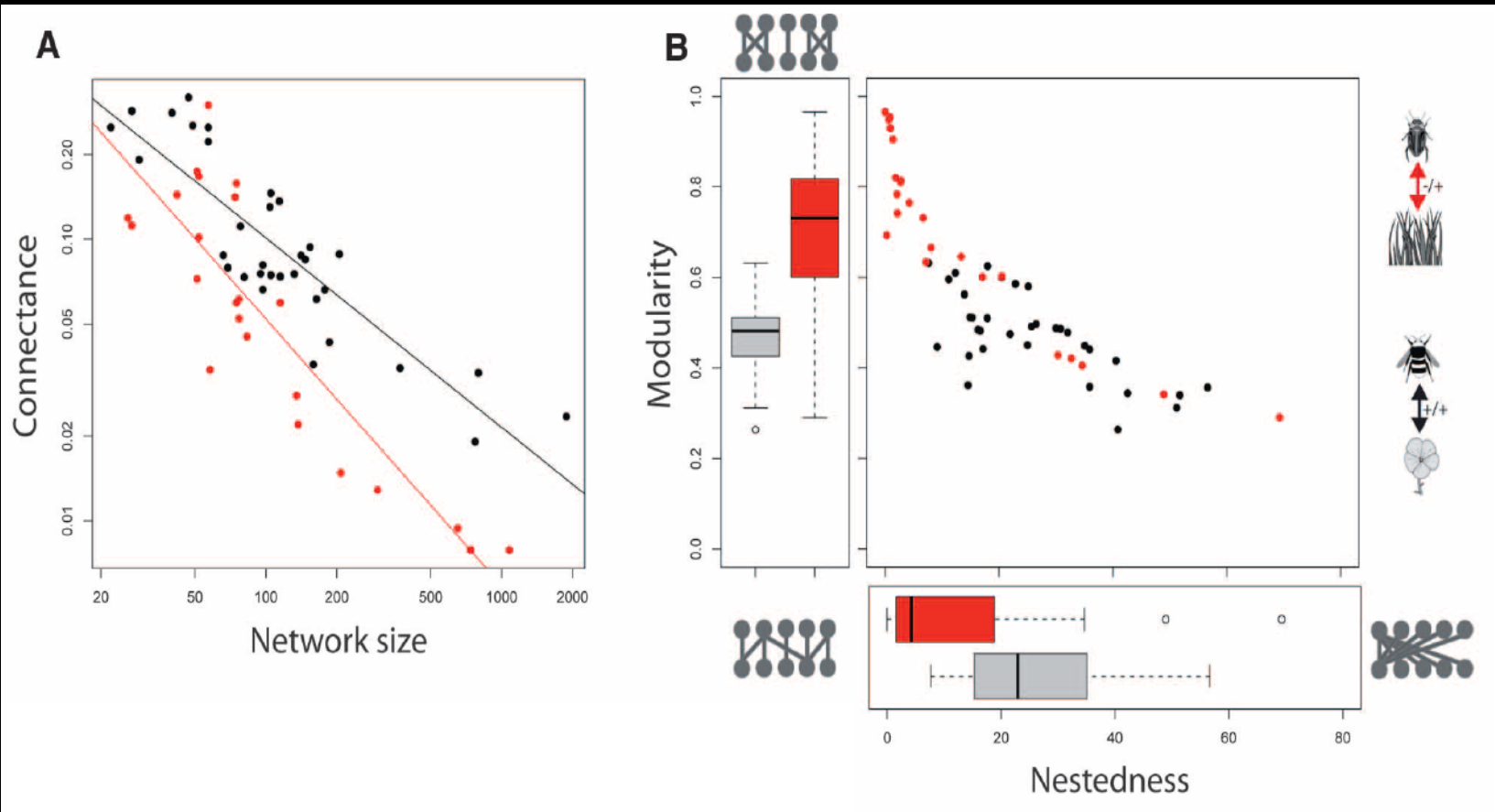


Modularity

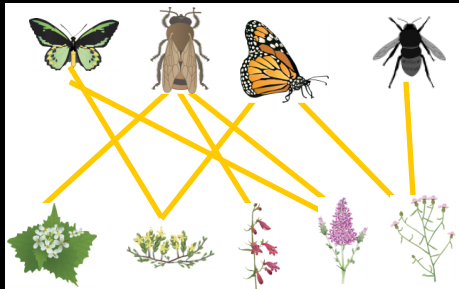




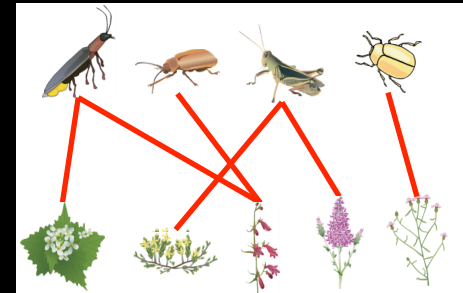
# Network structure and interaction type



# The model: dynamics of mutualistic and trophic webs



Mutualistic



Antagonistic

$$\frac{dA_i}{dt} = r_{A_i} A_i - I_{A_i} A_i^2 + \sum_{j=1}^{N_p} \frac{c_{ji} A_i P_j}{\alpha_{ji}^{-1} + \sum_{P_k \in \text{mut}(A_i)} P_k}$$

$$\frac{dP_i}{dt} = r_{P_i} P_i - I_{P_i} P_i^2 + \sum_{j=1}^{N_a} \frac{c_{ij} A_j P_i}{\alpha_{ij}^{-1} + \sum_{A_k \in \text{mut}(P_i)} A_k}$$

$$\frac{dA_i}{dt} = r_{A_i} A_i - I_{A_i} A_i^2 + \sum_{j=1}^{N_p} \frac{c_{ji} A_i P_j}{\alpha_{ji}^{-1} + \sum_{P_k \in \text{prey}(A_i)} P_k}$$

$$\frac{dP_i}{dt} = r_{P_i} P_i - I_{P_i} P_i^2 - \sum_{j=1}^{N_a} \frac{c_{ij} A_j P_i}{\alpha_{ij}^{-1} + \sum_{P_k \in \text{prey}(A_j)} P_k}$$

-intrinsic growth rates

$r_p$  and  $r_A < 0 \rightarrow$  obligate mutualism

-density dependence term

-interaction term

saturates with mutualistic partner densities

-intrinsic growth rates

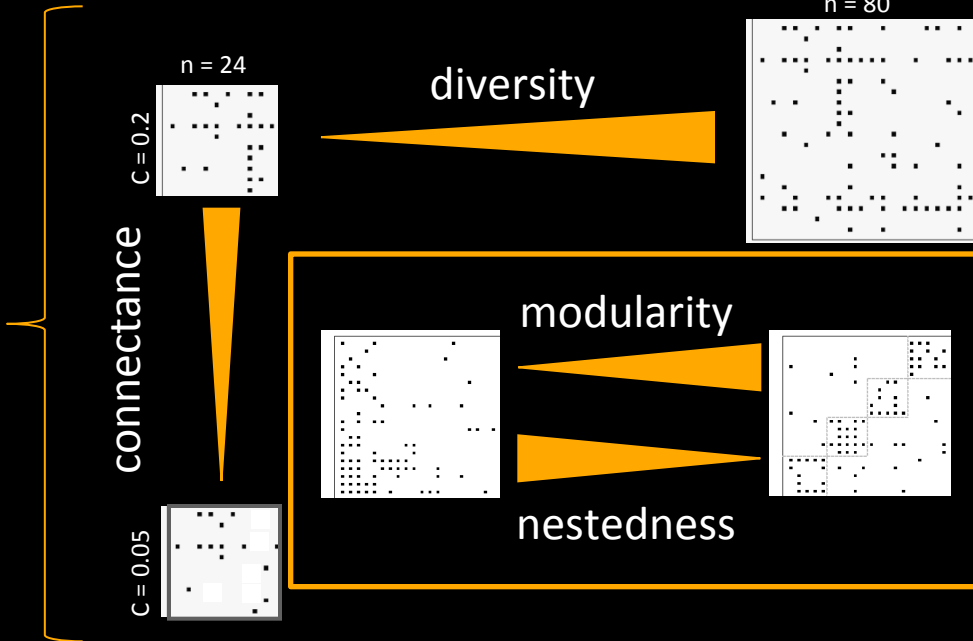
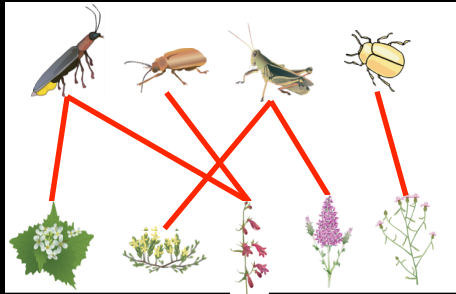
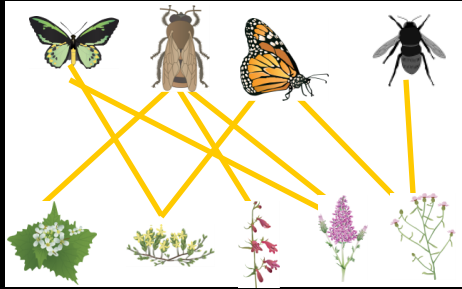
$r_p > 0$  and  $r_A < 0$

-density dependence term

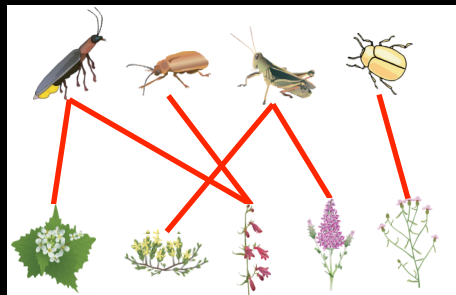
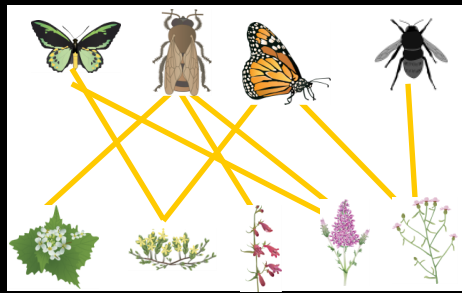
-interaction term

saturates with prey densities

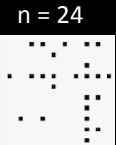
# The model: network structure and stability



# The model: network structure and stability



$C = 0.2$



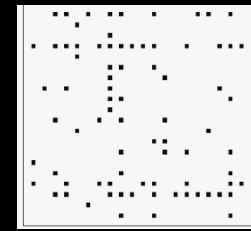
connectance

$C = 0.05$

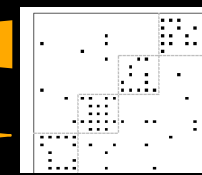
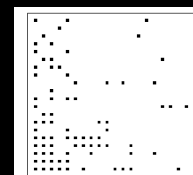


diversity

$n = 80$



modularity



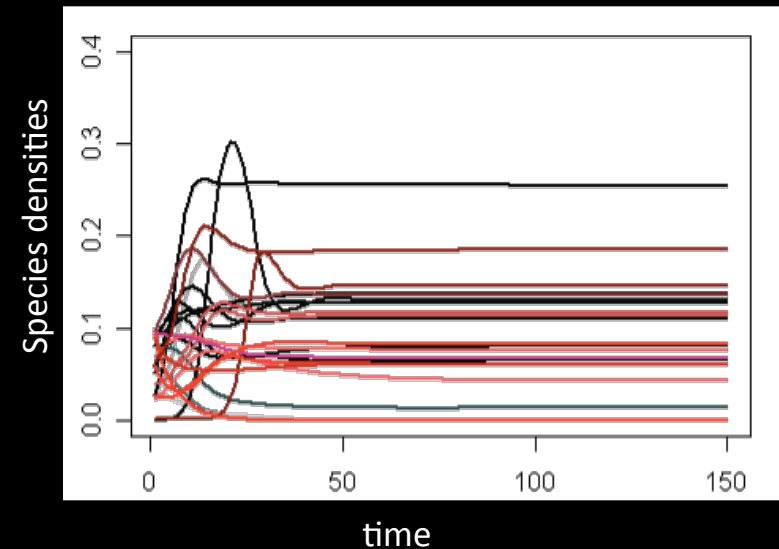
nestedness

## ➤ Persistence:

*proportion of species persisting at the equilibrium*

## ➤ Resilience:

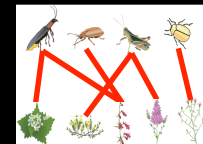
*measure of the speed at which a system returns to its original state after a perturbation*



# Results: impact of network structure on species persistence

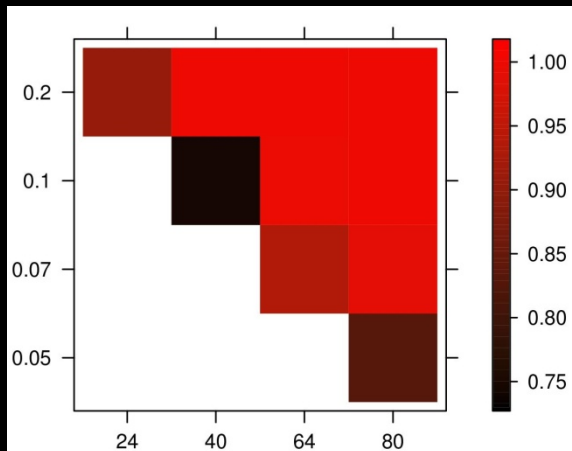


*Mutualistic networks*

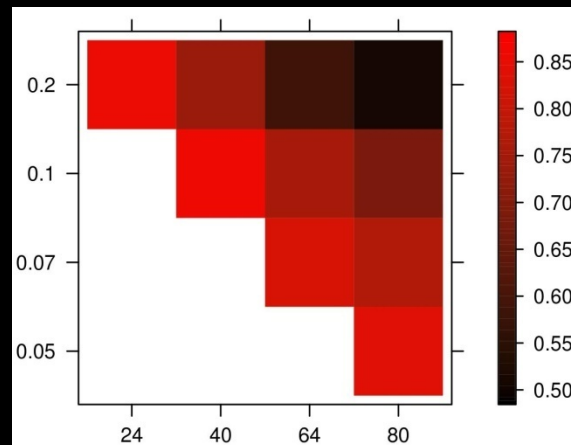


*Antagonistic networks*

Connectance

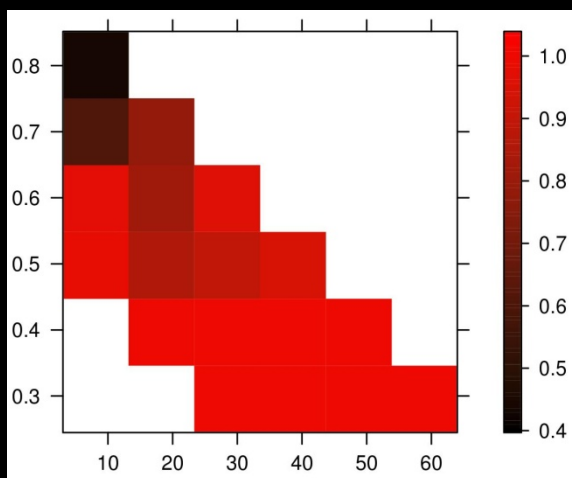


Diversity

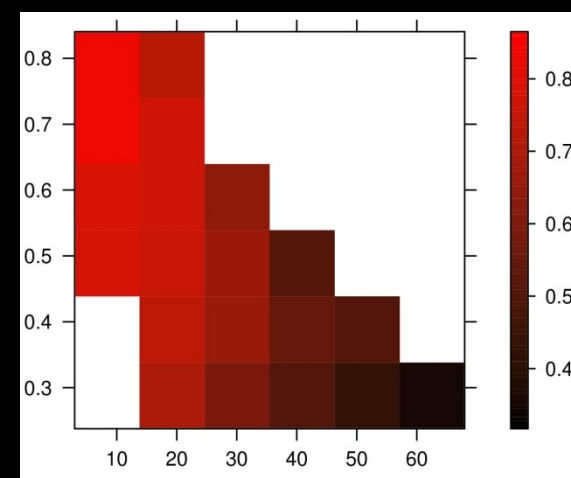


Diversity

Modularity

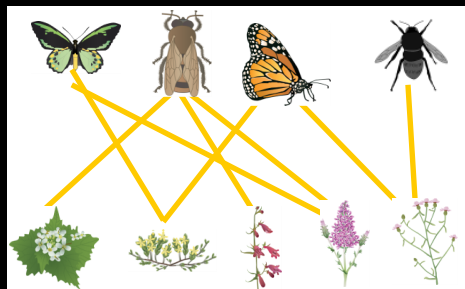


Nestedness

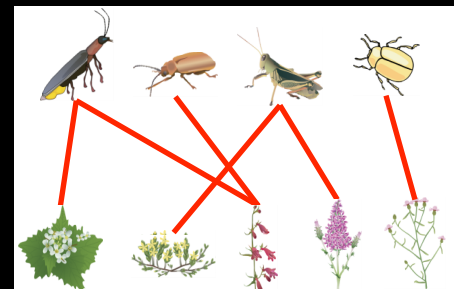


Nestedness

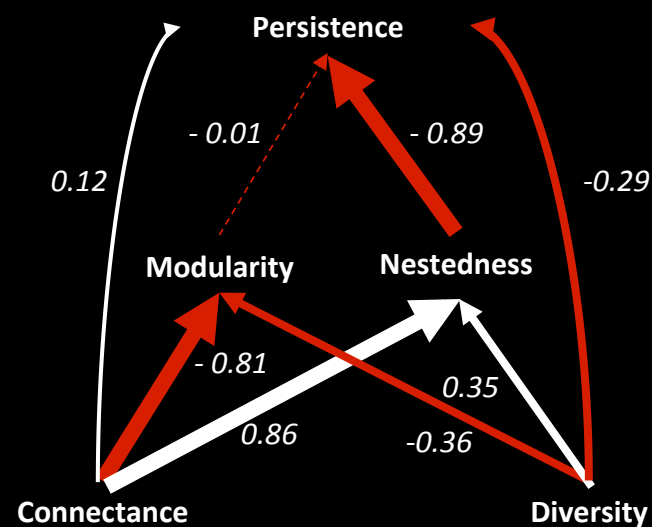
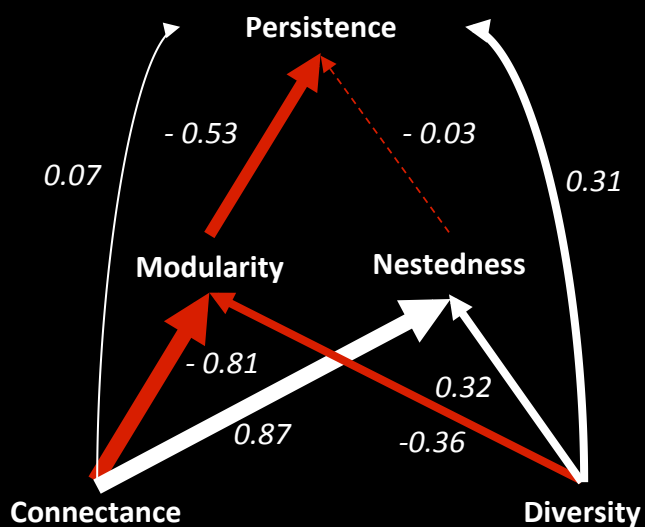
# Results: impact of network structure on species persistence



Mutualistic

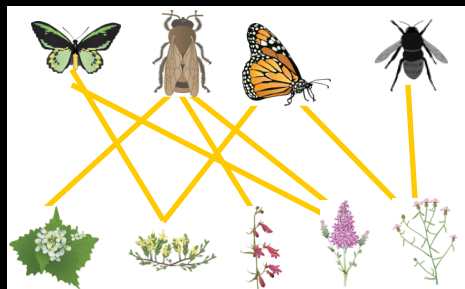


Antagonistic

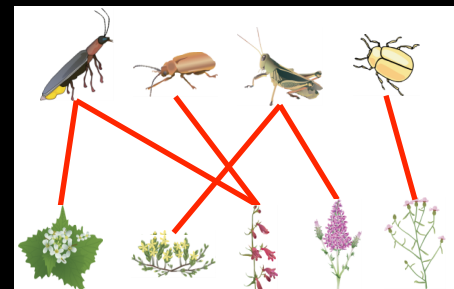


➤ opposite effect of network structure on the persistence of mutualistic and trophic networks

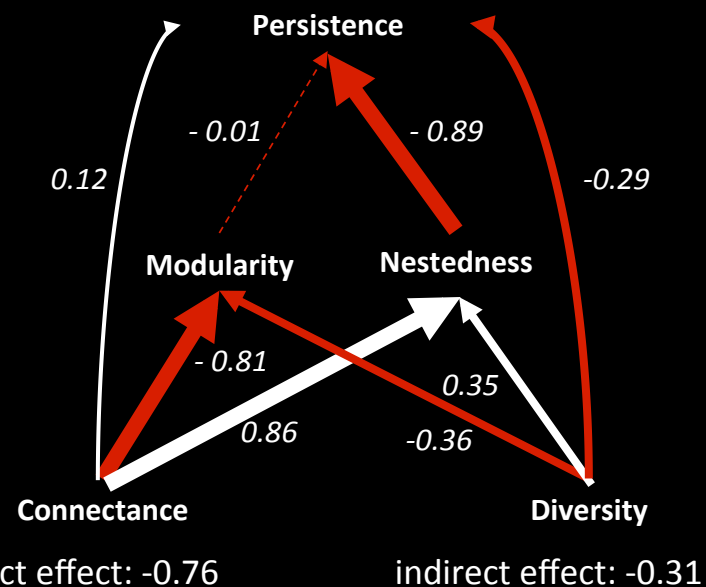
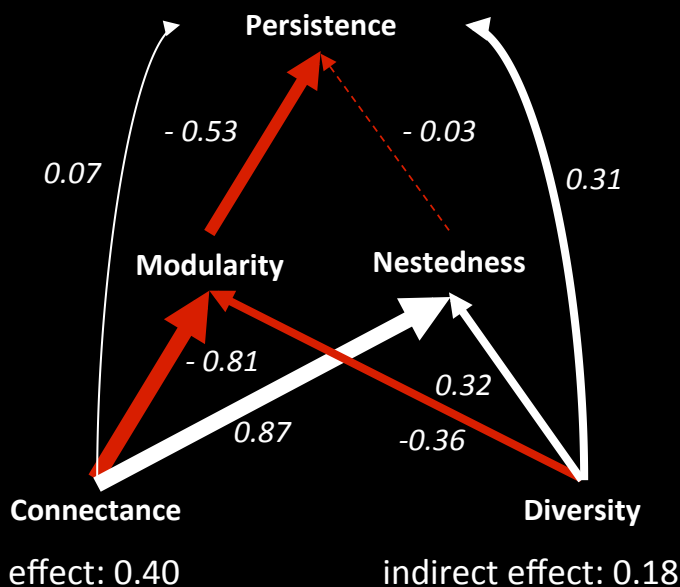
# Results: impact of network structure on species persistence



Mutualistic

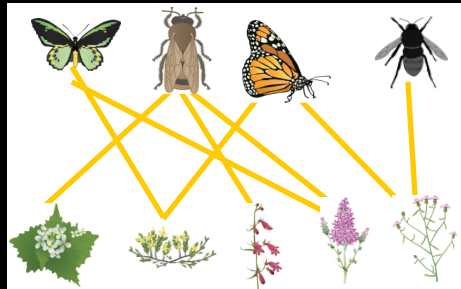


Antagonistic

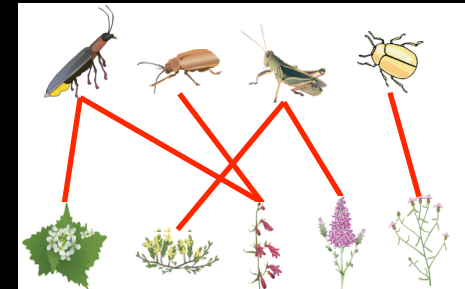


➤ Importance of nestedness and modularity for network stability

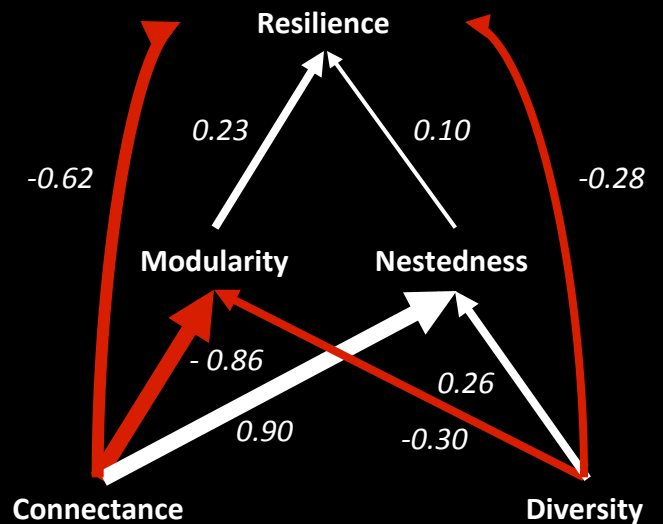
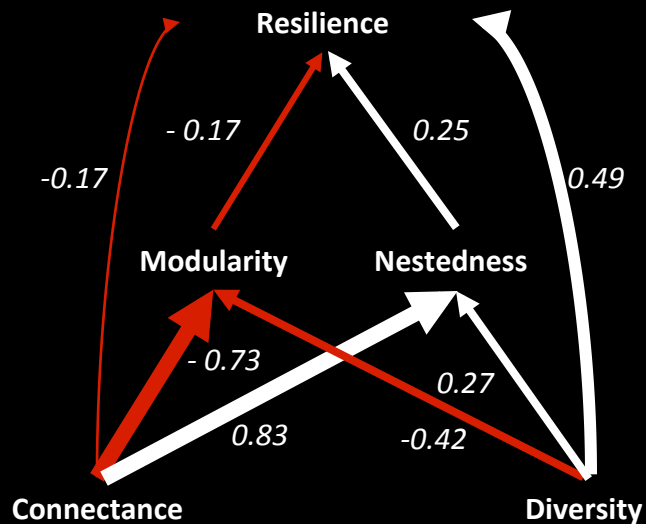
# Results: impact of network structure on resilience



Mutualistic



Antagonistic



➤ opposite effect of network structure on the resilience of mutualistic and trophic networks



# I. Comparing networks with mutualistic and antagonistic interactions

**Structure**



**Stability**

The structure of mutualistic and antagonistic networks seem to differ

Strong effects of network structure on community stability that depends on interaction types

Importance of the fine architecture of interaction networks in determining their stability

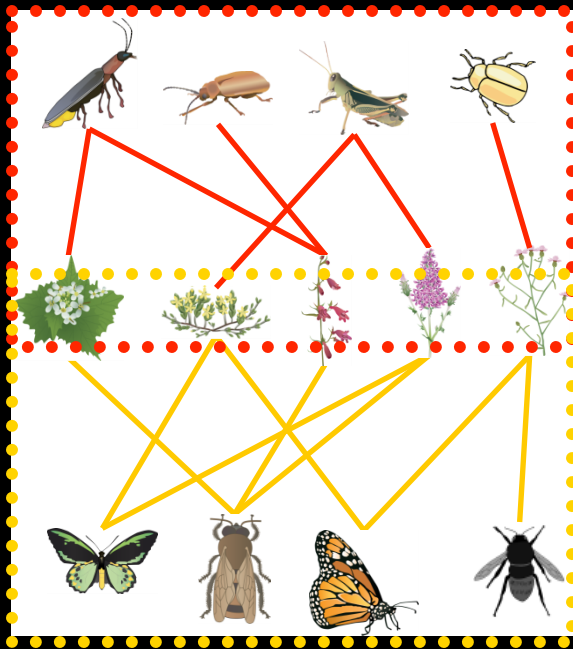
## II. Networks with both mutualistic and antagonistic interactions

**Structure**



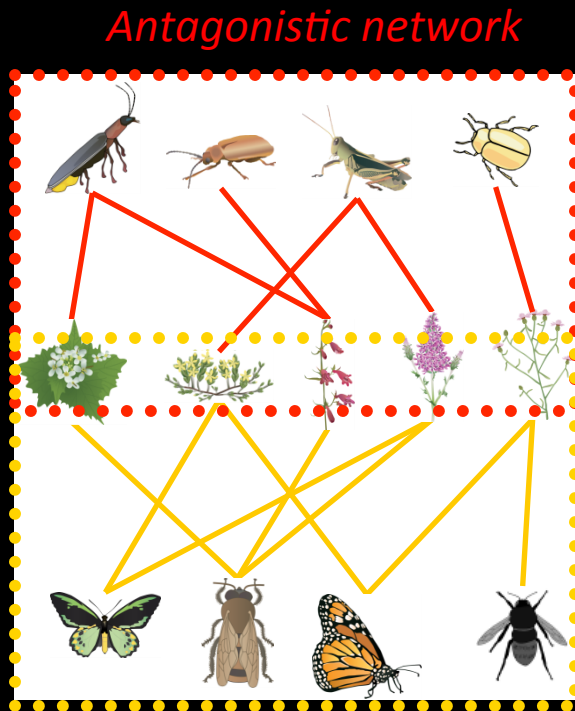
**Stability**

*Structure of networks with interaction type diversity*



*Same consequences on species coexistence and stability than when considered in networks with one interaction type?*

# The model: dynamics with both mutualistic and trophic interactions



Mutualistic network

$$\frac{dH_i}{dt} = r_{Hi}H_i - I_{Hi}H_i^2 + \sum_{j=1}^{Np} \frac{c_{ji}H_iP_j}{\alpha_{ji}^{-1} + \sum_{Pk \in \text{prey}(Hi)} P_k}$$

$$\frac{dM_i}{dt} = r_{Mi}M_i - I_{Mi}M_i^2 + \sum_{j=1}^{Np} \frac{c_{ji}M_iP_j}{\alpha_{ji}^{-1} + \sum_{Pk \in \text{mut}(Mi)} P_k}$$

$$\frac{dP_i}{dt} = r_{Pi}P_i - I_{Pi}P_i^2 + \sum_{j=1}^{Nm} \frac{c_{ij}M_jP_i}{\alpha_{ij}^{-1} + \sum_{Mk \in \text{mut}(Pi)} M_k} - \sum_{j=1}^{Na} \frac{c_{ij}H_jP_i}{\alpha_{ij}^{-1} + \sum_{Pk \in \text{prey}(Hj)} P_k}$$

-intrinsic growth rates

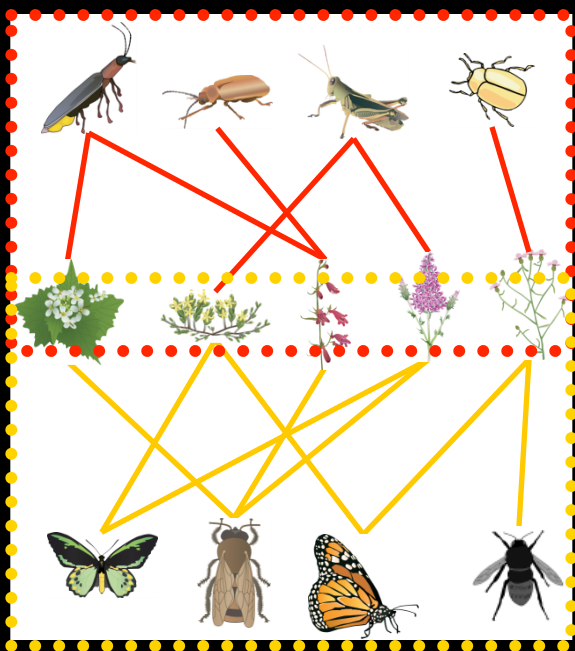
-density dependence term

- mutualistic interaction, saturates with mutualistic partner densities

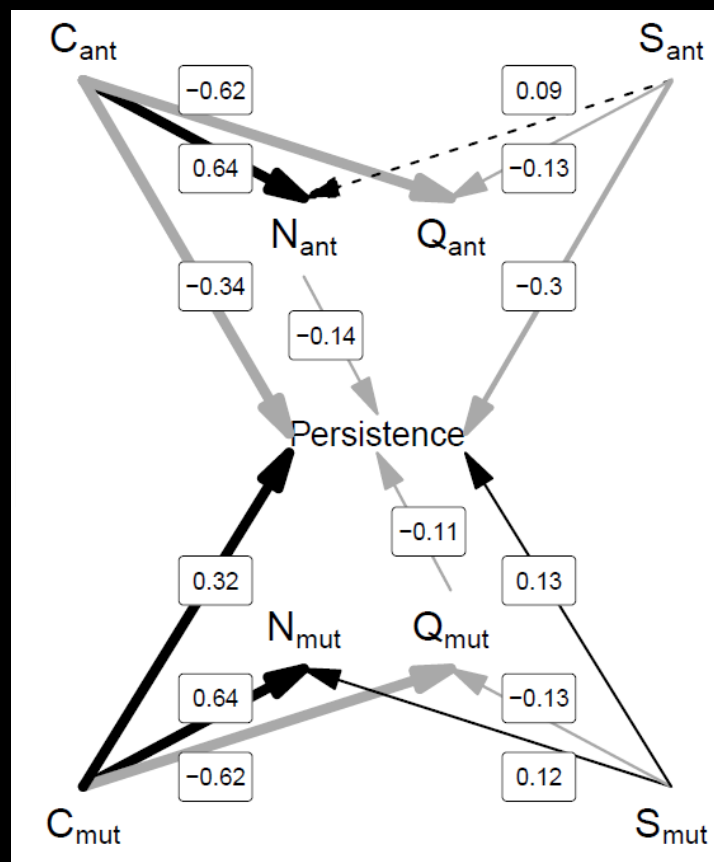
- plant-herbivore interaction term, saturates with prey densities

# Results: impact of network structure on species persistence

Antagonistic network



Mutualistic network

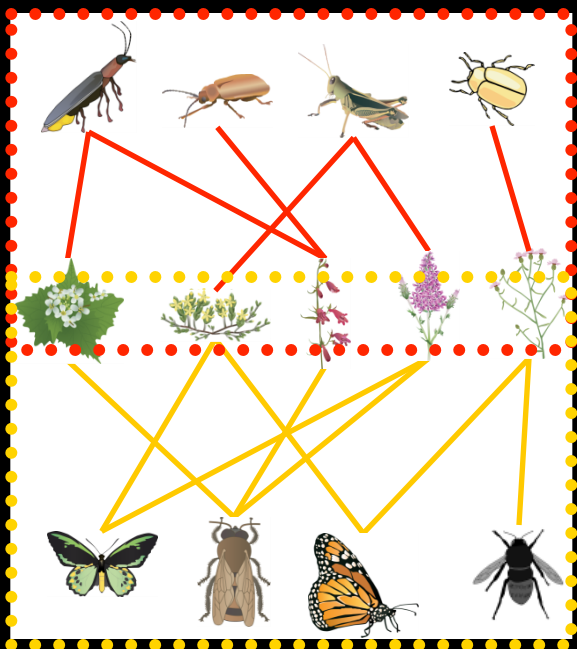


Sauve et al. *Oikos* in press

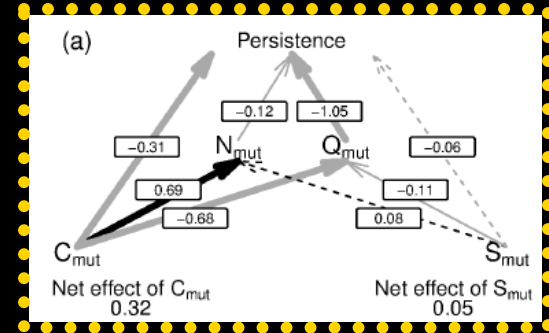
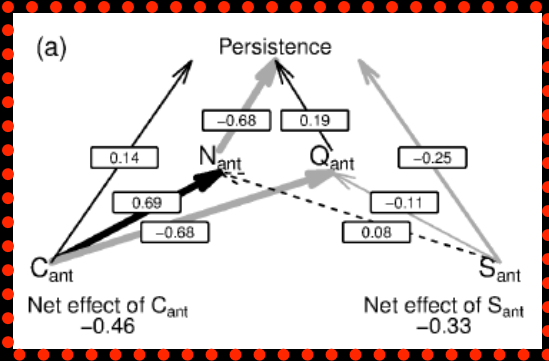
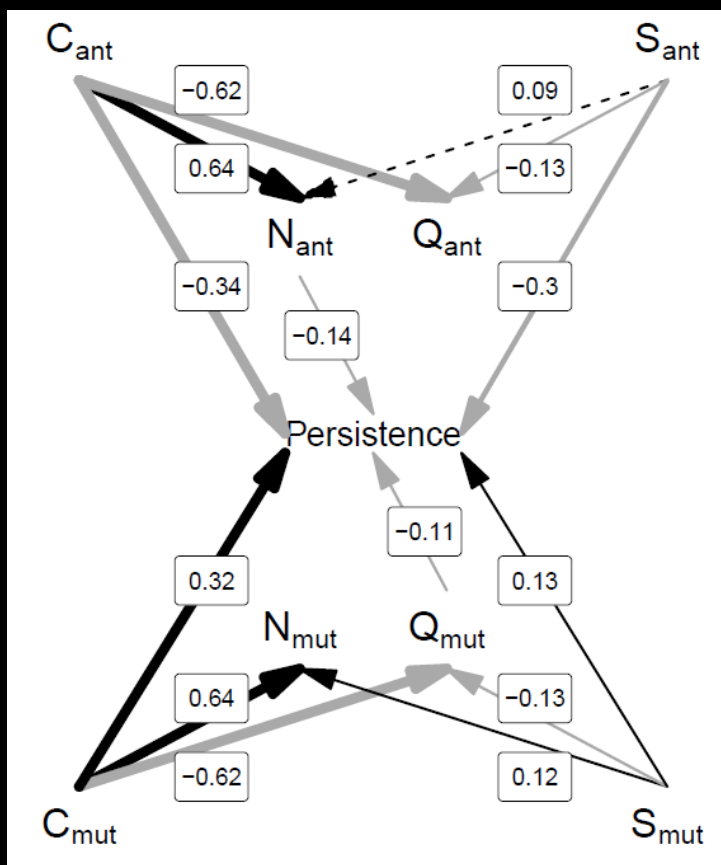
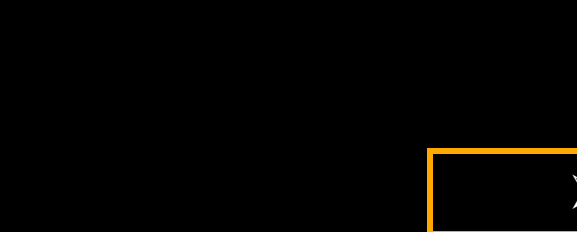
- opposite effect of mutualistic and trophic network structure on the persistence

# Results: impact of network structure on species persistence

Antagonistic network



Mutualistic network

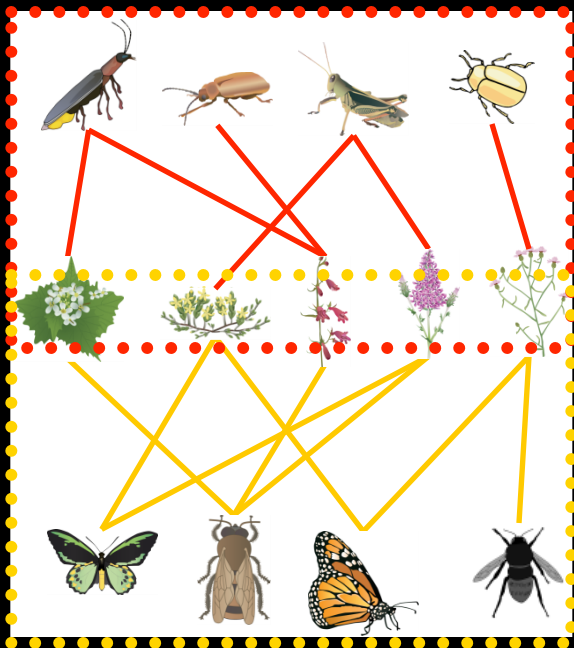


Sauve et al. *Oikos* in press

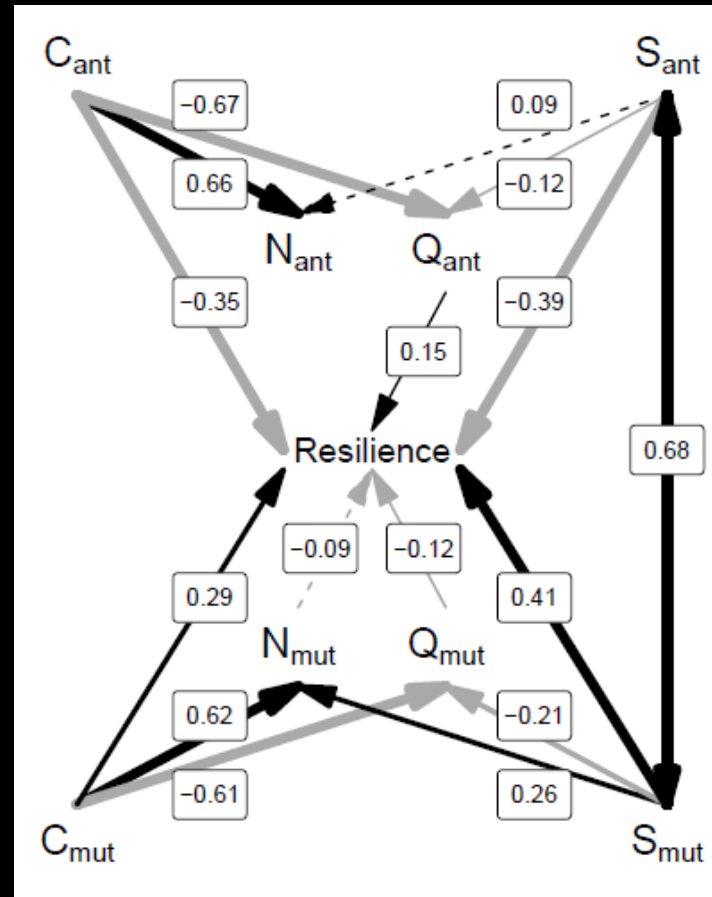
➤ main effects of diversity and connectance

# Results: impact of network structure on resilience

*Antagonistic network*



*Mutualistic network*



Sauve et al. *Oikos* in press

➤ opposite effect of mutualistic and trophic network structure on resilience

## II. Networks with both mutualistic and antagonistic interactions

**Structure**



**Stability**

Effects of diversity and connectance mostly unchanged

Effects of modularity and nestedness strongly weakened

Are structural indices developed for network with a single interaction type relevant to describe network with multiple interaction types?

# Acknowledgments

Most of the interactions networks were provided by the Interaction Web Database (<http://www.nceas.ucsb.edu/interactionweb/index.html>)

Thanks to OT Lewis, J Loye, T Tcharntke, LA Dyer, DH Janzen for information on their datasets, and to JM Olesen and R Guimera for the help provided on modularity

**Thank you for your attention**



