

# Modelling respiro-fermentative dynamics of *Saccharomyces cerevisiae* batch culture to understand the evolution of life-history strategies

Collot Dorian

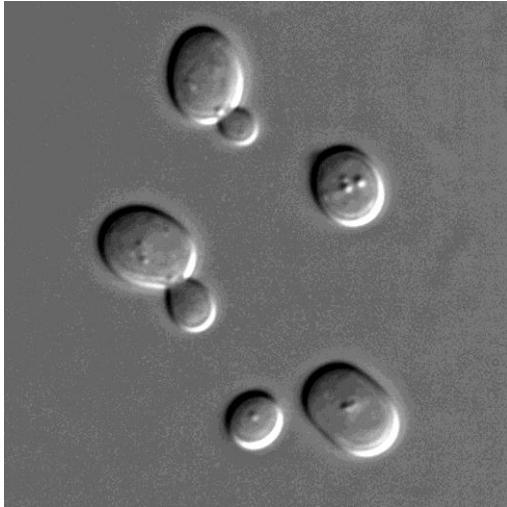


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Méléard Sylvie, Martin Olivier

**Ecole de printemps de la chaire MMB**

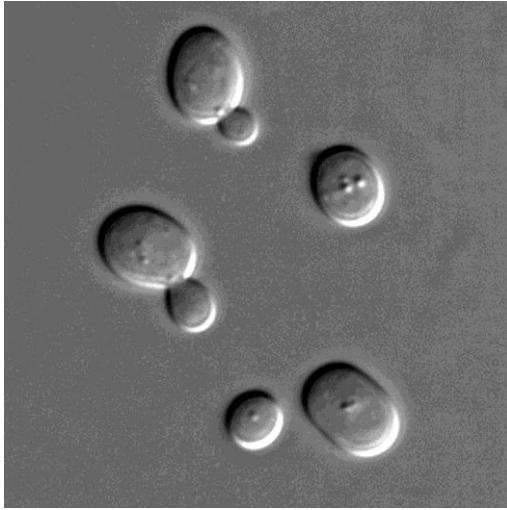


# *Saccharomyces cerevisiae*



<http://fr.wikipedia.org/wiki/Saccharomyces>

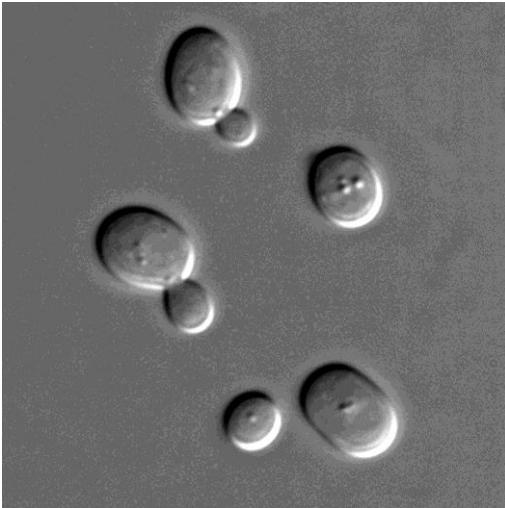
# *Saccharomyces cerevisiae*



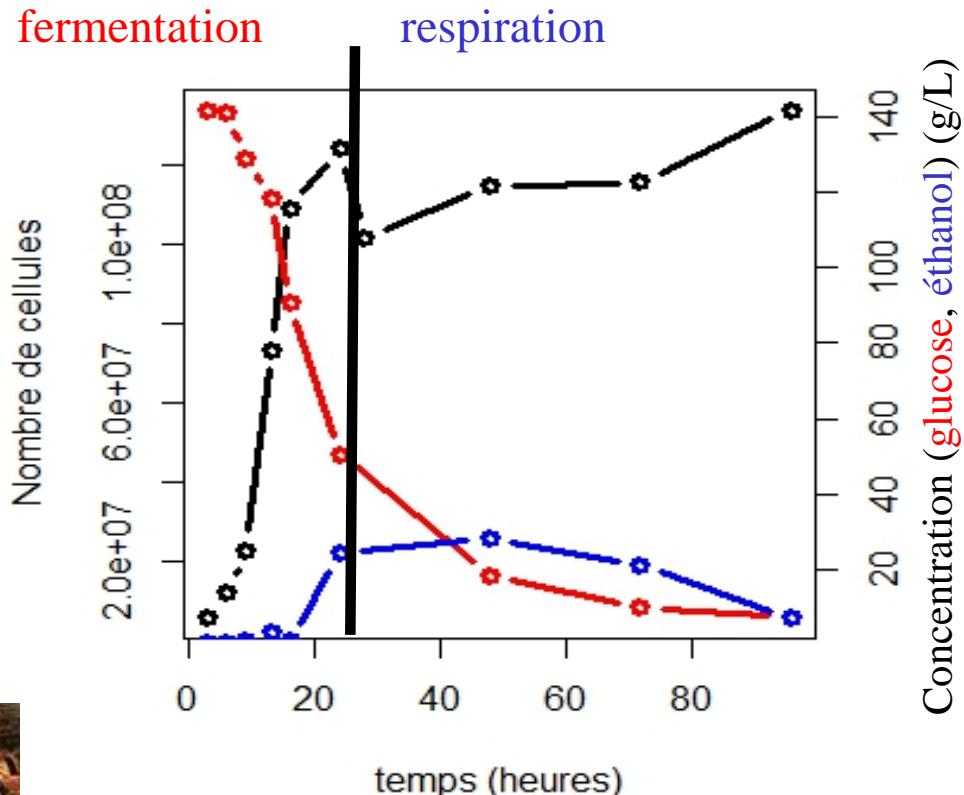
<http://fr.wikipedia.org/wiki/Saccharomyces>



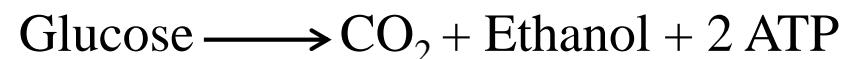
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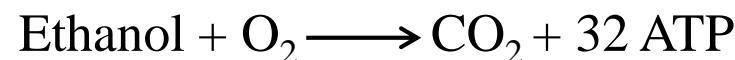
<http://fr.wikipedia.org/wiki/Saccharomyces>



## Fermentation :

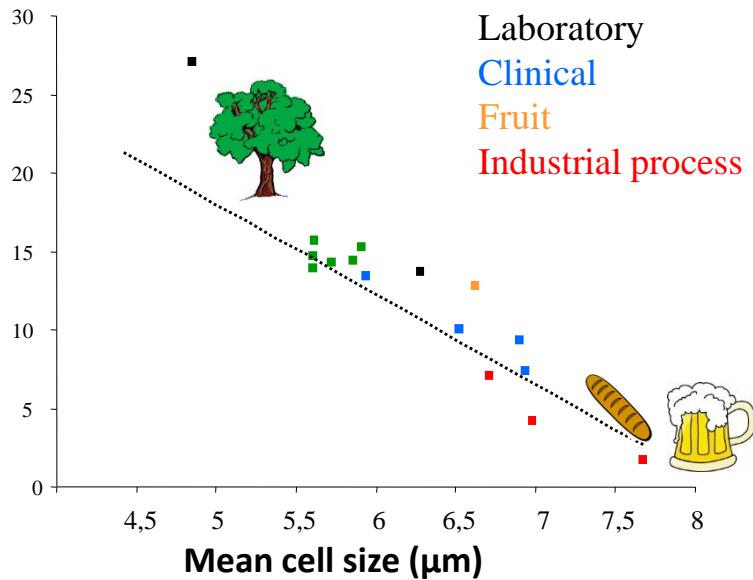


## Respiration:



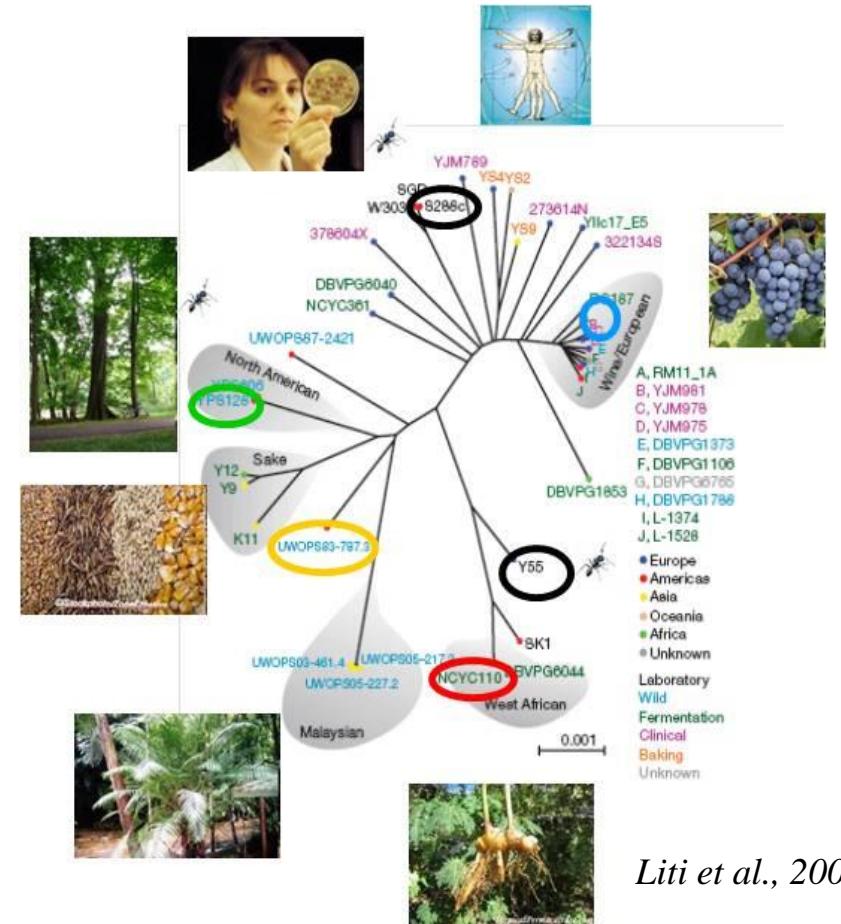
# Adaptation *in natura*

**Final population density**  
 $\times 10^7$  cells/mL



Forest  
 Laboratory  
 Clinical  
 Fruit  
 Industrial process

Spor et al., 2009



Liti et al., 2009

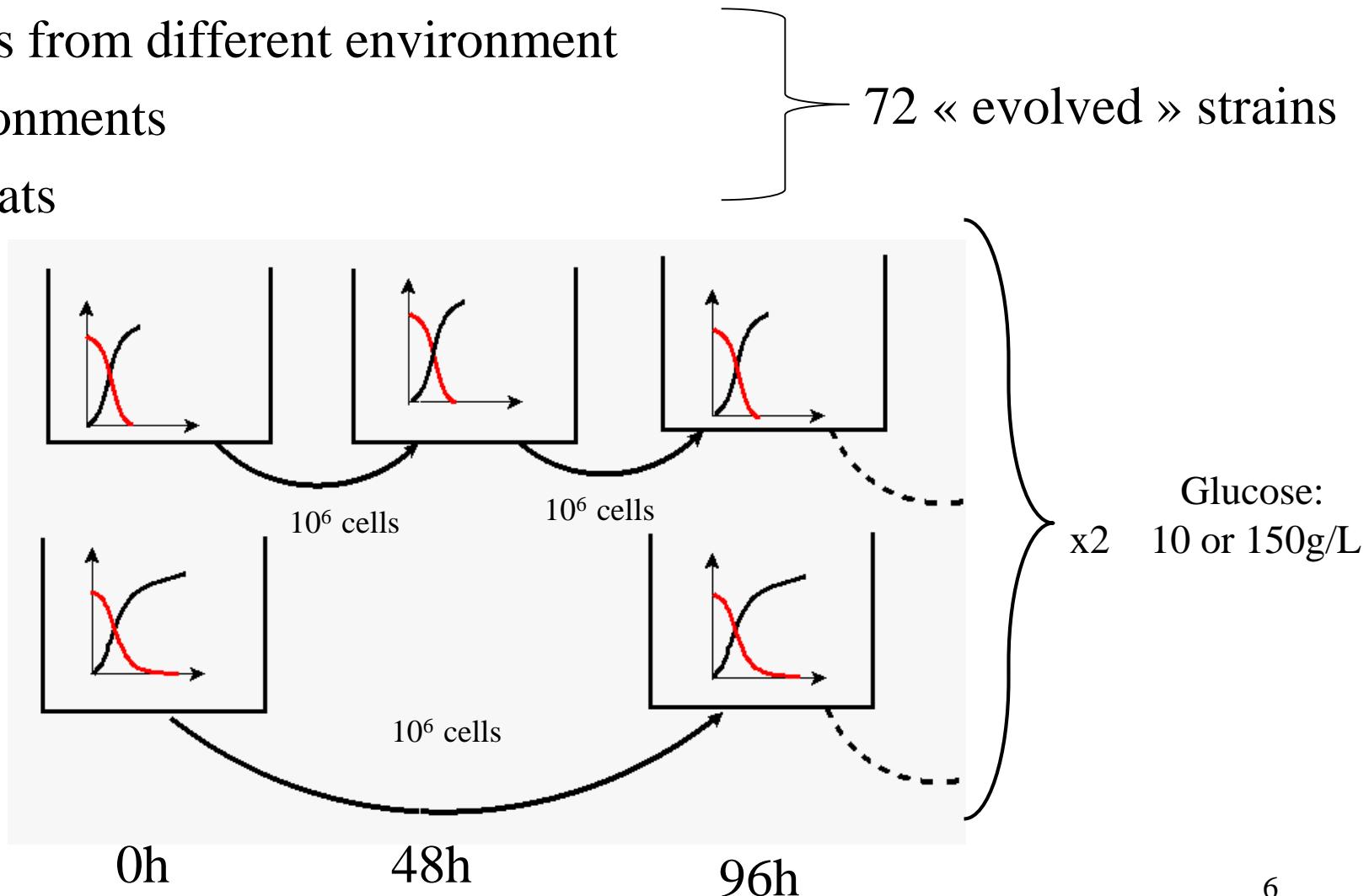
# Adaptation *in vitro*

Experimental evolution: (*Spor et al., 2014*)

6 strains from different environment

4 environments

3 replicates



# Traits convergency

Experimental evolution: (Spor et al., 2014)

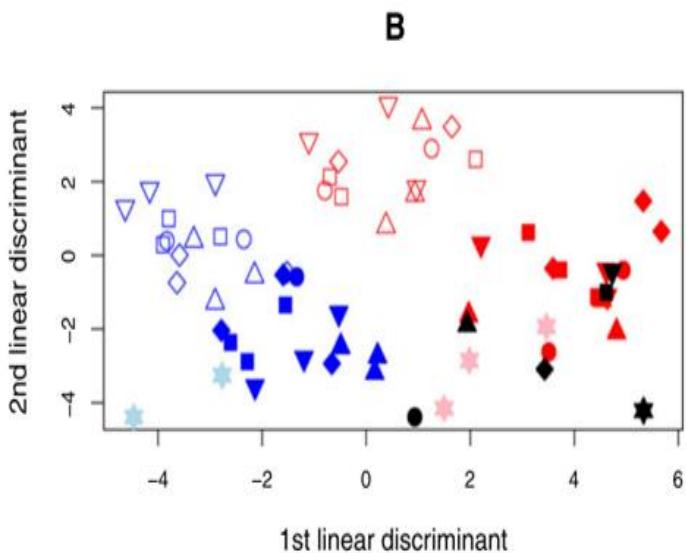
6 strains from different environment

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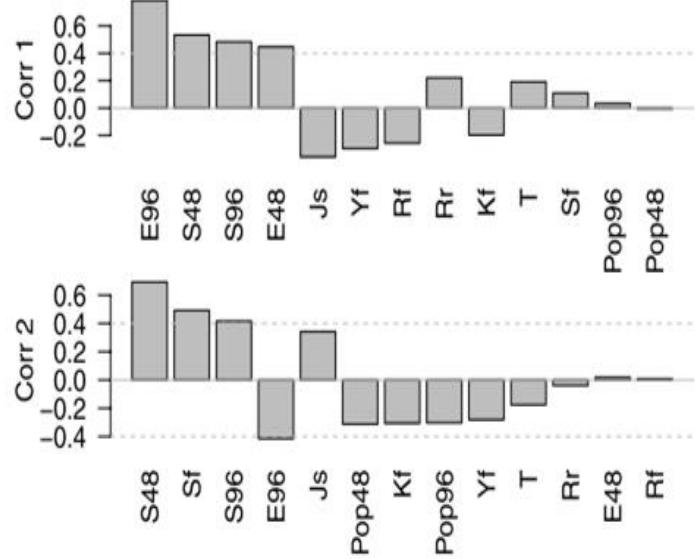
3 replicates

72 « evolved » strains

1%-96h  
15%-96h  
1%-48h  
15%-48h



Spor et al., 2014



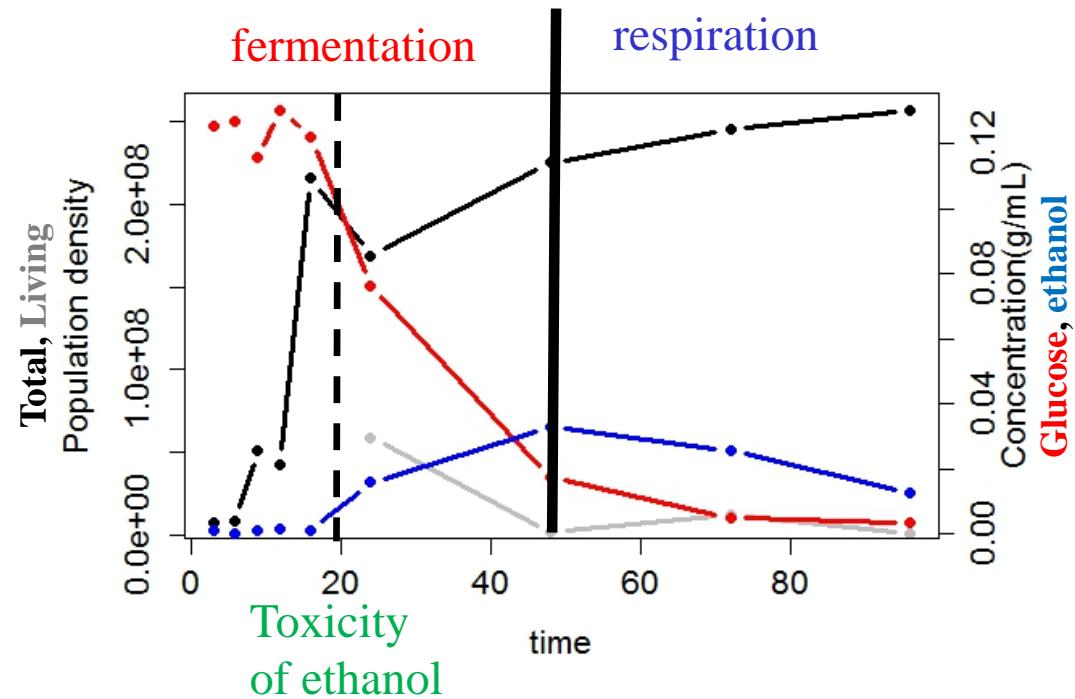
# What are the traits which determine the outcome of the competition in a seasonal environment?

Traits that influence fitness.

Characterization of mutant frequencies dynamics  
in a resident population.

Determinants of the mutant frequencies  
dynamics.

# Batch culture model



$$\frac{dG}{dt} = - \sum_i J_{fi} \frac{G}{K_f + G} N_i$$

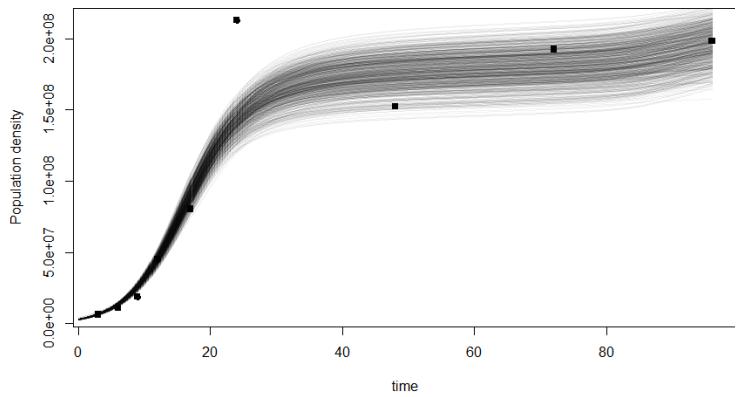
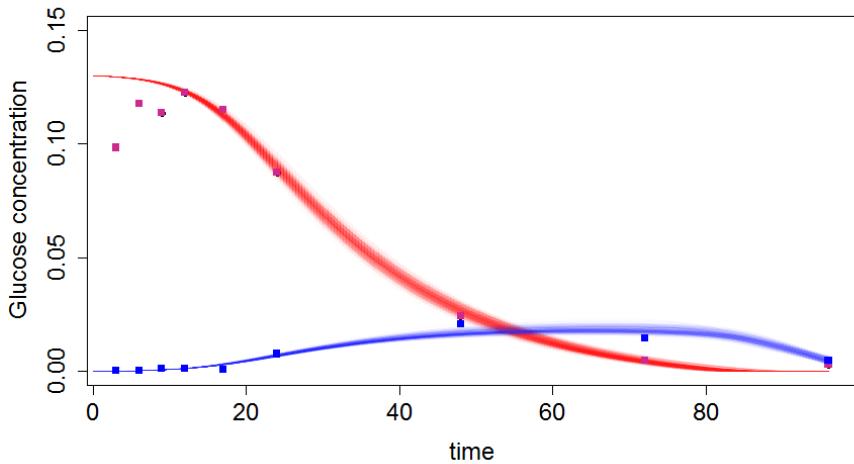
$$\frac{dN_i}{dt} = r_{fi} \frac{G}{K_{fi} + G} \cdot \exp\left(-\frac{E}{E_{m,i}}\right) N_i + r_{ri} \frac{E}{K_{ri} + E} \left(\frac{K_{Ci}}{K_{Ci} + G}\right) N_i - m \cdot N_i$$

$$\frac{dE}{dt} = \sum_i J_{fi} \frac{G}{K_f + G} p_i N_i - \sum_i J_{ri} \frac{E}{K_{ri} + E} \left(\frac{K_{Ci}}{K_{Ci} + G}\right) N_i$$

Adapted from MacLean *et al.*, 2006

# Inference of the parameters

Inference by ABC method,  
*Toni et al.*



Parameters	Boundary set
Glucose consmption rate $J_f$	$10^{-11}$ - $2.10^{-10}$ (g.cell $^{-1}$ .h $^{-1}$ )
Fermentation growth rate $r_f$	0.2-0.6 (h $^{-1}$ )
Fermentation yield p	0-0.5
« Affinity » of the reaction K	$10^{-7}$ - $10^{-2}$ (g/mL)
Ethanol consmption rate $J_r$	$10^{-11}$ - $10^{-9}$ (g.cell $^{-1}$ .h $^{-1}$ )
Fermentation growth rate $r_r$	0.01-0.1 (h $^{-1}$ )
Inhibition of Glucose on resp. Kc	$10^{-7}$ - $10^{-2}$ (g/mL)
Mortality rate m	0.01-0.4 (h $^{-1}$ )
Toxic effect of ethanol Em	$10^{-4}$ - $10^{-2}$ (g/mL)

$$\frac{dG}{dt} = - \sum_i J_{fi} \frac{G}{K_f + G} N_i$$

$$\frac{dN_i}{dt} = r_{fi} \frac{G}{K_{fi} + G} \cdot \exp\left(-\frac{E}{E_{m,i}}\right) \cdot N_i + r_{ri} \frac{E}{K_{ri} + E} \left(\frac{K_{Ci}}{K_{Ci} + G}\right) N_i - m \cdot N_i$$

$$\frac{dE}{dt} = \sum_i J_{fi} \frac{G}{K_f + G} p_i N_i - \sum_i J_{ri} \frac{E}{K_{ri} + E} \left(\frac{K_{Ci}}{K_{Ci} + G}\right) N_i$$

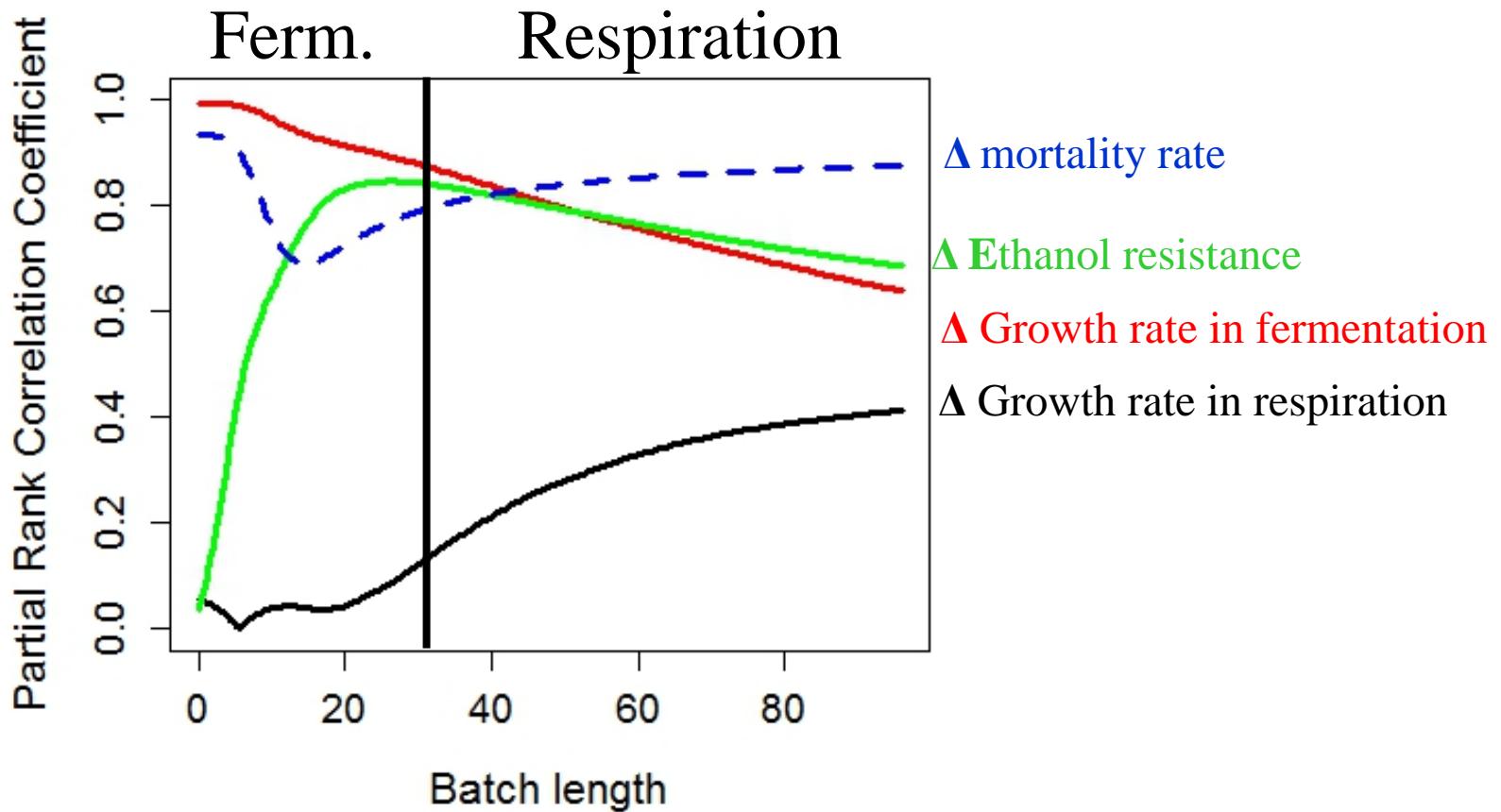
# Competitions *in Silico*

- Sampling of 100 strains (Latin Hypercube Sampling)
- Initial frequency of the mutant : 0.001%
- 10 000 competitions.
- Fitness definition:

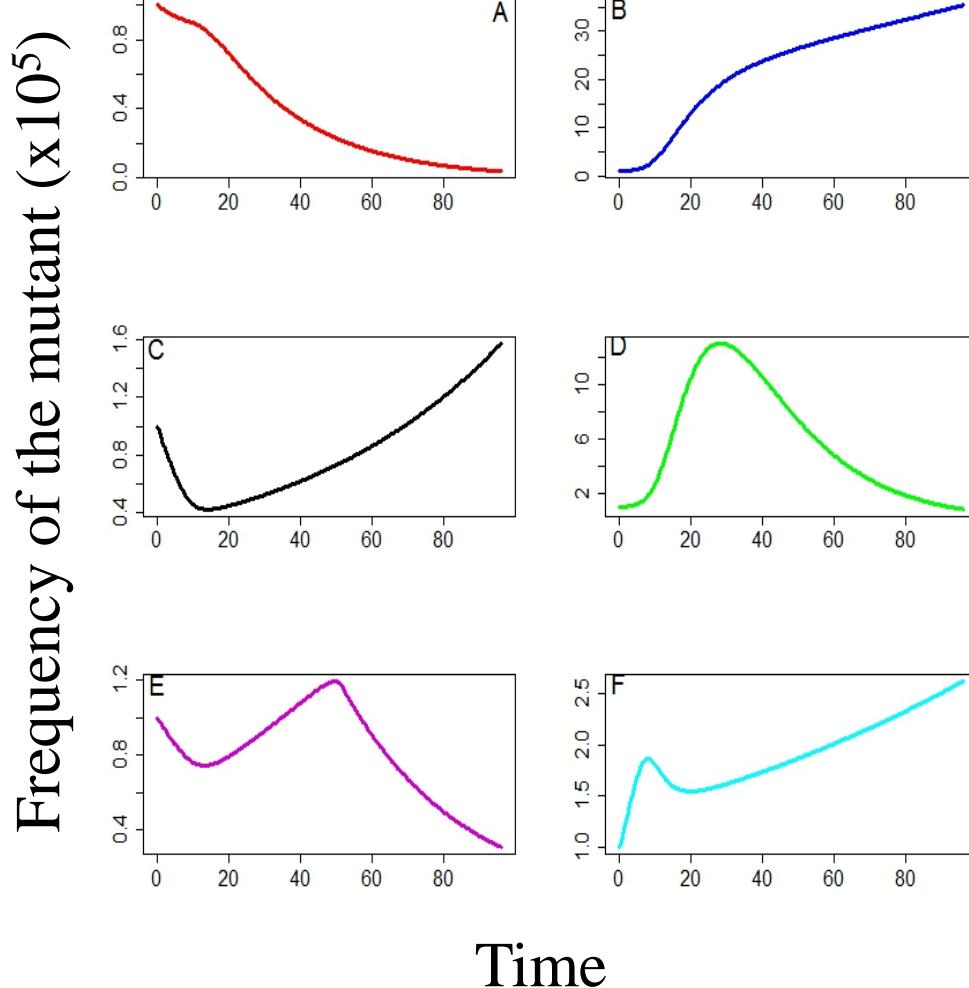
$$W_{1/2}(t) = \ln\left(\frac{N_1(t)}{N_1(0)}\right) - \ln\left(\frac{N_2(t)}{N_2(0)}\right)$$

$N_i$  is the density of strain i.

# Correlation between fitness and traits

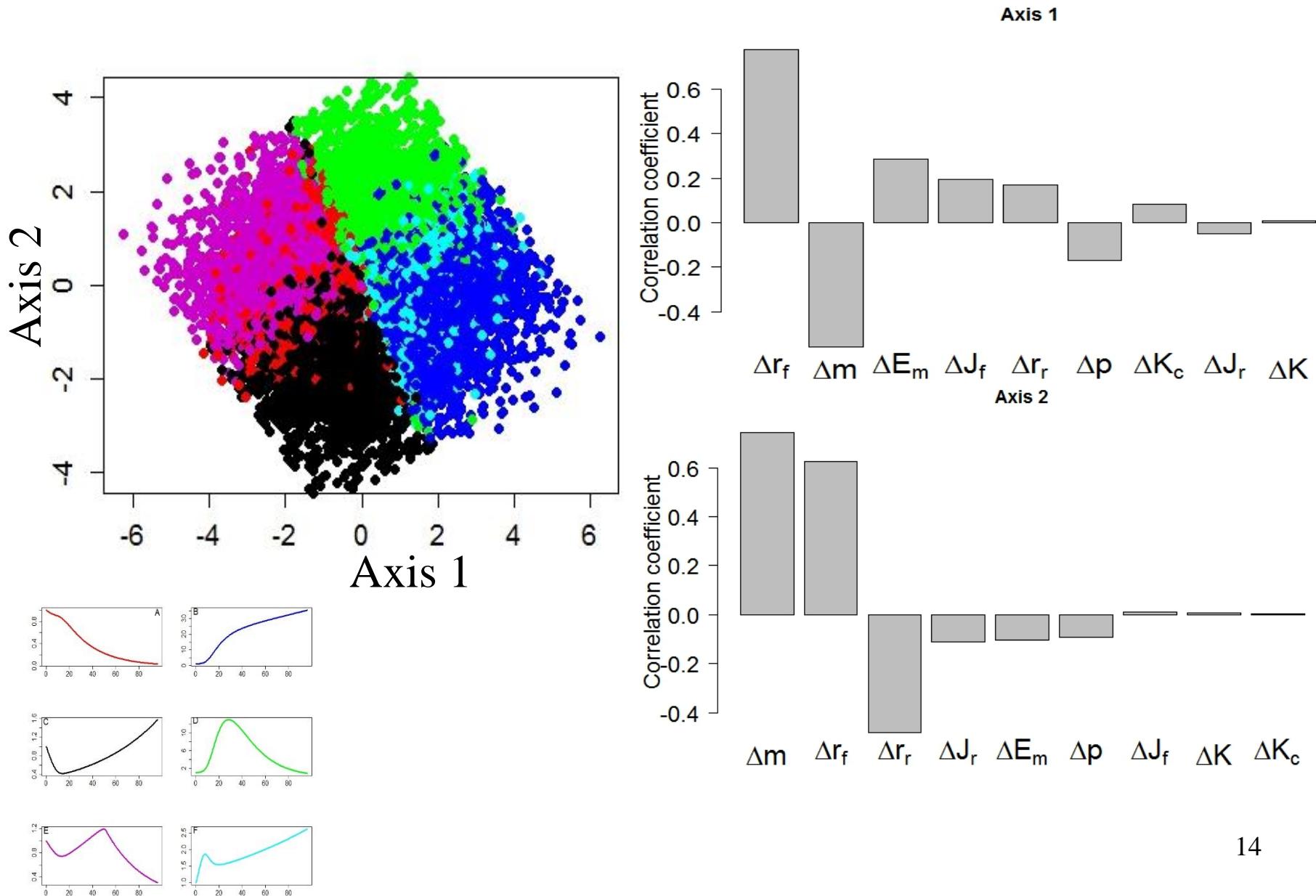


# Different mutant frequencies dynamics

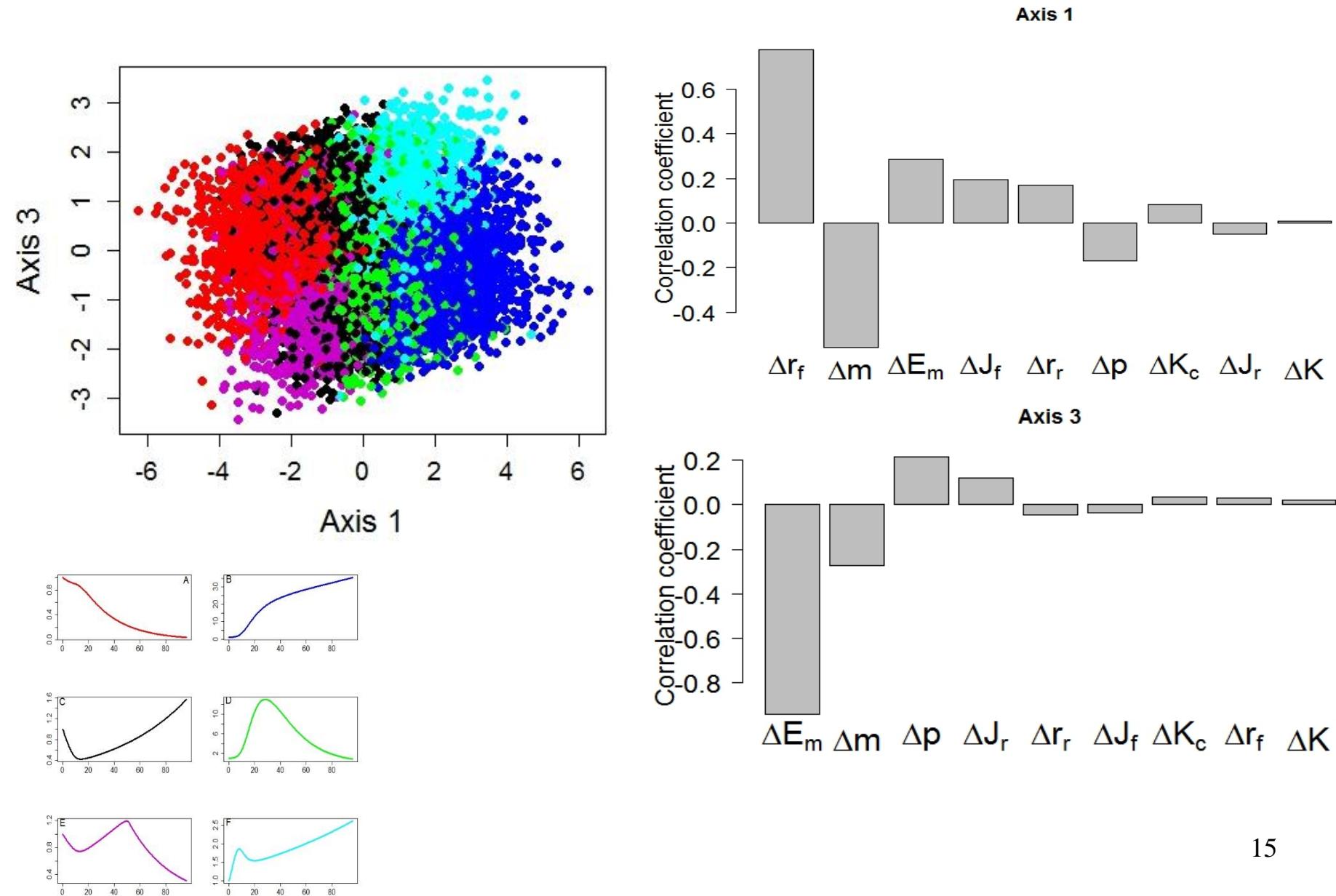


- 6 types of possible dynamics of frequency of the mutant.
- Low frequency = low chance to go to the next batch.

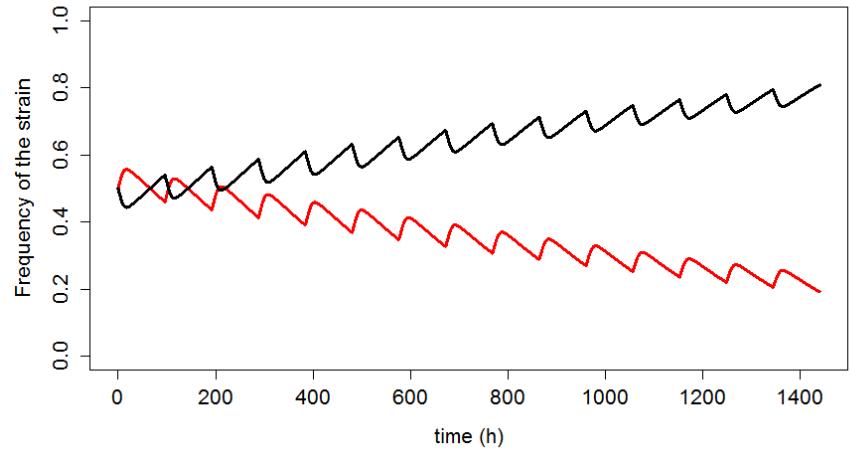
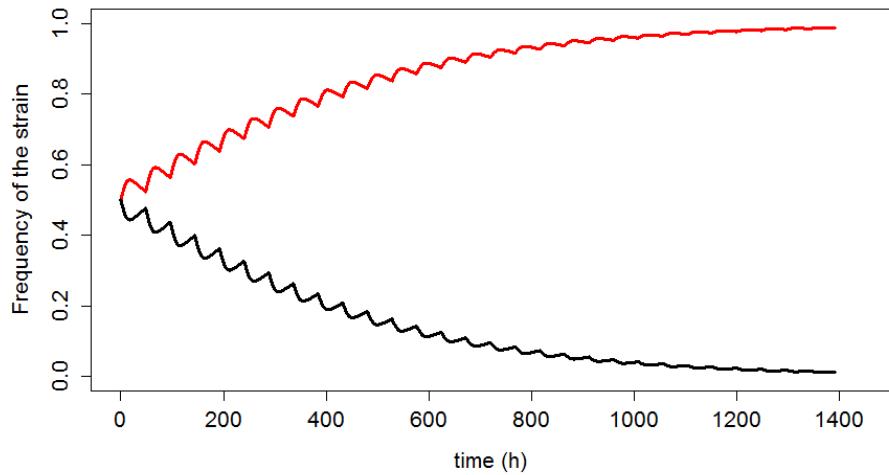
# Links between traits and dynamics



# Links between traits and dynamics



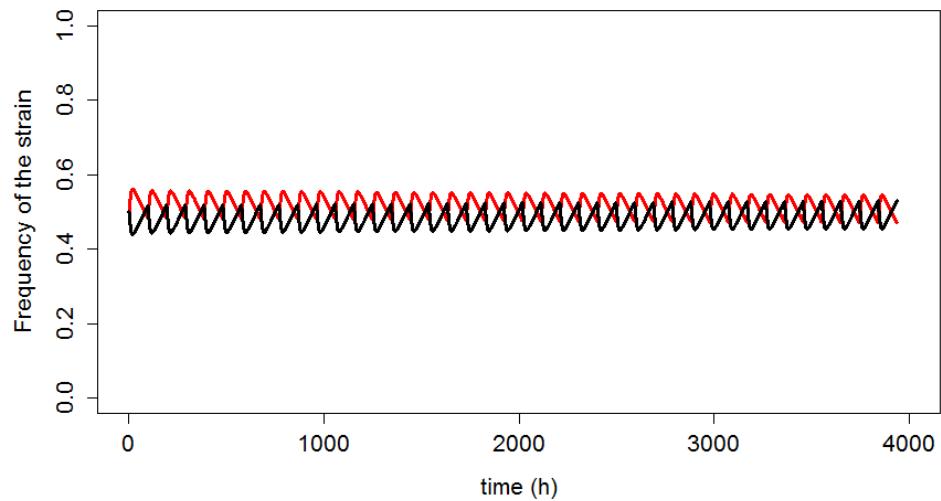
# Effect of the length of the batch



Parameters	Red	Black
m	0.106	0.1
$J_f$	$7.10^{-11}$	$7.10^{-11}$
$r_f$	0.43	0.4
$E_m$	$9.10^{-3}$	$9.10^{-3}$
p	0.25	0.25
$J_r$	$2.10^{-10}$	$2.10^{-10}$
$r_r$	0.05	0.05
$K_c$	$8.10^{-4}$	$8.10^{-4}$
K	$5.10^{-4}$	$5.10^{-4}$

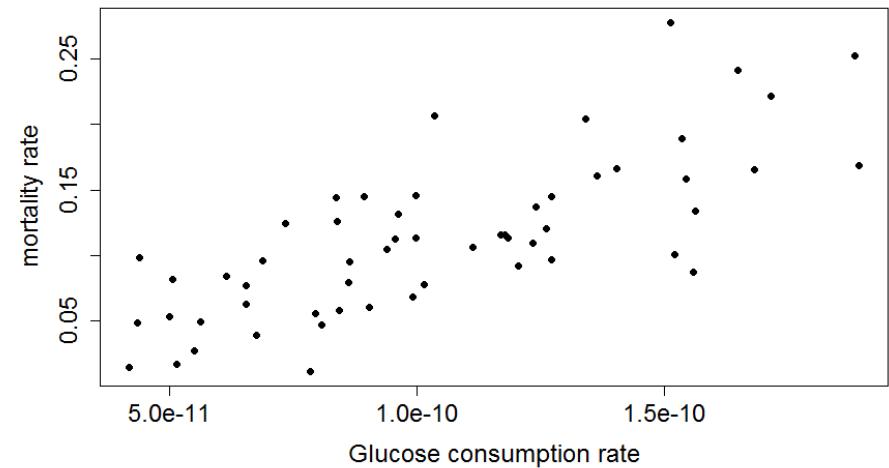
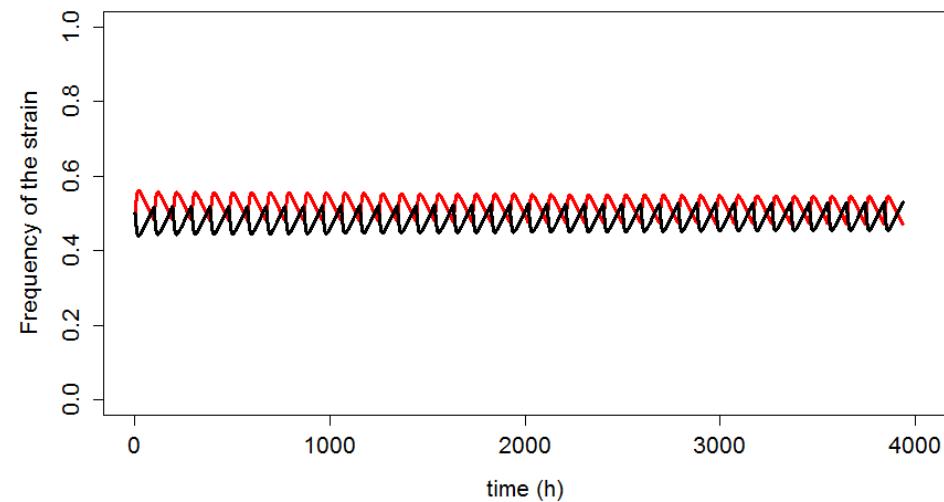
# Future developments

- Study the frequency dependence of fitness



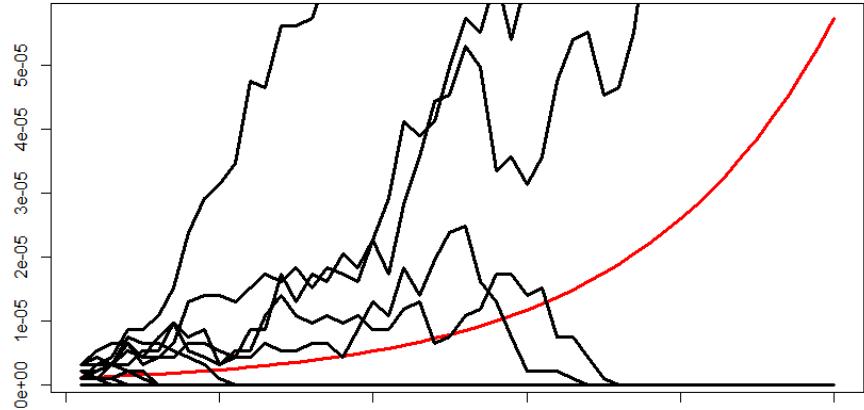
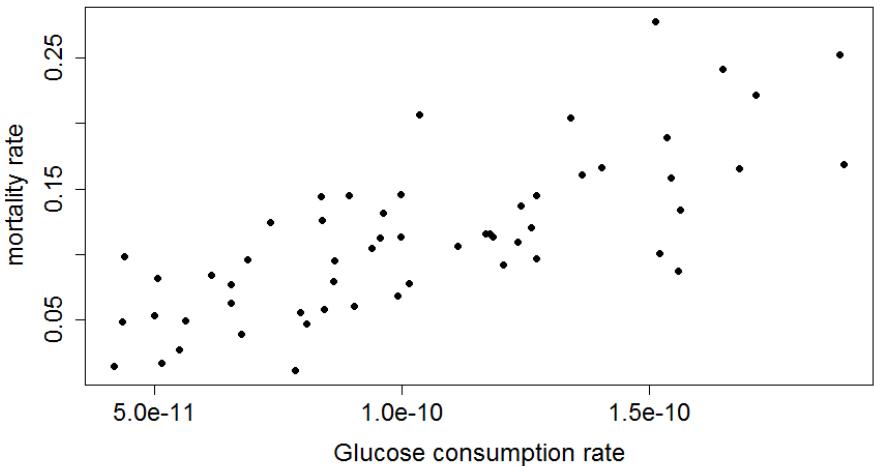
# Future developments

- Study the frequency dependence of fitness
- Add trade-off between the traits



# Future developments

- Study the frequency dependence of fitness
- Add trade-off between the traits
- Adding random process



# Thanks to:

Nidelet Thibault  
Dillmann Christine  
Sicard Delphine  
Legrand Judith  
Martin Olivier  
Méléard Sylvie

Experimental evolution:  
Spor Aymé  
Bourgais Aurélie