

# Merging mutualistic and antagonistic networks : What consequences for community stability?

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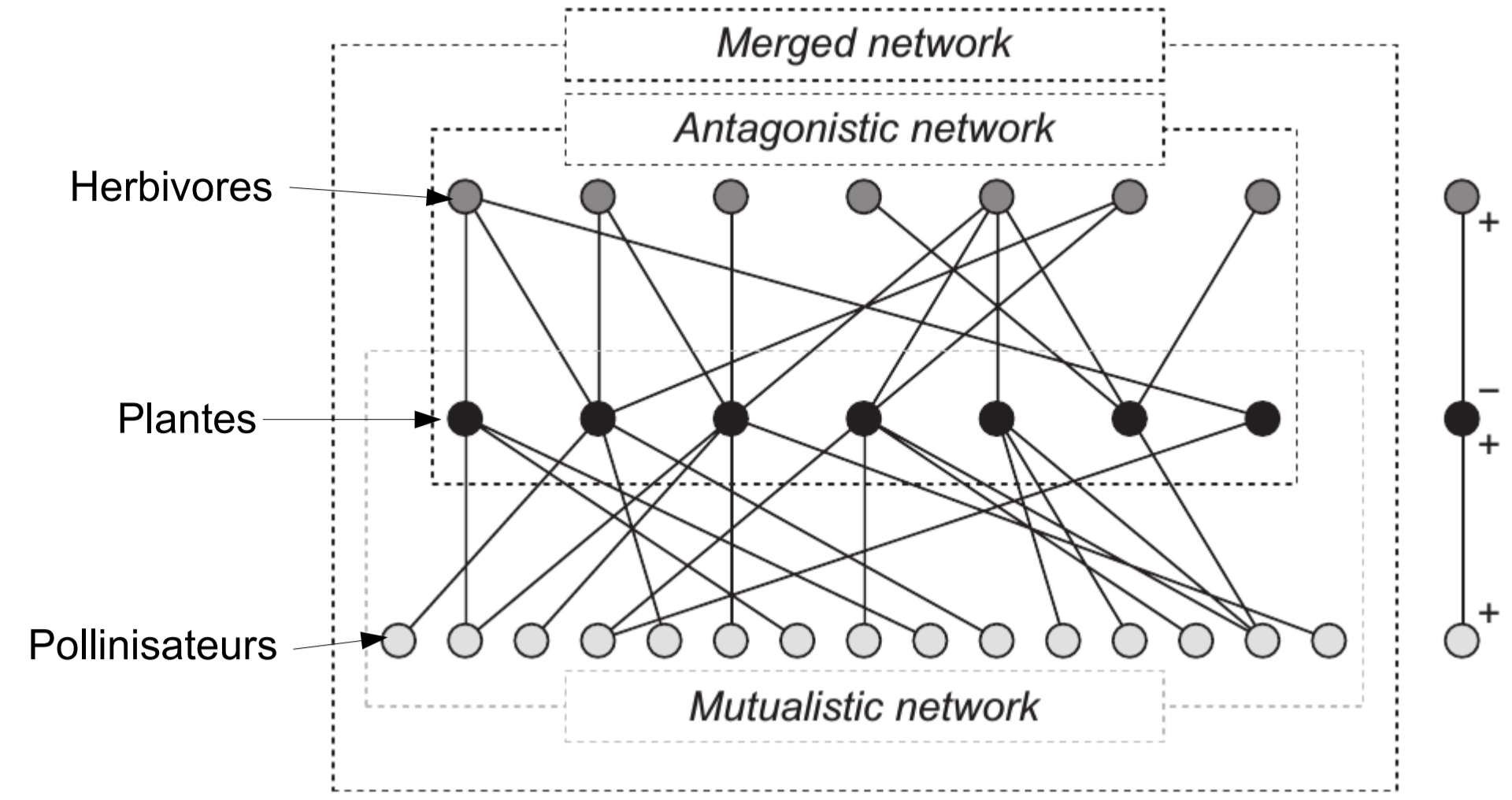
Sauve A. M. C., Fontaine C., Thébault E. (2014) Structure-stability relationships in networks combining mutualistic and antagonistic interactions. *Oikos* 123 (3), 378-384

## INTRODUCTION

In one ecological community, **different types of interactions** occur among species, and define different types of networks that have always been **studied separately**. The structures of these different types of networks affect differently **the response of the communities to disturbance**<sup>1</sup>.

Since these interactions occur together in space and time, it may be more relevant to consider them in **one single framework**<sup>2</sup> which is likely to impact the dynamics of ecological communities.

We suggest to study in a theoretical approach **how interconnecting an antagonistic network and a mutualistic network in a super-network**, illustrated here with a herbivory network and a pollination network, **could change our perception of their dynamics**.



## QUESTIONS

- (i) In a merged network, does the structure of one sub-network affect the persistence of the other?
- (ii) What is the relationship between one sub-network's structure and the whole community persistence?

## MATERIALS & METHODS

Population dynamics' model : To each guild its dynamic

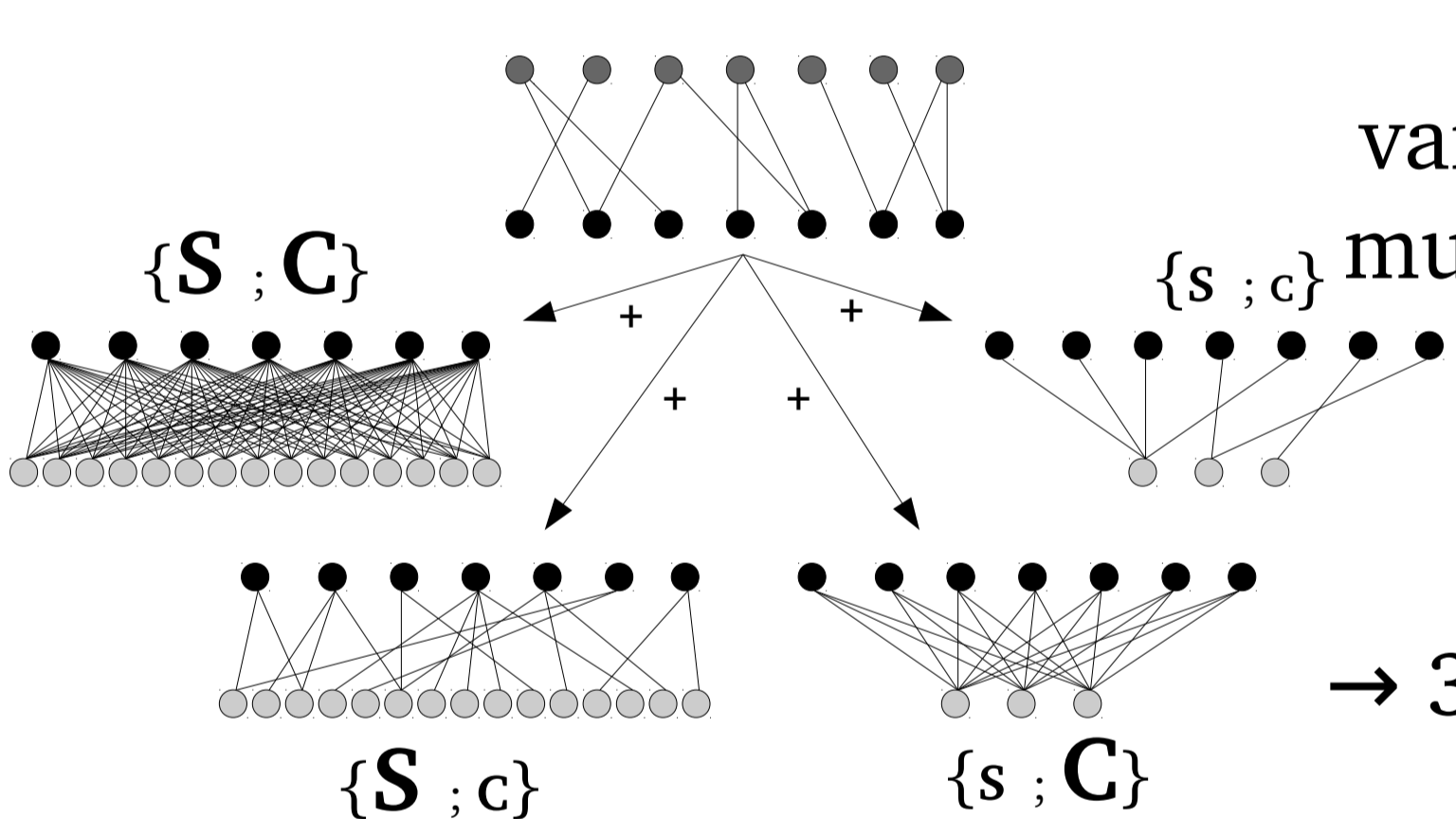
$$\frac{dH_i}{dt} = r_{H_i}H_i - I_{H_i}H_i^2 + \sum_{j=1}^{N_p} \frac{c_{ji}H_jP_j}{\alpha_{ji}^{-1} + \sum_{k \in \text{prey}(H_i)} P_k}$$

$$\frac{dP_i}{dt} = r_{P_i}P_i - I_{P_i}P_i^2 + \sum_{j=1}^{N_m} \frac{c_{ji}M_jP_j}{\alpha_{ji}^{-1} + \sum_{k \in \text{mut}(P_i)} M_k} - \sum_{j=1}^{N_a} \frac{c_{ij}H_jP_i}{\alpha_{ij}^{-1} + \sum_{k \in \text{prey}(P_i)} P_k}$$

$$\frac{dM_i}{dt} = r_{M_i}M_i - I_{M_i}M_i^2 + \sum_{j=1}^{N_m} \frac{c_{ji}M_jP_j}{\alpha_{ji}^{-1} + \sum_{k \in \text{mut}(M_i)} M_k}$$

- Intrinsic growth rate:  $r_p > 0$  et  $r_A < 0$ ,
- Density-dependant self-limitation,
- Functional response to mutualism, saturating with mutualistic partners' densities,
- Holling type II functional response to predation, saturating with preys' densities.

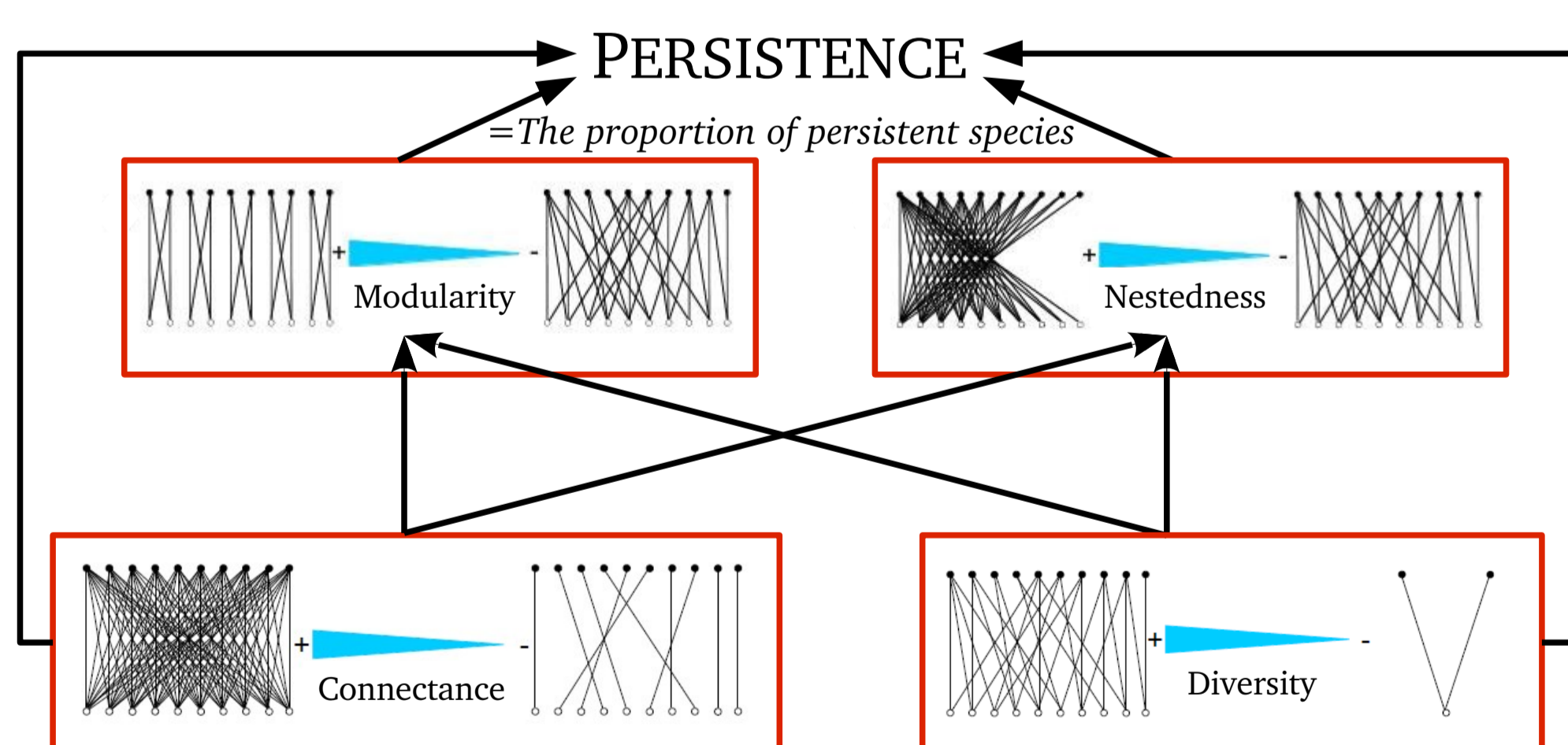
Numerical simulation design



An antagonistic network, with a varying structure is associated with a mutualistic network, initially more or less complex, and vice versa.  
→ 4 cases of complexity  
 $K = S$  (diversity) \*  $C$  (connectance)  
→ 3 cases of interaction strength ratio  
 $c_{ij}^{(mut)}/c_{ij}^{(ant)} = \{0.5, 1, 2\}$

$$K \{2.8, 4.48, 10, 16\} \Leftrightarrow \{S, C\} = \{[40, 0.25], [16, 0.07], [16, 0.25], [40, 0.07]\}$$

Network analysis and relating stability with structure



Correlated measures of network's structure: We perform a *path analysis* according to the model illustrated here.

## RESULTS

In a merged network, does the structure of one sub-network affect the persistence of the other?

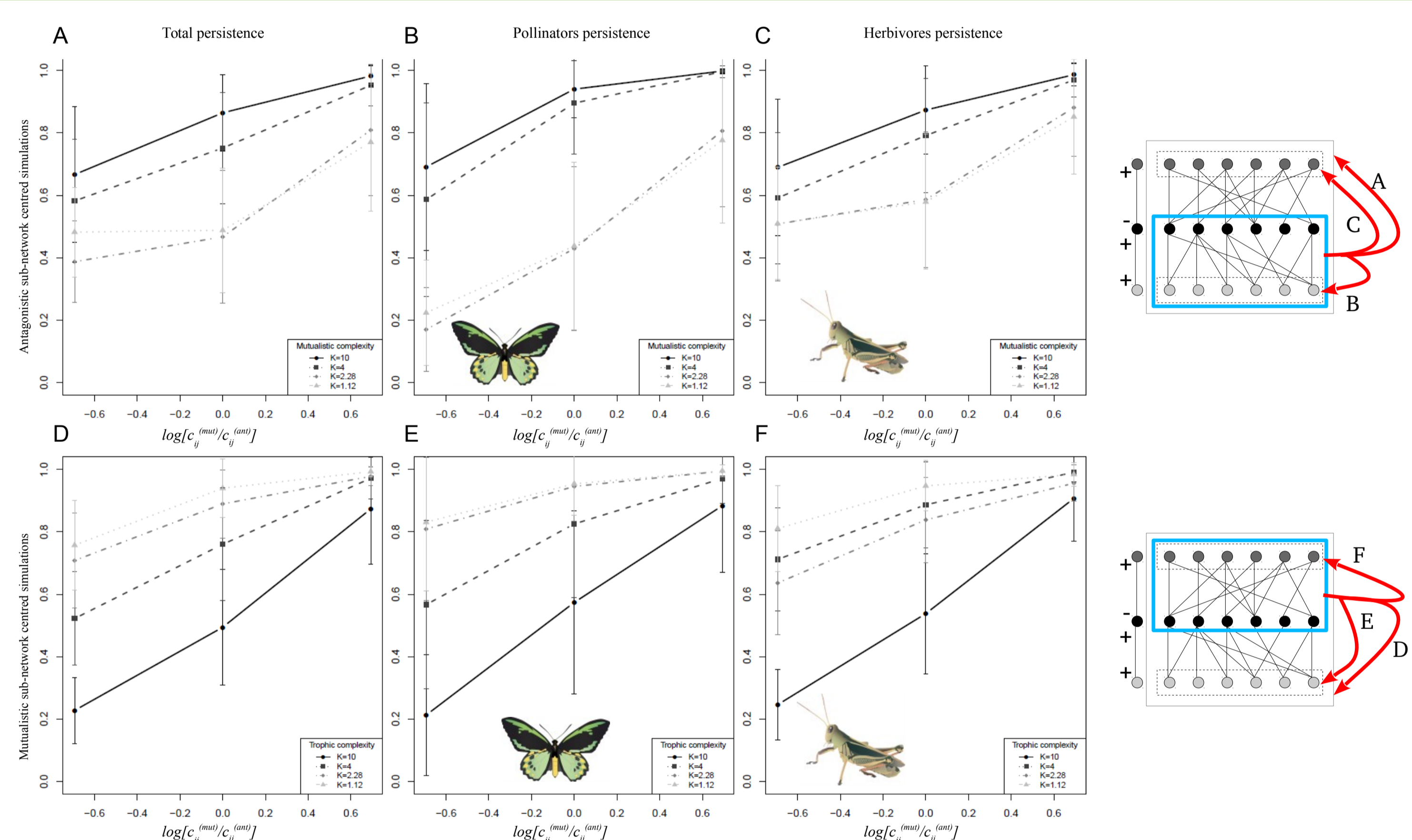


Figure 2: (A-B-C) Persistence against  $\log[c_{ij}^{(mut)}/c_{ij}^{(ant)}]$ , considering different cases of mutualistic complexity; (D-E-F) Persistence against  $\log[c_{ij}^{(mut)}/c_{ij}^{(ant)}]$ , considering different cases of antagonistic complexity.

What is the relationship between one sub-network structure and the whole community persistence?

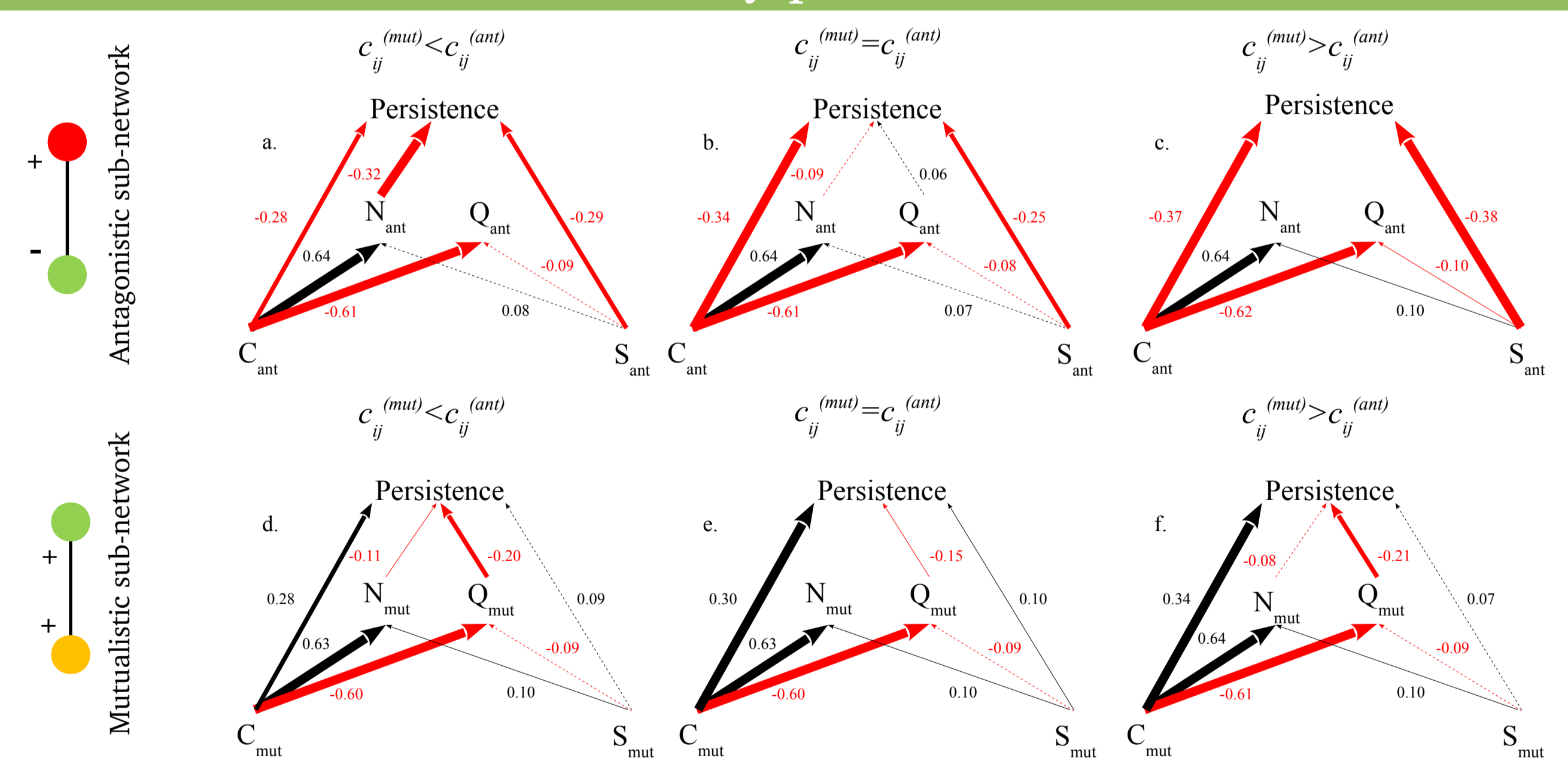


Figure 3: Path diagram of the effects of the initial measures of each sub-network structure on persistence of the merged network, for different ratios of interaction strength.

## CONCLUSION

This theoretical study suggests that:

- The structure of one sub-network influences the stability of the other sub-network, and vice versa,
- Current bipartite network metrics are no longer adapted,
- Complexity-stability relationships are robust to the interconnection.

Two networks that are merged influence each other's persistence as **disturbances can be propagated from one sub-network to the other**. The way the community responds depends on the respective structures, and their interaction types.

Fine architectural patterns have weak effects on stability. We assume the propagation of disturbance depends on **the way the two sub-networks are linked**<sup>2,3</sup>, and **the type of interaction** (strength and kind).

Considering the diversity of interaction in a single framework needs to be developed further, as **the interaction types interact**.

<sup>1</sup> Thébault, E., & Fontaine, C. (2010). Stability of ecological communities and the architecture of mutualistic and trophic networks. *Science*, 329, 853-856.

<sup>2</sup> Fontaine, C., Guimarães, P. R. J., Kéfi, S., Loeuille, N., Memmott, J., van der Putten, W. H., van Veen, F. J. F., et al. (2011). The ecological and evolutionary implications of merging different types of networks. *Ecology Letters*, 1-12.

<sup>3</sup> Melian, C. J., Bascompte, J., Jordano, P., & Krivan, V. (2009). Diversity in a complex ecological network with two interaction types. *Oikos*, 118(July), 122-130.