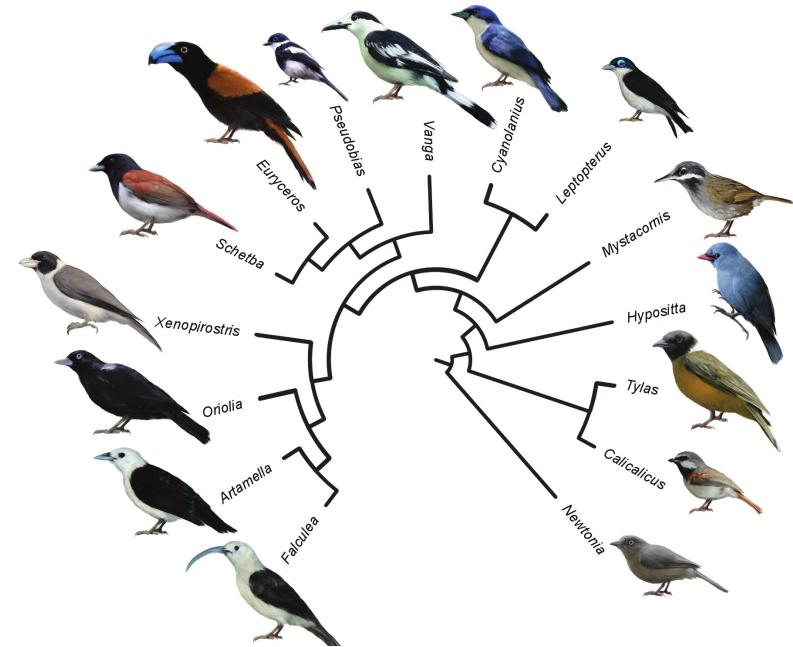
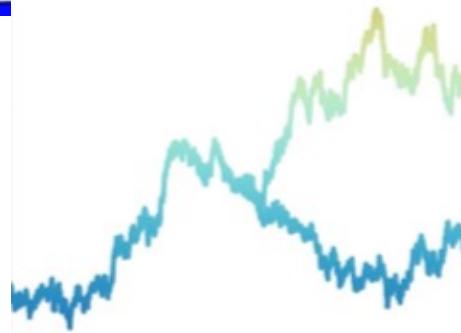
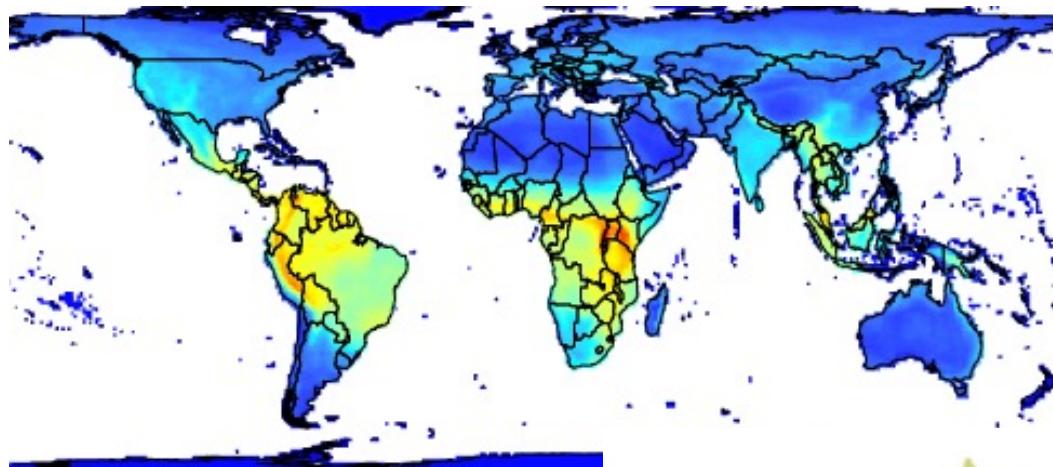


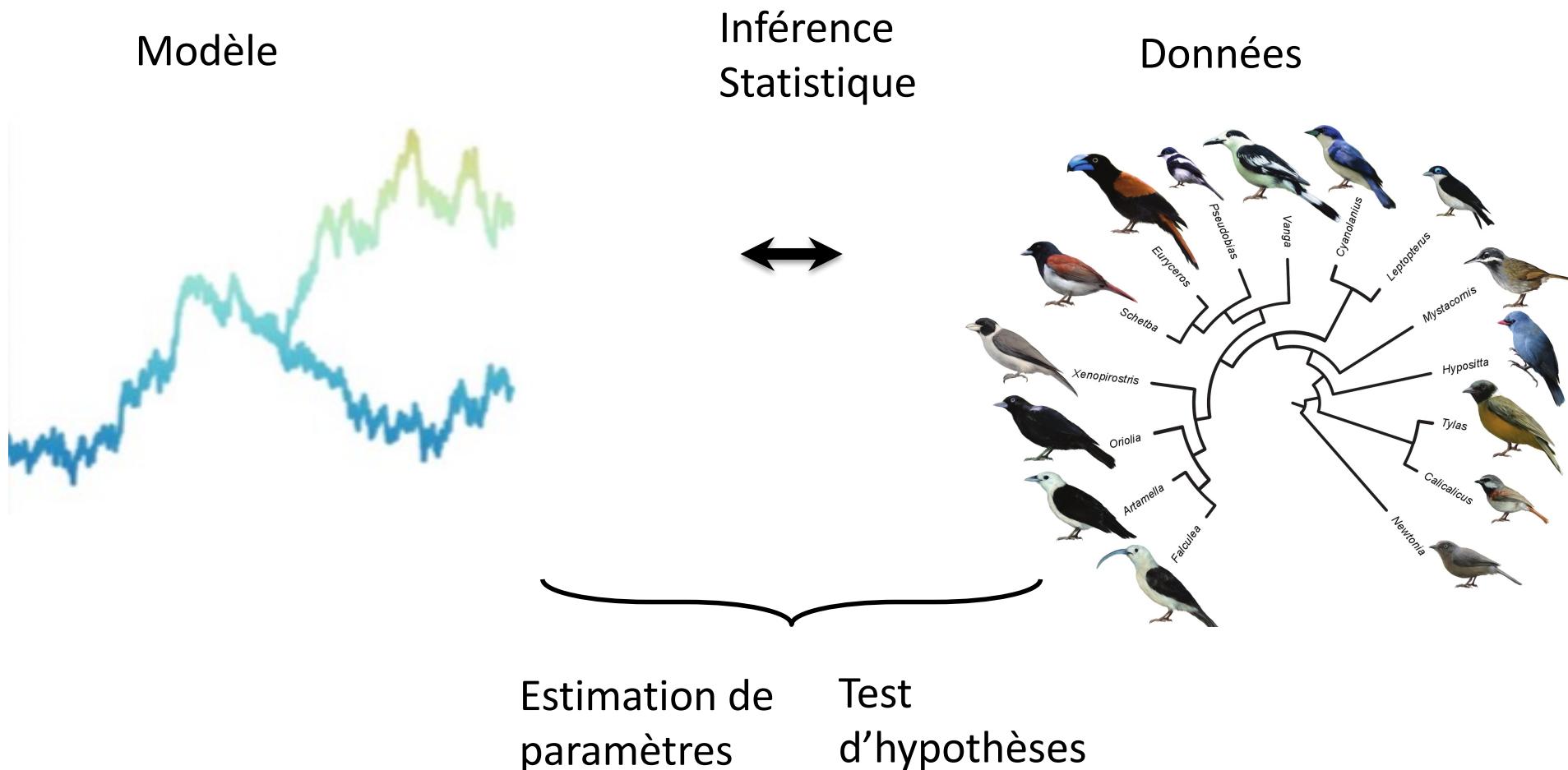
# Application de modèles stochastiques à l'étude phylogénétique de l'évolution de la biodiversité



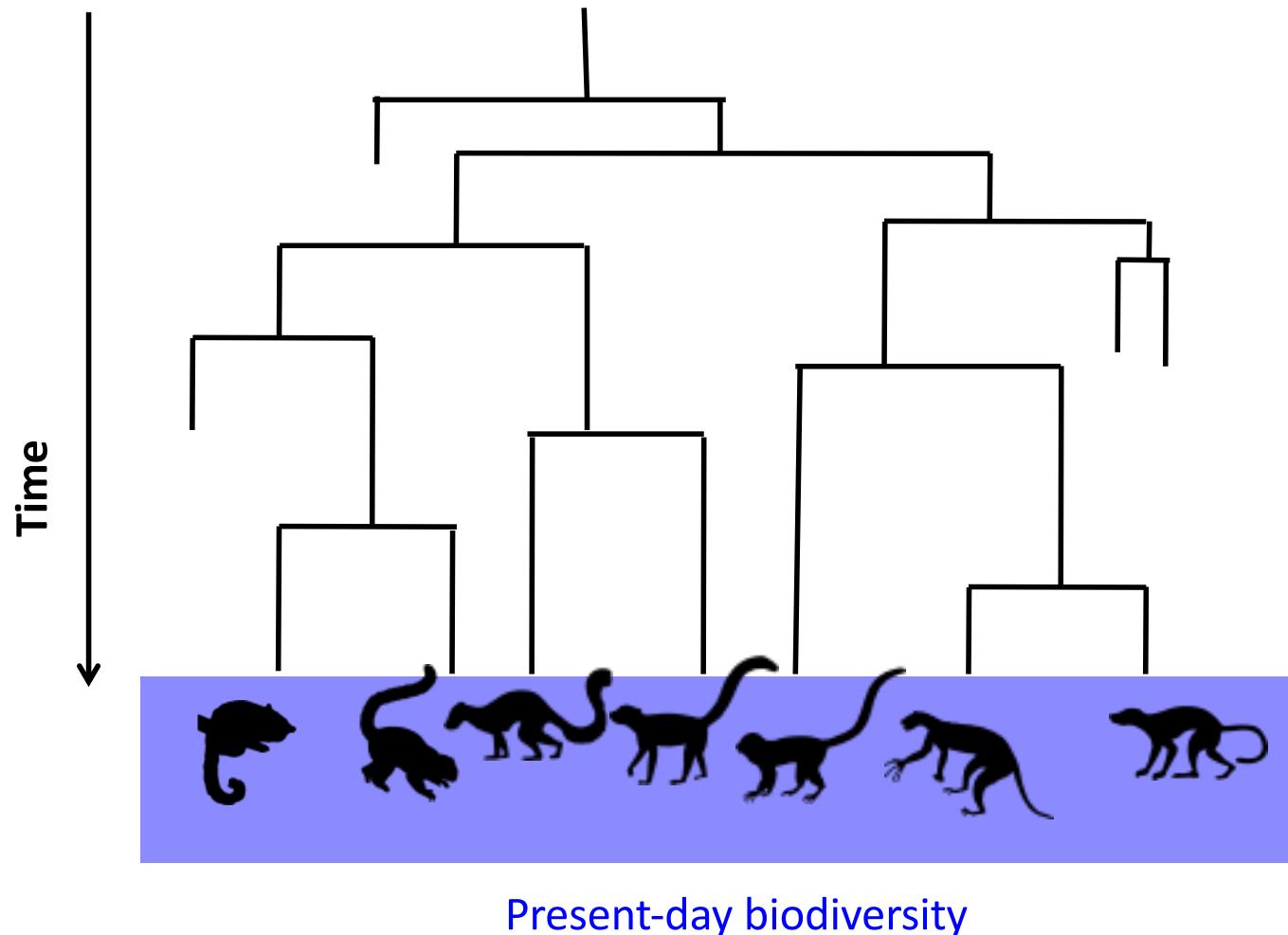
Hélène Morlon  
Ecole Normale Supérieure

# BUT

Développer des **modèles** ET des approches d'**inférence statistique** qui permettent d'ajuster les modèles à des **données empiriques** de façon à **estimer des paramètres biologiques et tester différentes hypothèses biologiques**

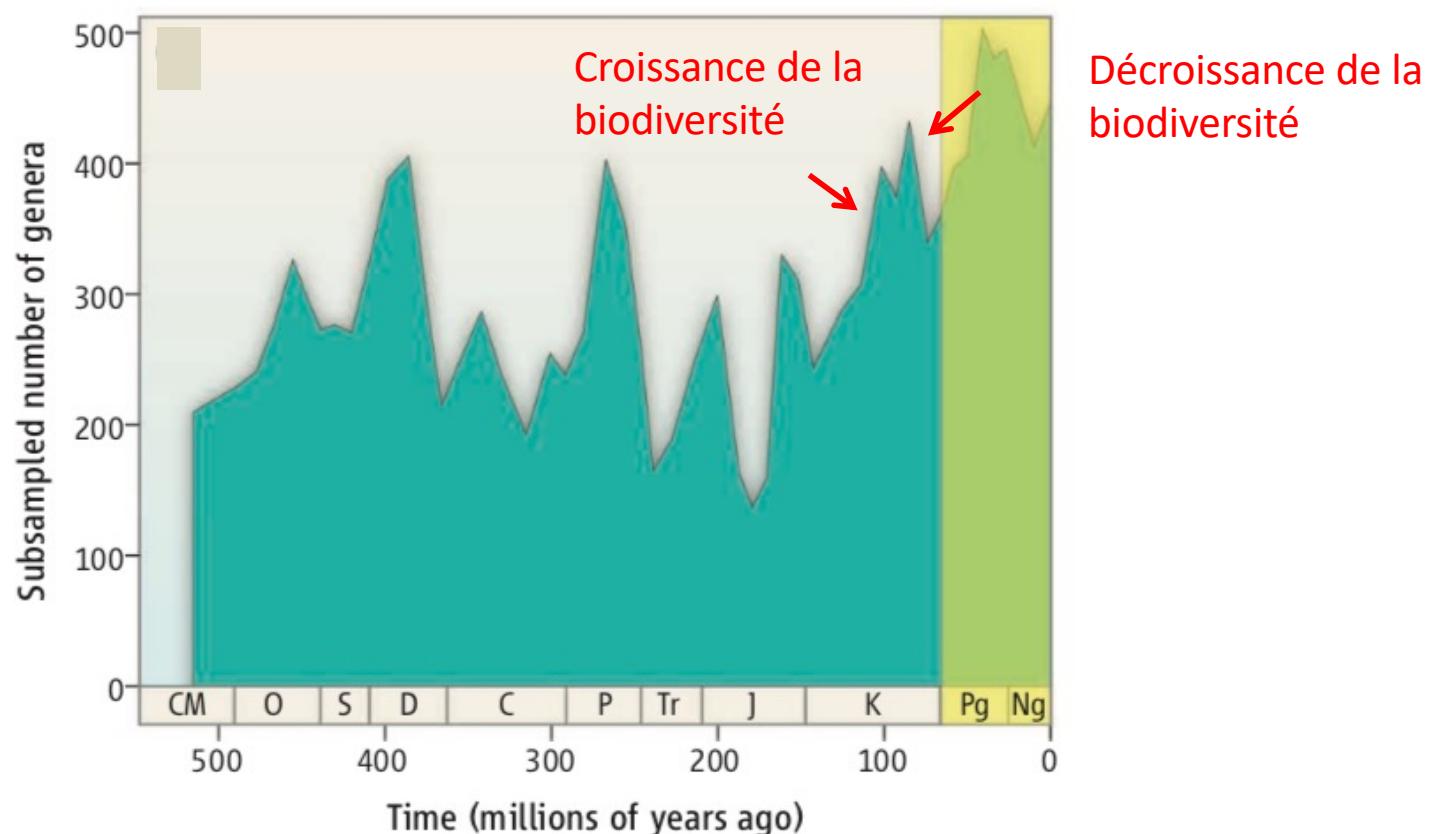


# Application des modèles de naissance-mort à l'étude phylogénétique de la diversification



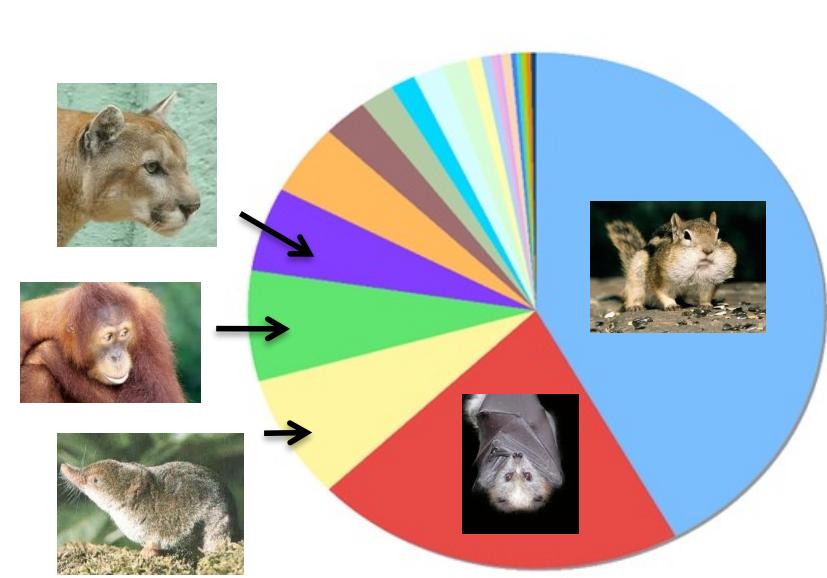
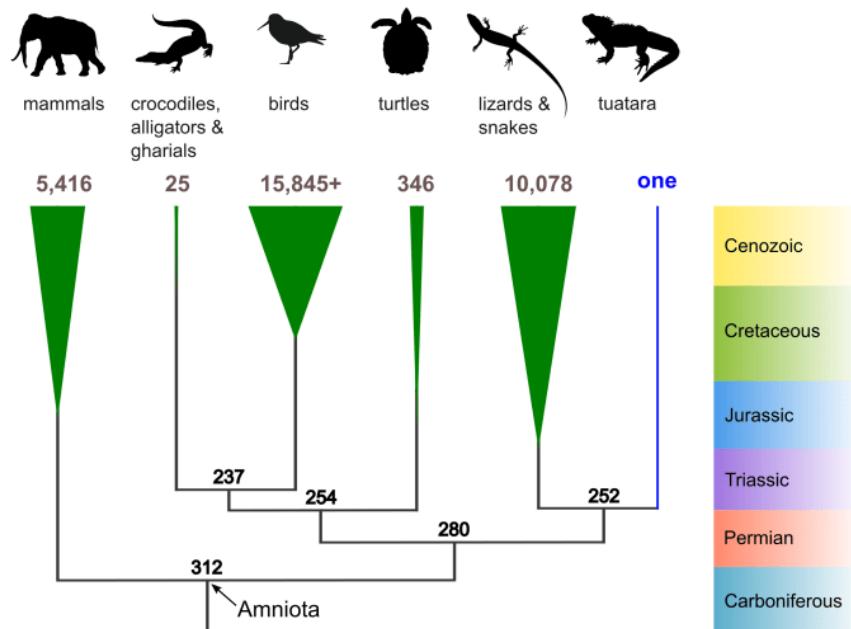
# La diversification des espèces

Les espèces s'éteignent (extinction) et donnent naissance à de nouvelles espèces (spéciation). La balance entre événements de spéciation et d'extinction explique les variations en nombre d'espèces au cours du temps.



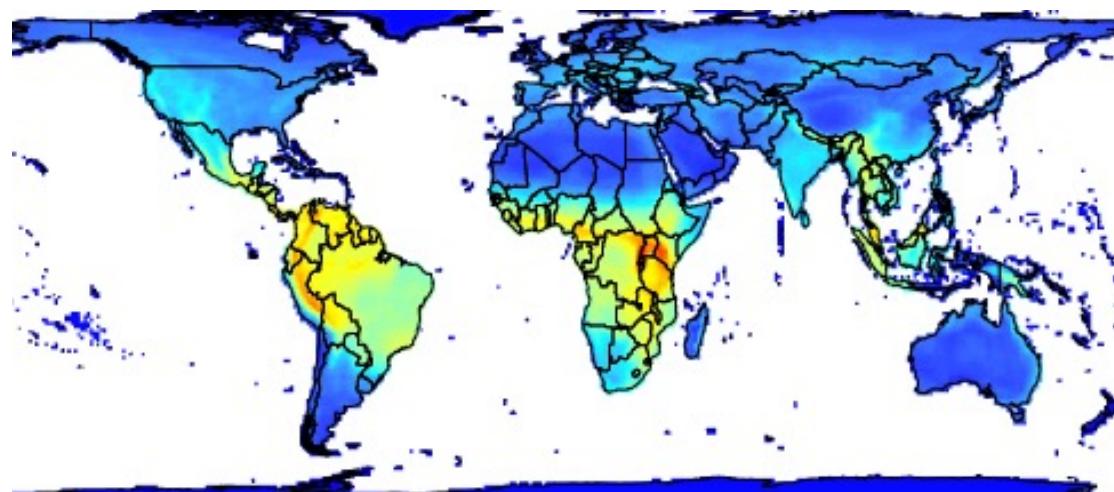
# La diversification des espèces

La balance entre événements de spéciation et d'extinction explique pourquoi certains groupes d'espèces sont beaucoup plus riches que d'autres



# La diversification des espèces

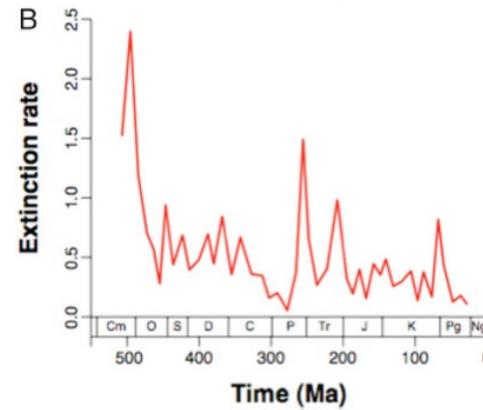
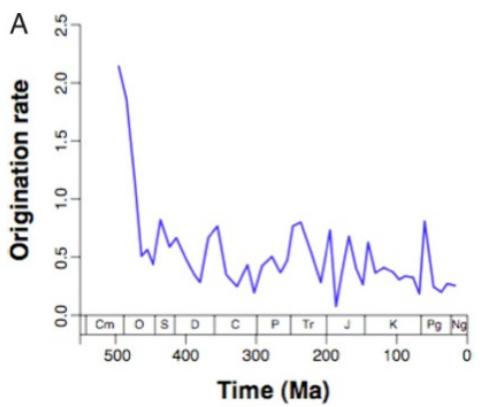
La balance entre événements de speciation, d'extinction et de dispersion explique pourquoi certaines régions de la planète sont beaucoup plus riches que d'autres



**Comment estimer, à partir de données empiriques, les taux de spéciation et d'extinction des espèces?**

# Comment estimer, à partir de données empiriques, les taux de spéciation et d'extinction des espèces?

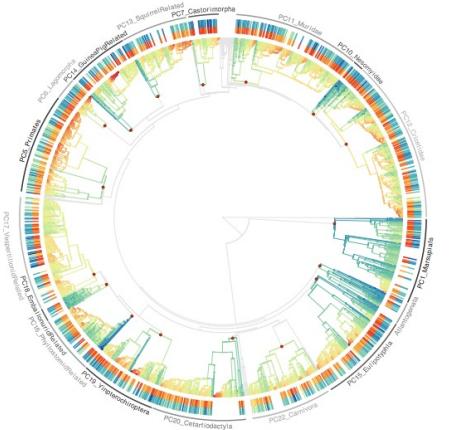
A partir des données fossiles



Alroy *PNAS* 2008

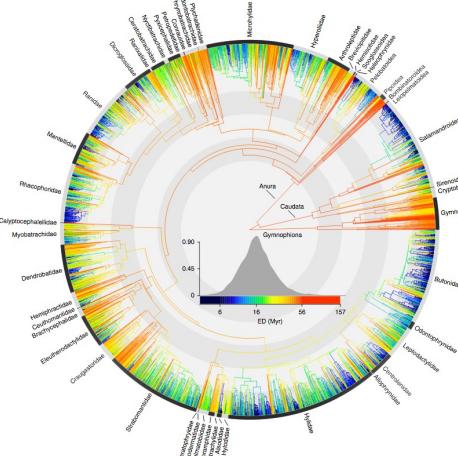
A partir des données phylogénétiques

# Etude de la diversification des espèces à partir des arbres phylogénétiques des espèces actuelles



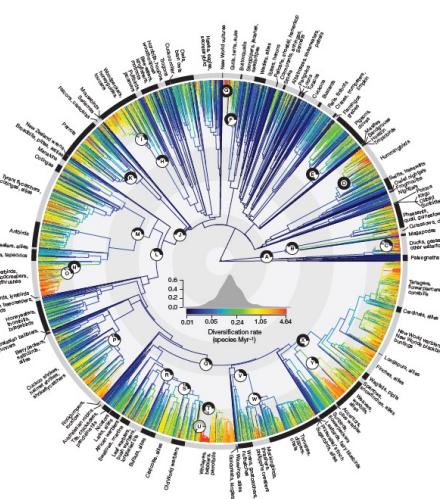
6 000 mammal species

Upham *et al.* *PloSB* 2019



> 7 000 amphibian species

Jetz & Pyron *Nat Ecol Evol* 2018

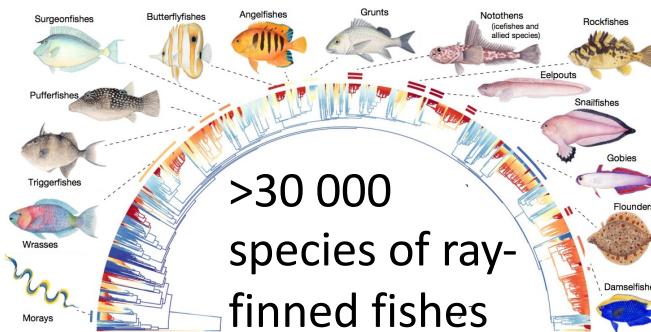


10 000 bird species

Jetz *et al.* *Nature* 2012

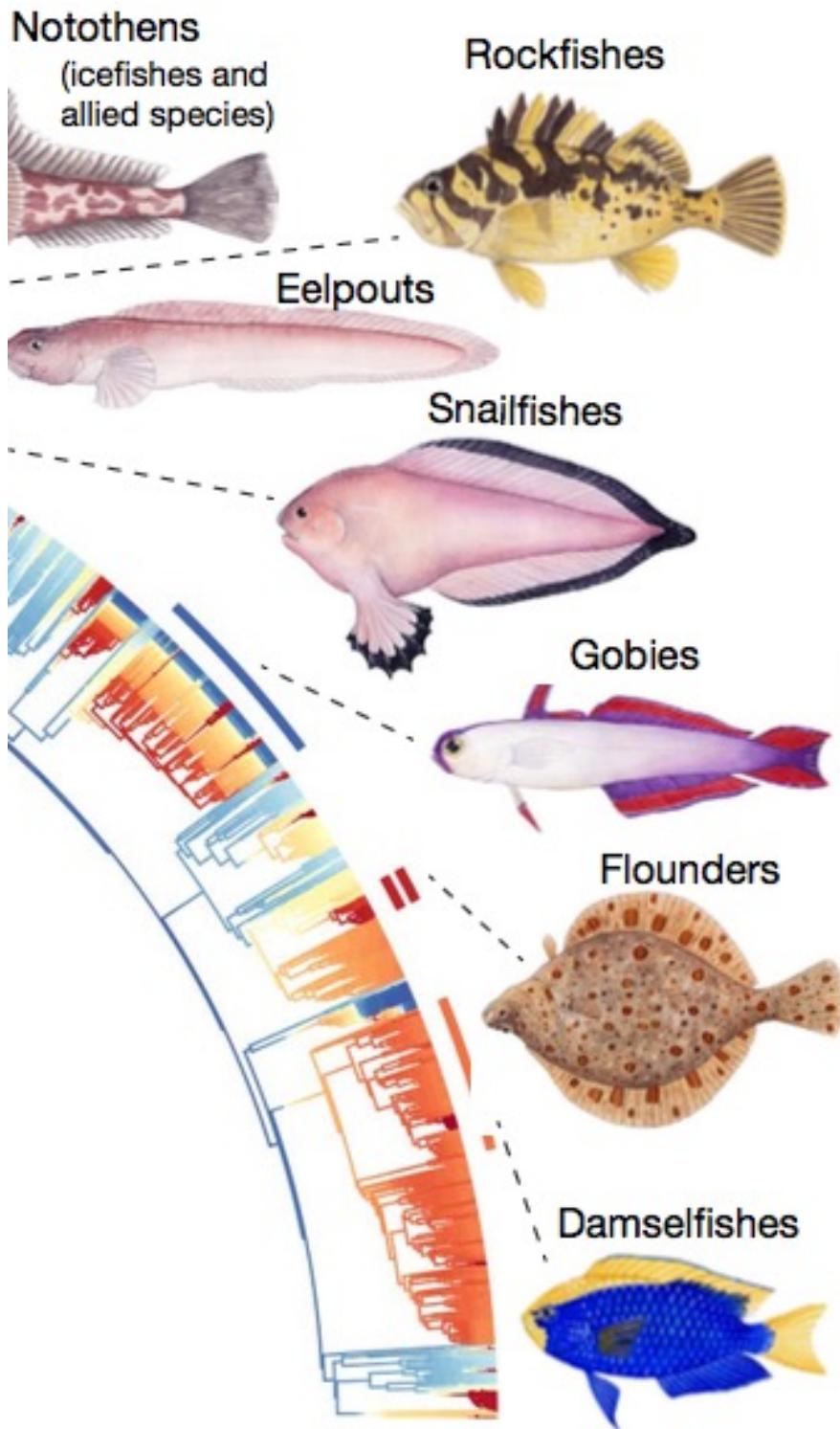


2.2 Million species  
on a single tree



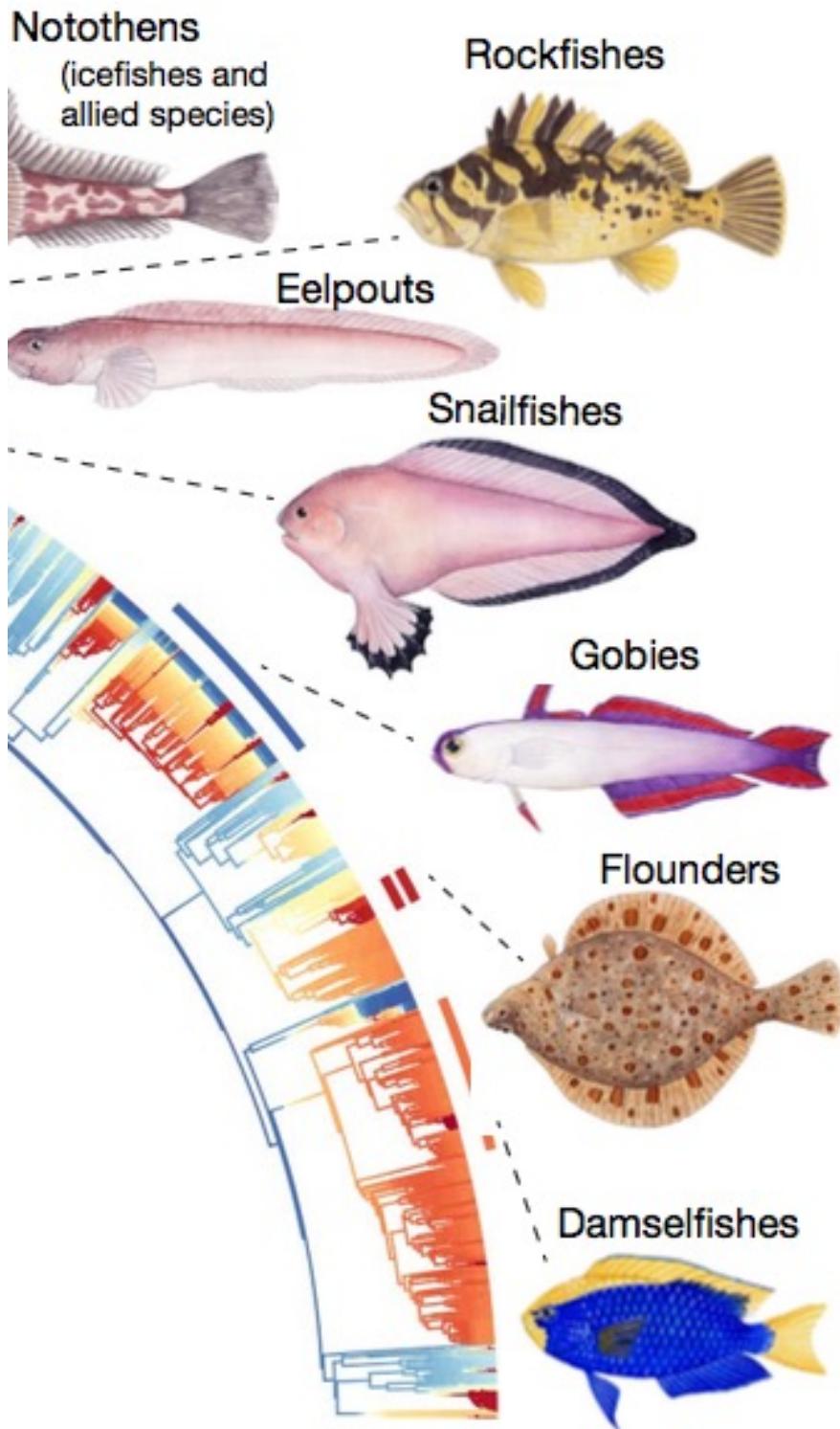
>30 000  
species of ray-  
finned fishes

Rabosky *et al.* *Nature* 2018

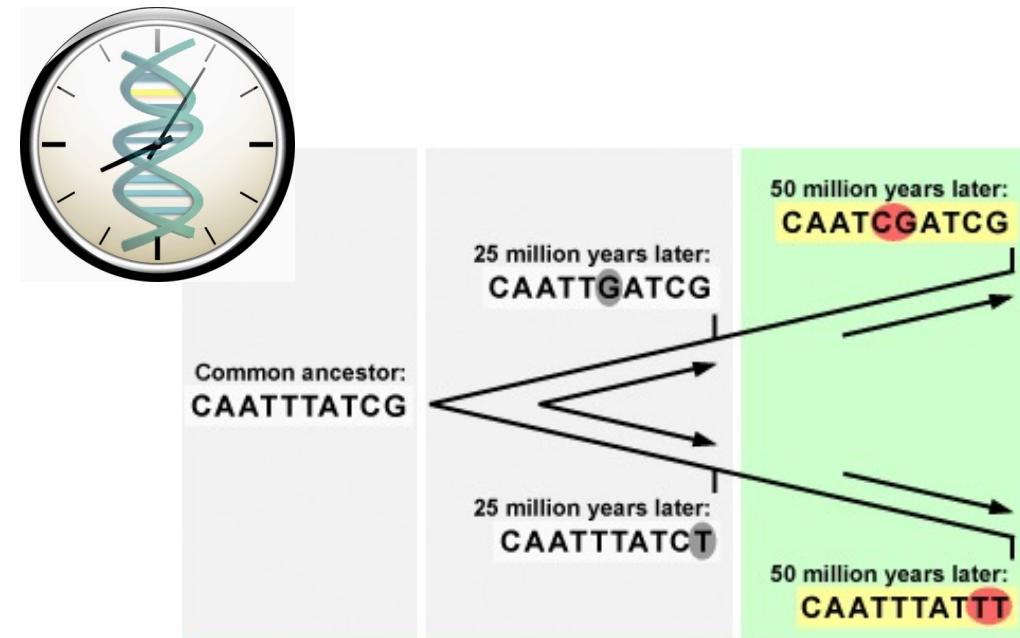


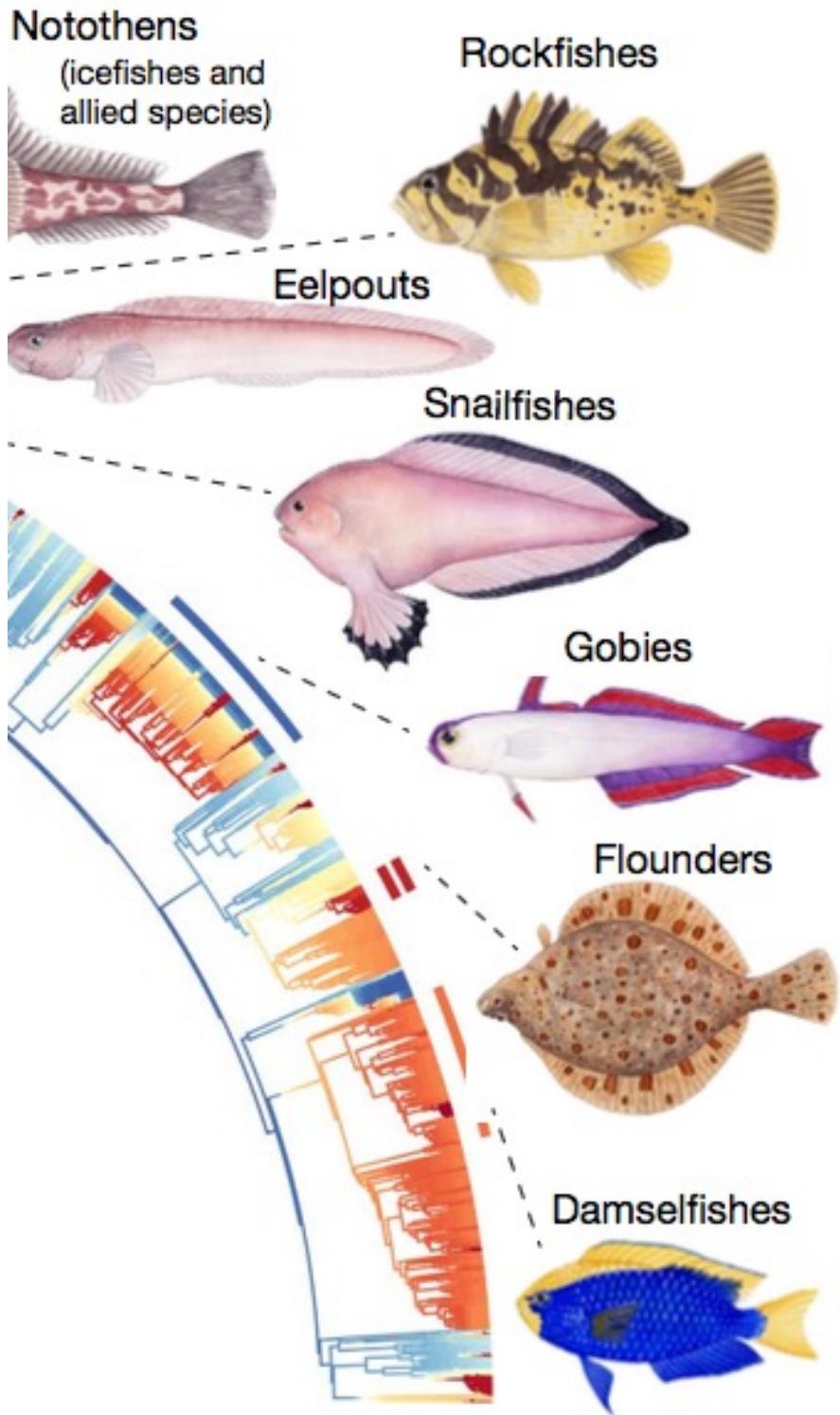
**Phylogenies represent the order and timing of divergences between ancestral species that led to present-day species**

Phylogenies are constructed from the genetic (and sometimes phenotypic) similarity between present-day species



The datation is performed with fossil calibrations and the molecular clock



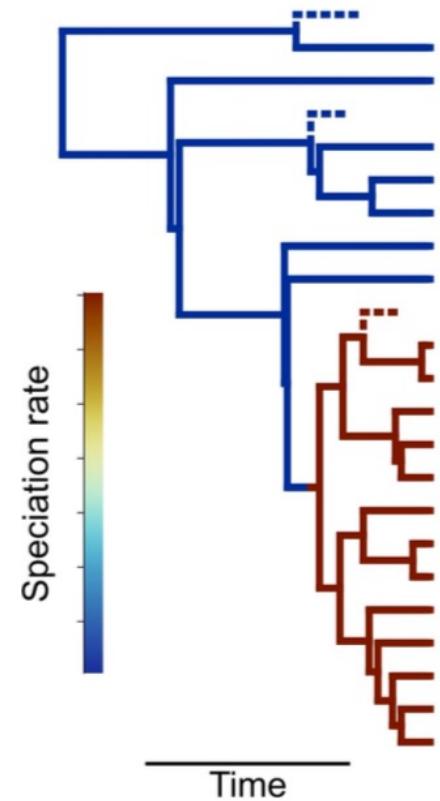


Dans ce qui suit, nous considérons l'arbre phylogénétique (daté) comme une donnée

# BUT

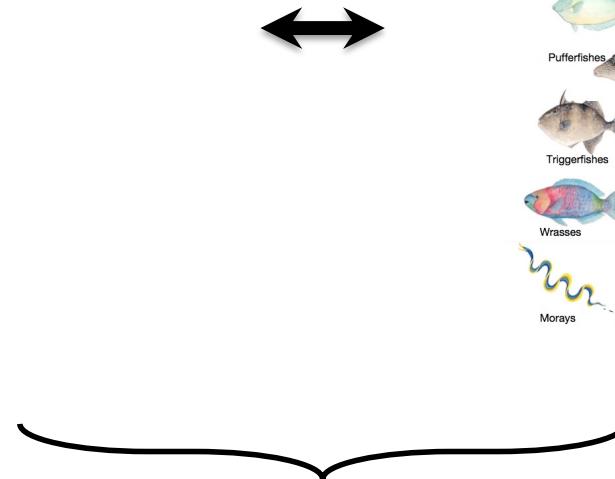
Développer des **modèles de diversification** ET des approches d'**inférence statistique** qui permettent d'ajuster les modèles à des **arbres phylogénétiques** de façon à **estimer les taux de spéciation et extinction**

Modèle de diversification

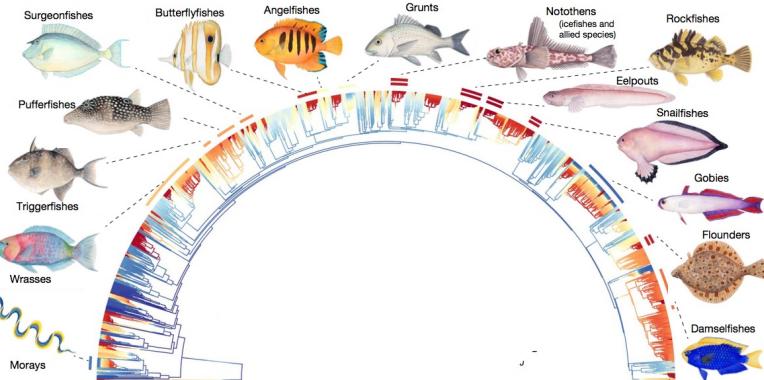


Inférence  
Statistique

Arbre phylogénétique



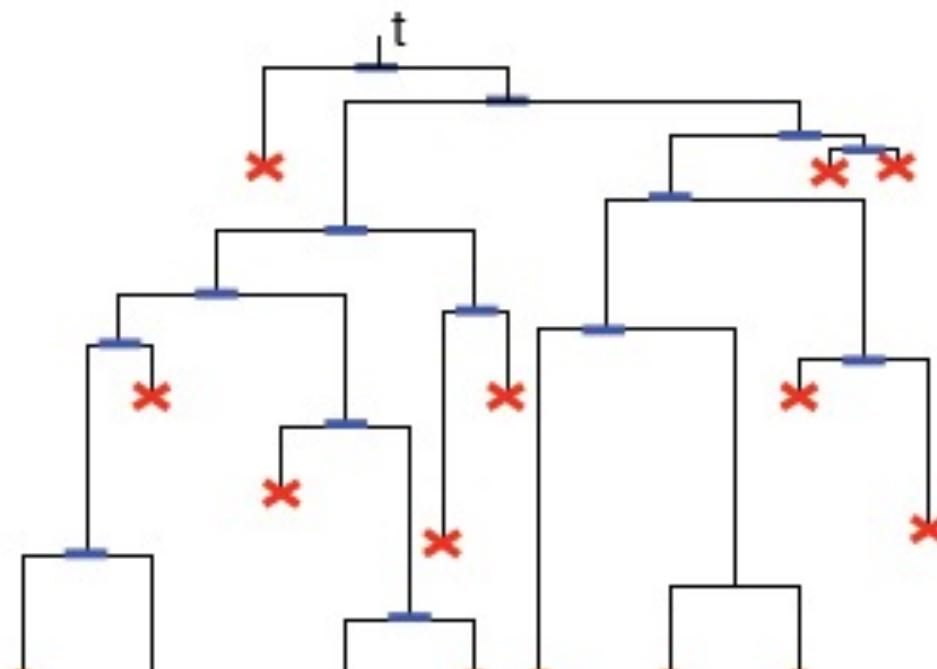
Estimation des taux de  
spéciation et extinction



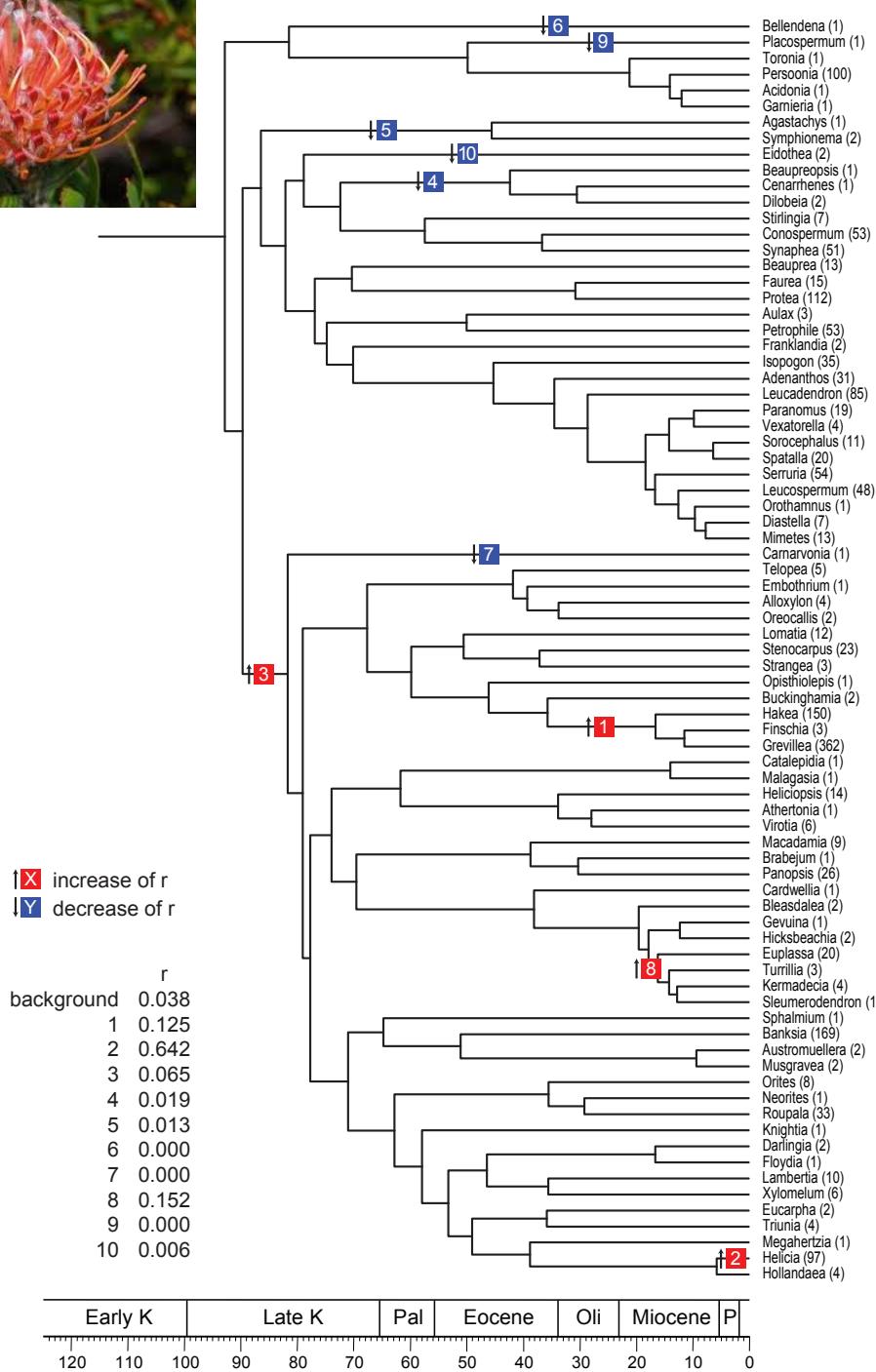
# Birth-death model for the analysis of diversification

We model the evolution of a given clade (group of species that contains a common ancestor and all its descendants) with stochastic birth-death models:

- the clade starts with a single ancestor at time T
  - species give rise to new species with the **per lineage per unit time rate of speciation**  $\lambda$ , and they go extinct with the **per lineage per unit time rate of extinction**  $\mu$



Ici une lignée est  
une espèce



# Estimating diversification from the age and size of a clade

In the absence of extinction

$$\hat{\lambda} = \frac{\log(n)}{T}$$

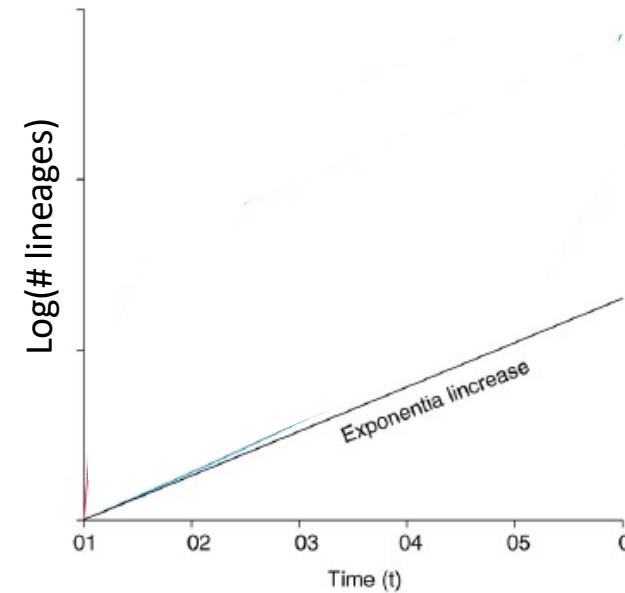
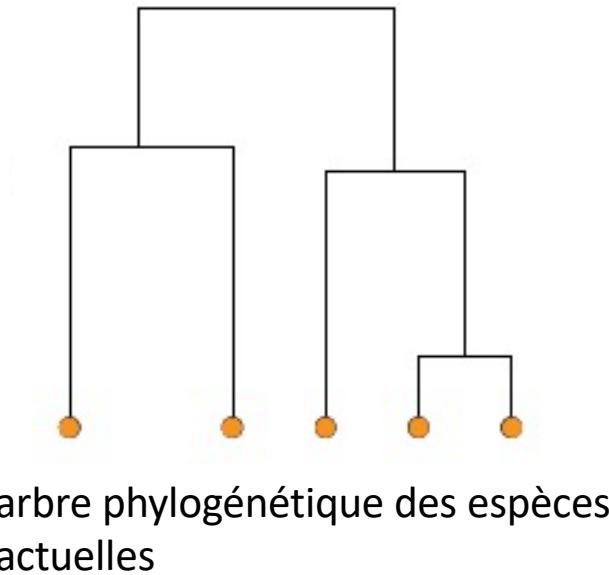
With extinction

$$\hat{r} = \frac{1}{T} \log(n(1 - \varepsilon) + \varepsilon)$$

$$\varepsilon = \frac{\mu}{\lambda}$$

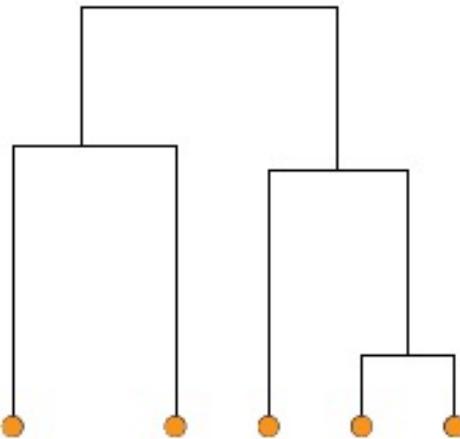
$$r = \lambda - \mu$$

# Estimating diversification using Lineage Through Time plots (LTT)

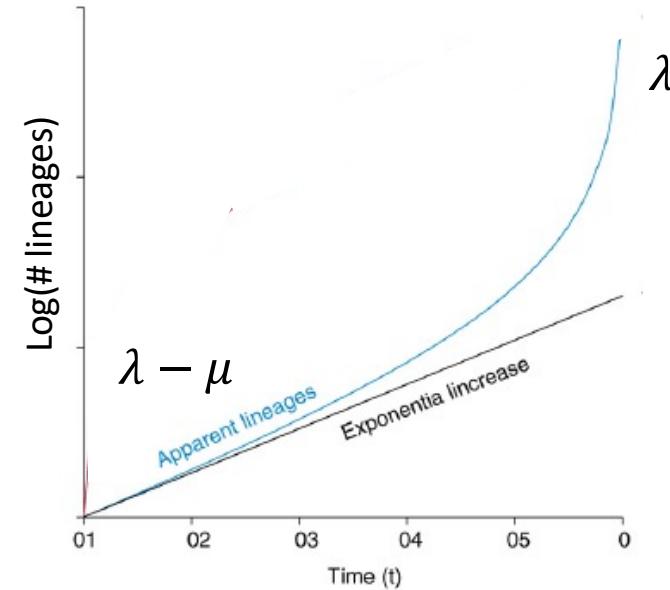


In the absence of extinction, an estimate of the speciation rate is given by the slope of the Lineage Through Time plot

# Estimating diversification using Lineage Through Time plots (LTT)



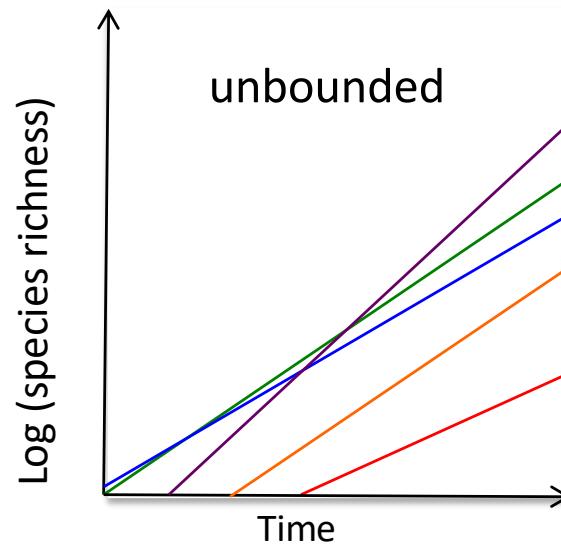
arbre phylogénétique des espèces actuelles



With extinction, the Lineage Through Time plot is characterized by an acceleration towards the present known as « the pull of the present »

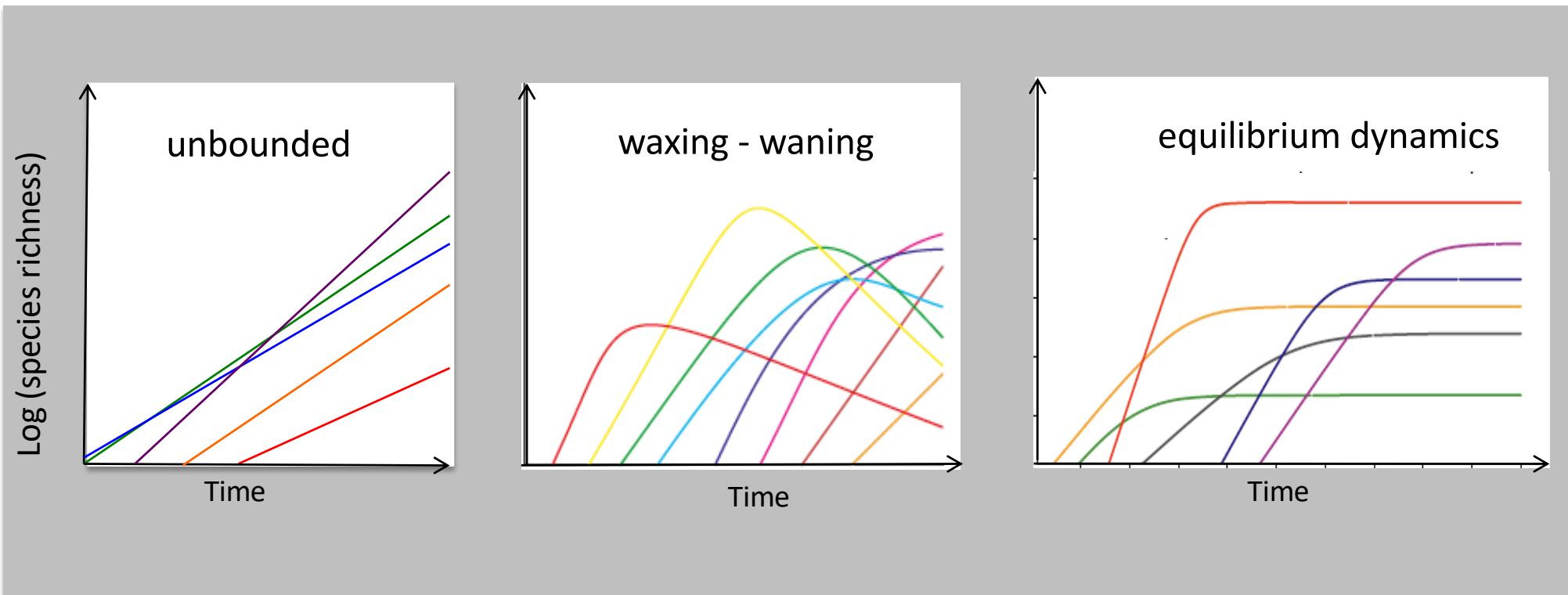
The slope towards the present provides an estimate of the speciation rate, the slope in the past provides an estimate of the net diversification rate.

All the above methods assume speciation and extinction rates are constant through time and homogeneous across lineages

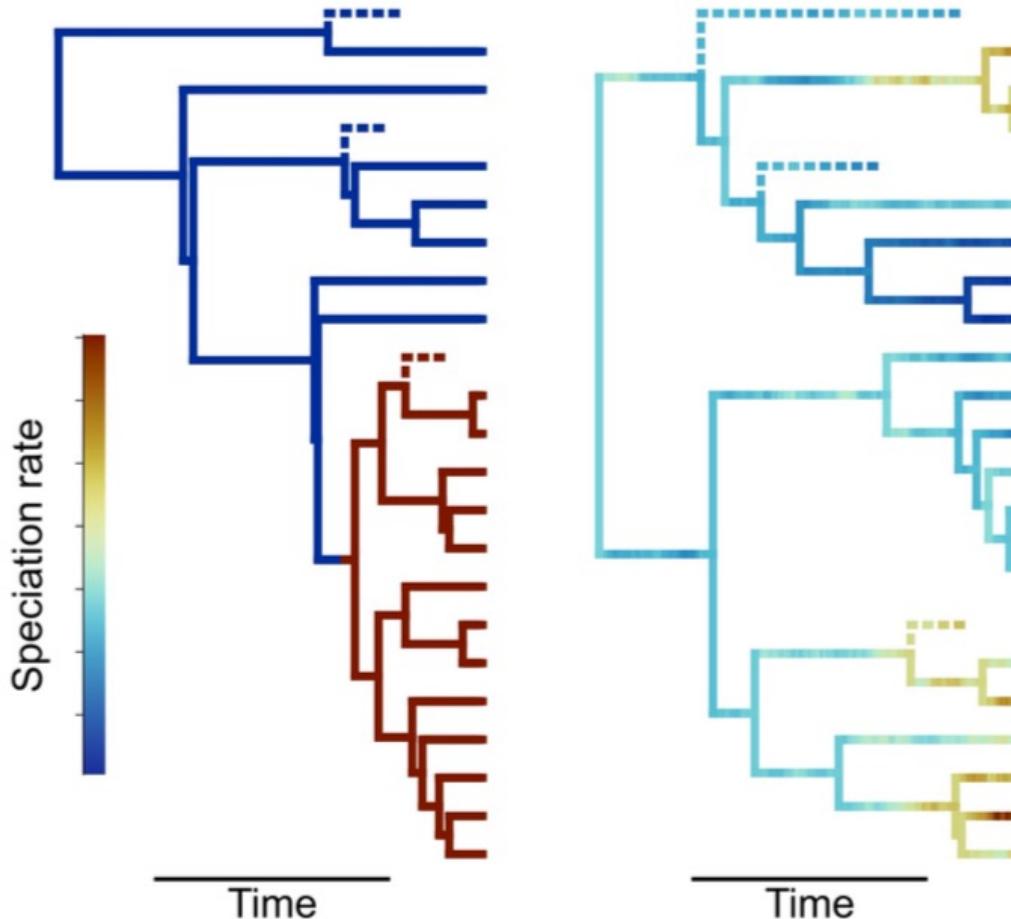


# What if biodiversity dynamics are not unbounded?

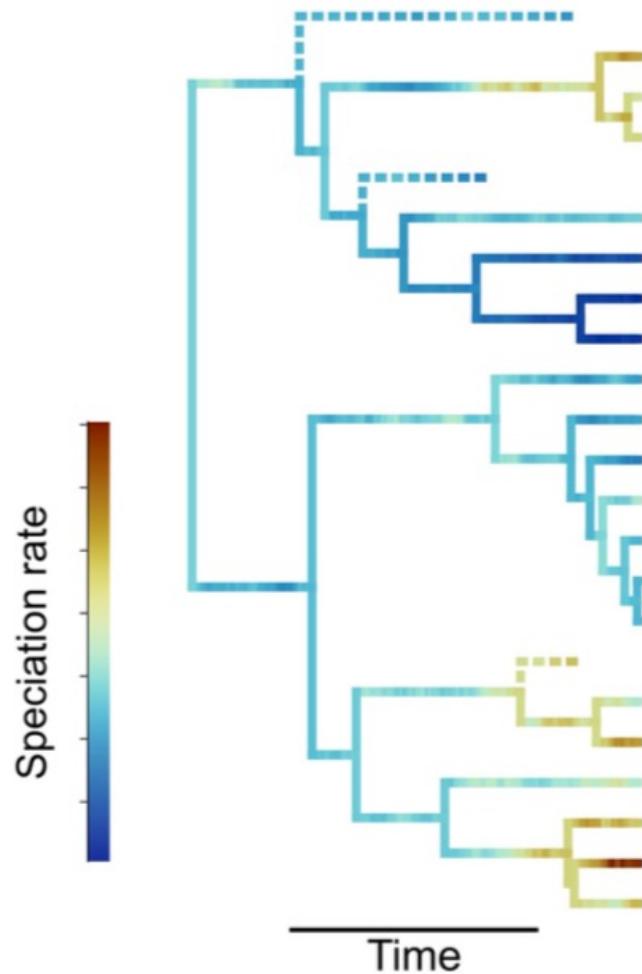
What if we want to test the support of different visions of how the evolution of diversity proceeds?



**What if we rates are not homogeneous across lineages  
and we want to test the support of different visions of  
how rate variation occurs?**



**Intuitivement, la distribution des temps de branchement informe sur la variation des taux dans le temps, la topologie informe sur la variation des taux entre lignées**

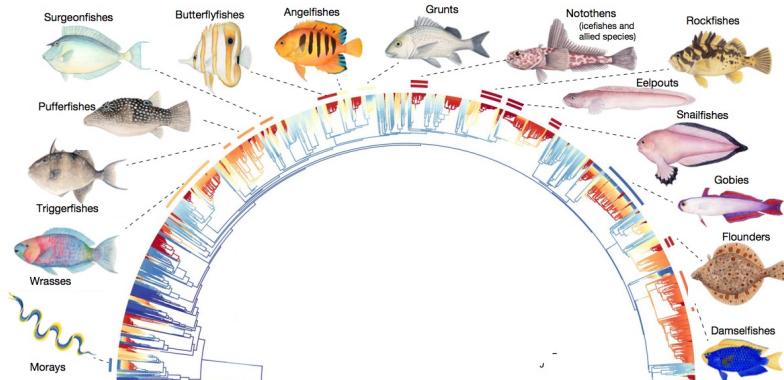
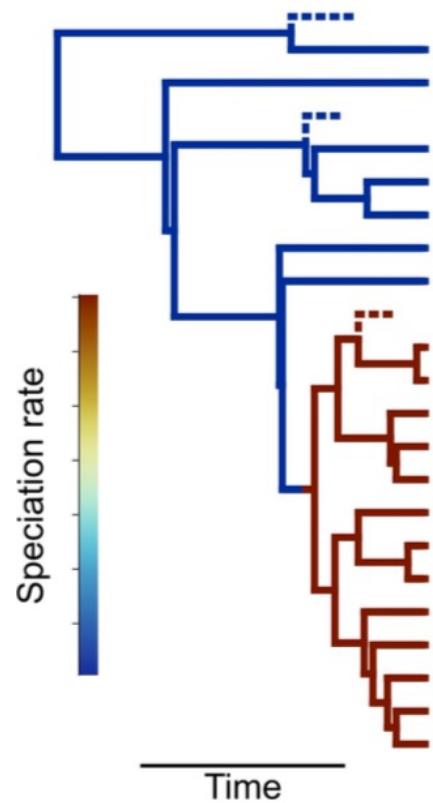


# Inférence Statistique

Modèle de diversification



Arbre phylogénétique



Estimation des taux de  
spéciation et extinction,  
Test d'hypothèses

# Inférence par vraisemblance

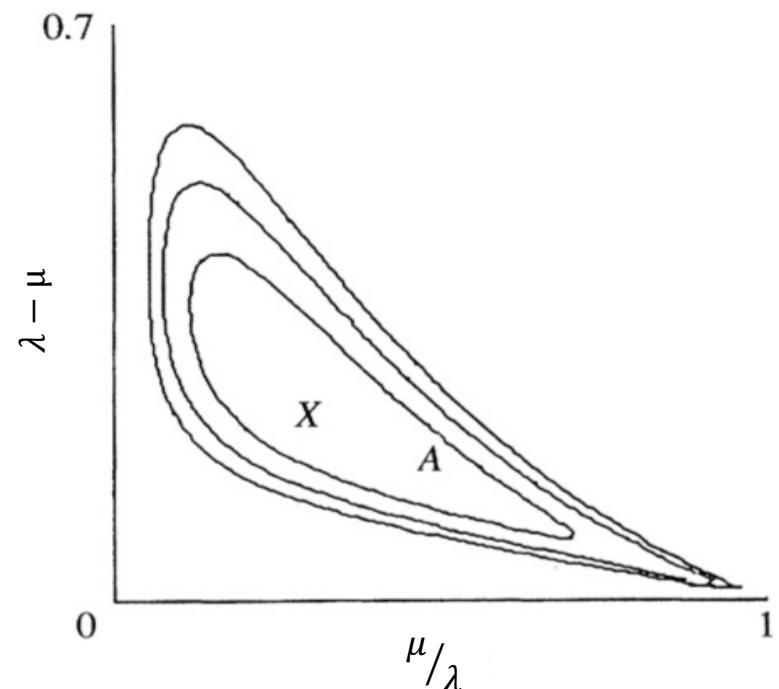
The likelihood is defined as

$$\mathcal{L}_x(\theta) = f_\theta(x)$$

where  $f_\theta(x)$  is the probability of observing  $x$  under the model for parameters  $\theta$

The ML estimate is the parameter  $\theta$  that maximizes  $\mathcal{L}_x(\theta)$

Contour de vraisemblance d'un modèle de naissance-mort sur une phylogénie simulée

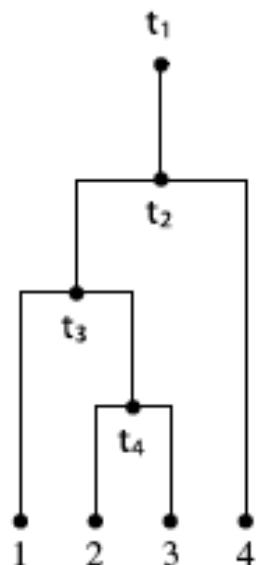


# Likelihood of a phylogeny of extant species under the birth-death process

stem age  $t_1$   
 speciation rate  $\lambda$   
 extinction rate  $\mu$

+

$\lambda$  and  $\mu$  can vary over time  
 sampling probability  $f$



sampling probability

probability that a lineage survives from  $t_1$  to  $t_2$  and leaves no descendant in the sample

$$\mathcal{L}(t_1, \dots, t_n) = \frac{f^n \Psi(t_2, t_1) \prod_{i=2}^n \lambda(t_i) \Psi(s_{i,1}, t_i) \Psi(s_{i,2}, t_i)}{1 - \Phi(t_1)},$$

speciation rate at time  $t_i$

probability that a lineage alive at time  $t_1$  has no descendant in the sample

# Likelihood of a phylogeny of extant species under the birth-death process

**birth-death model**

stem age  $t_1$

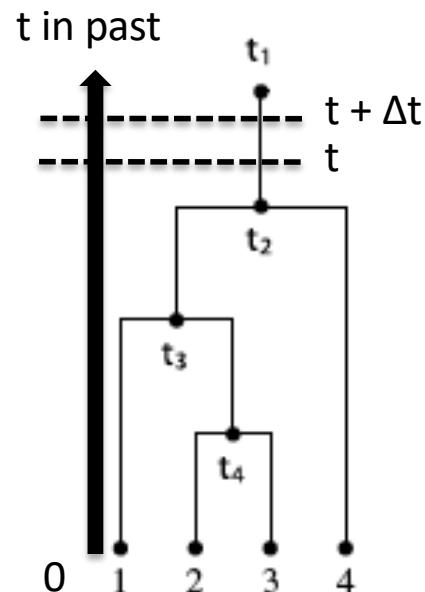
speciation rate  $\lambda$

extinction rate  $\mu$

+

$\lambda$  and  $\mu$  can vary over time

sampling fraction  $f$



$\Phi(t) = \mathbb{P}\{\text{a lineage is } \textit{not} \text{ in the sample} | \text{it was alive at the time } t\}$

$$\Phi(t + \Delta t) = \mu(t)\Delta t$$

$$+ (1 - \mu(t)\Delta t)\lambda(t)\Phi^2(t)$$

$$+ (1 - \mu(t)\Delta t)(1 - \lambda(t)\Delta t)\Phi(t)$$

$$+ o(\Delta t)$$

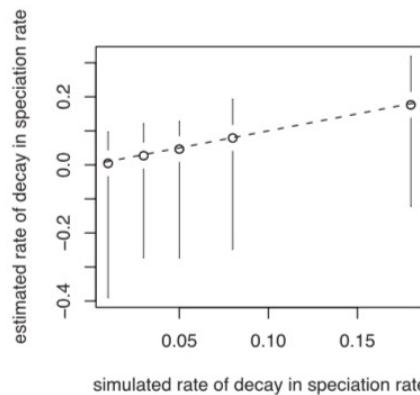
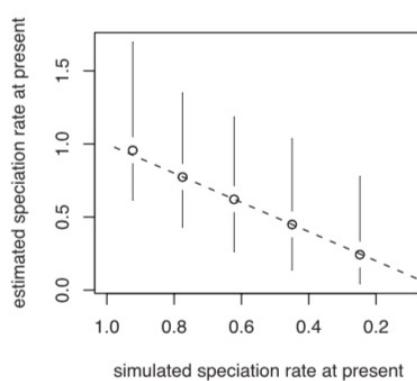
$$\Delta t \rightarrow 0$$

$$\frac{d\Phi}{dt} = \mu(t) - (\lambda(t) + \mu(t))\Phi(t) + \lambda(t)\Phi^2(t)$$

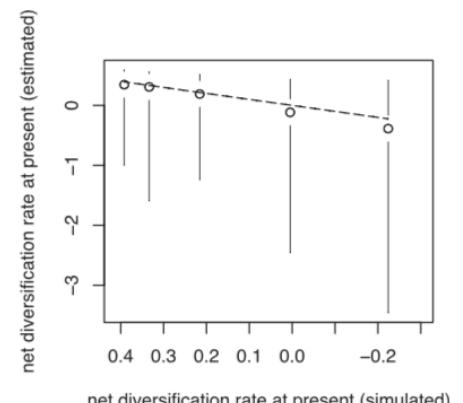
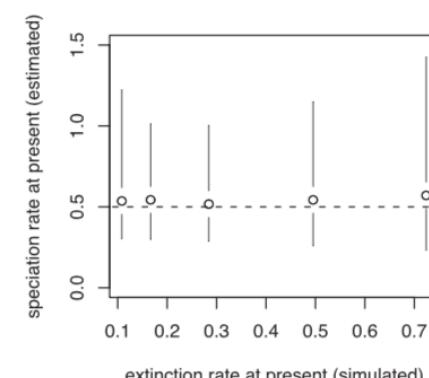
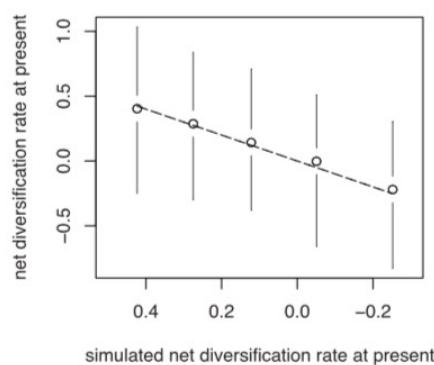
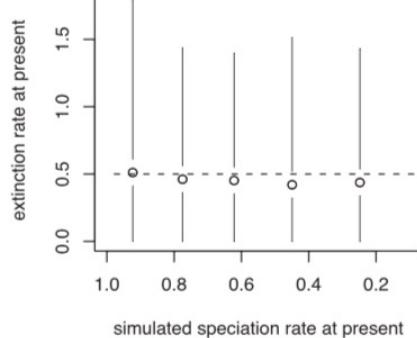
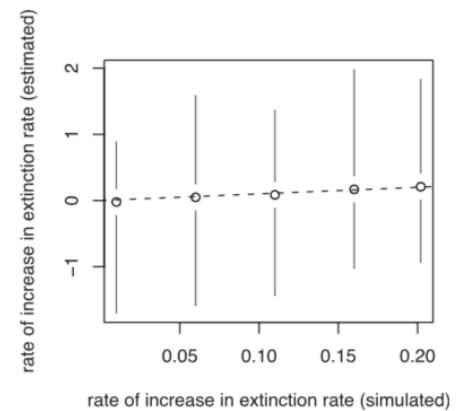
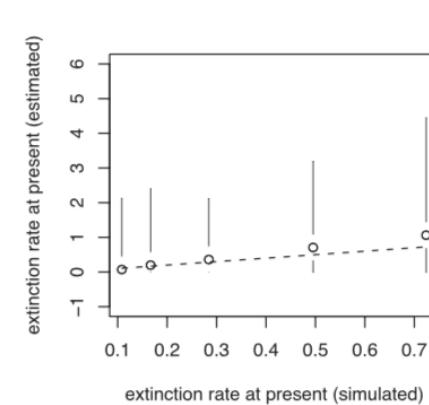
$$\Phi(t) = 1 - \frac{e^{\int_0^t \lambda(u) - \mu(u) du}}{\frac{1}{f} + \int_0^t e^{\int_0^s \lambda(u) - \mu(u) du} \lambda(s) ds}$$

# Unbiased parameter estimates

Exponential decay of speciation rate,  
constant extinction



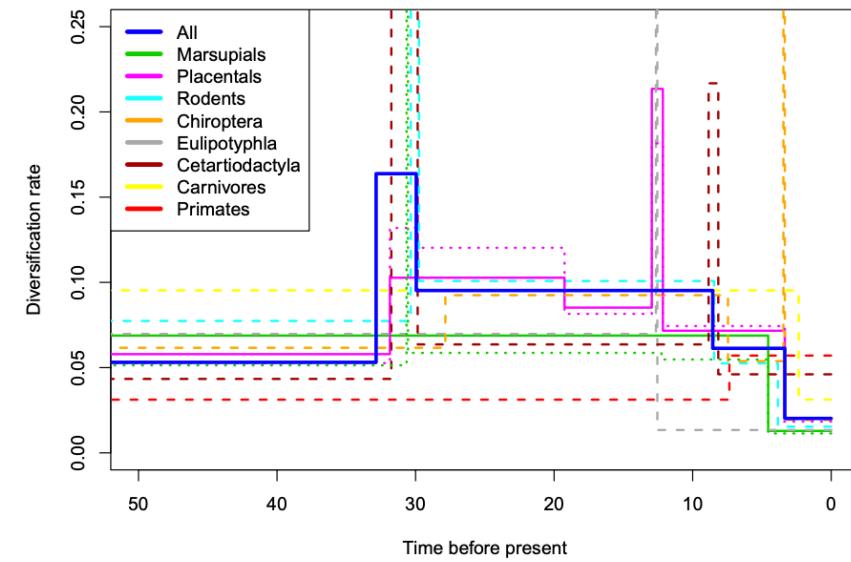
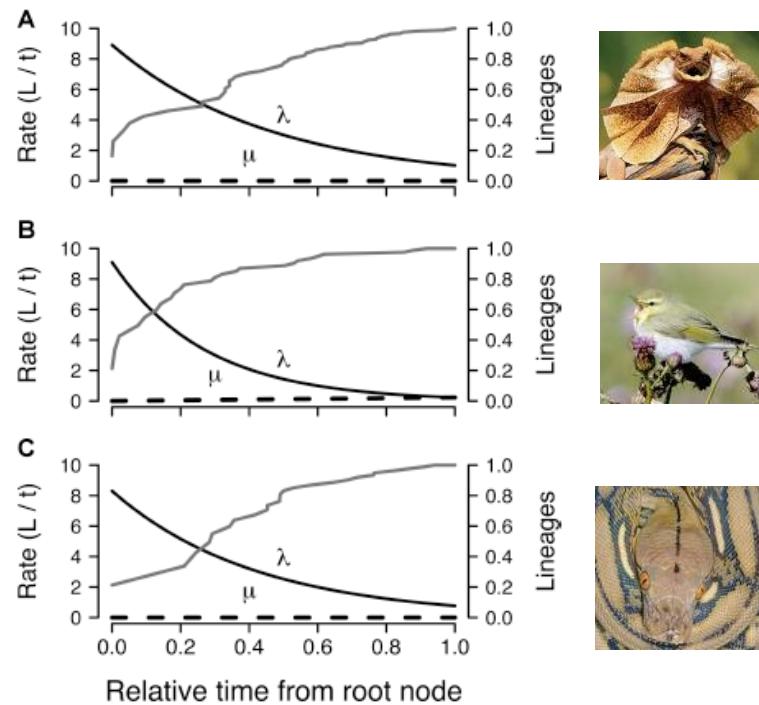
Exponential increase of extinction rate,  
constant speciation



**Do rates of species diversification vary through time?  
How?**

# Speciation rates often decline through time

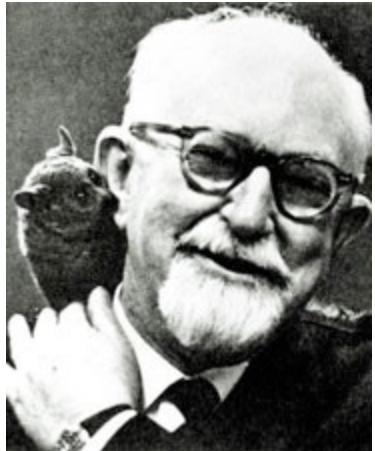
Estimates obtained by maximum-likelihood fit of birth-death models to phylogenies of present-day species



Stadler et al.  
PNAS 2011

Rabosky & Lovette Evolution 2008

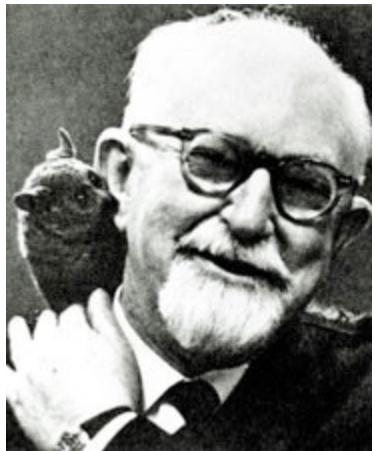
**Why do rates of species diversification vary through time?**



**Most diversity of life on Earth arises from adaptive radiations, the fast diversification of ecological traits in a rapidly speciating group of organisms**

**George Gaylord Simpson**

Under this hypothesis, diversification is fast in the presence of ecological opportunities, but slows down as these opportunities are exploited by an increasing number of species, generating so-called « Early burst » patterns.



# Diversity slowdowns linked to limited ecological opportunities and the diversity-dependent diversification model

George Gaylord Simpson

PROCEEDINGS OF THE ROYAL SOCIETY B | BIOLOGICAL SCIENCES

**Diversity-dependence brings molecular phylogenies closer to agreement with the fossil record**

Rampal S. Etienne, Bart Haegeman, Tanja Stadler, Tracy Aze, Paul N. Pearson, Andy Purvis and Albert B. Phillimore

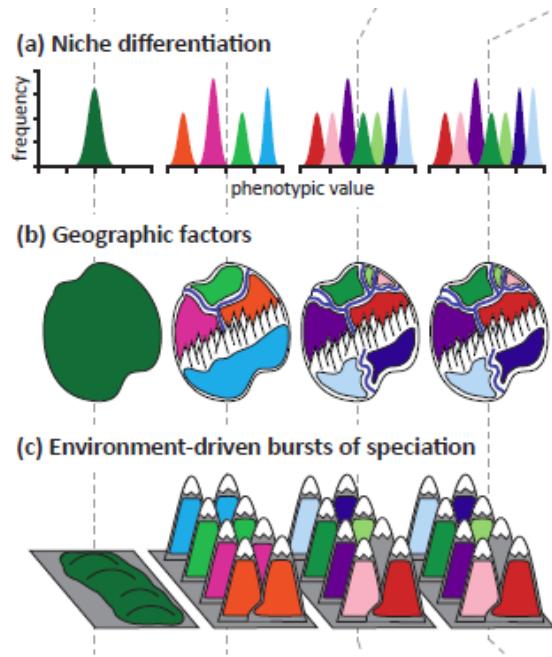
$$\lambda_n = \max\left(0, \lambda_0 - (\lambda_0 - \mu) \frac{n}{K}\right) \quad \text{and} \quad \mu_n = \mu$$



Maximum number of species

# Why does diversification slow down?

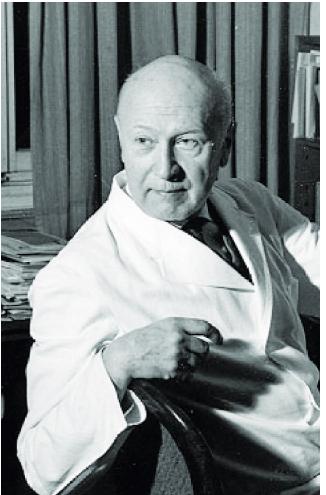
Daniel Moen and Hélène Morlon



Trends Ecol Evol 2014

Why are diversification slowdowns observed even when species do not coexist (and therefore do not compete for ecological opportunities)?

Do interactions with closely-related species necessarily impede diversification?



## The evolutionary speed hypothesis and other climate-related hypotheses

**Bernhard Rensch**

Warmer climates select for small-bodied species, which have fast generation times, high mutation rates, and therefore potentially higher speciation rates

Metabolic activity is faster under warm climates, potentially increasing the action of free radicals and increasing mutation rates

Warmer climates are often associated with increased climatic stability and productivity, which could promote speciation

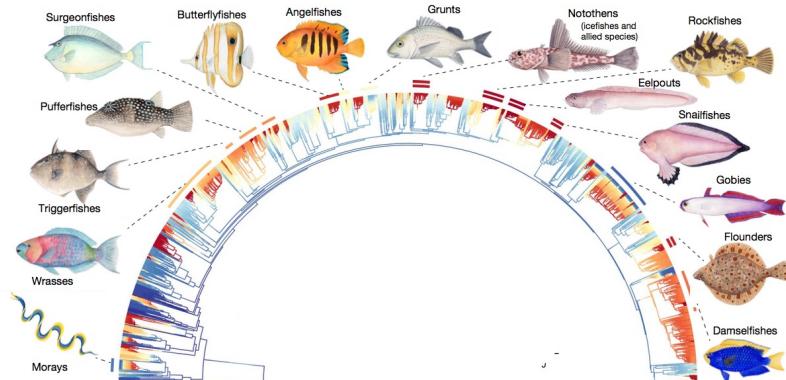
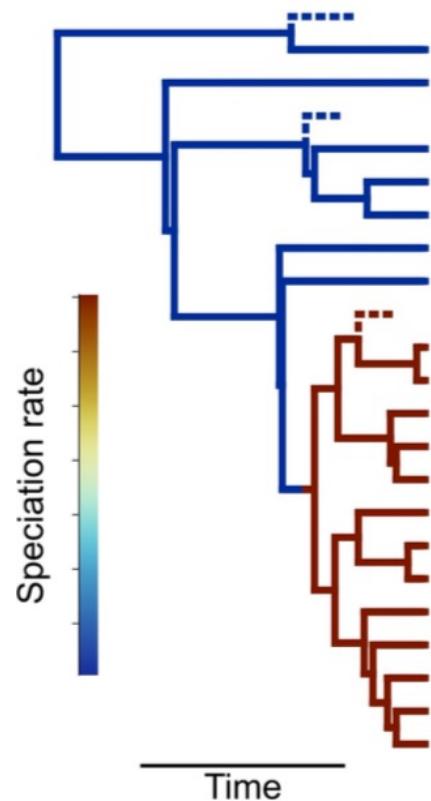
Could diversification slowdowns be related to the cooling of the Earth during the Cenozoic?

# Inférence Statistique

Modèle de diversification

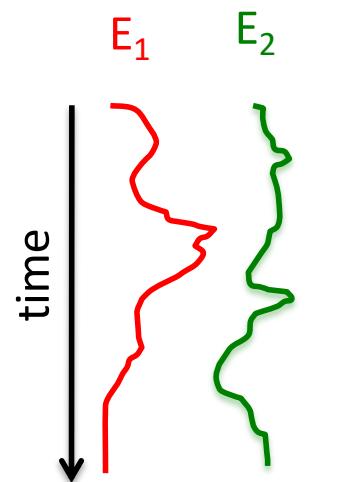


Arbre phylogénétique



**Test d'hypothèses par  
comparaison de  
vraisemblances**

# Models of diversification with rates that depend on measured (a)biotic variables



$$\tilde{\lambda}(t) = \lambda(t, E_1(t), E_2(t), \dots, E_k(t))$$

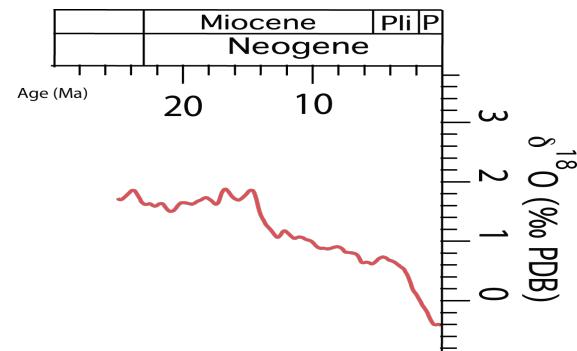
$$\tilde{\mu}(t) = \mu(t, E_1(t), E_2(t), \dots, E_k(t))$$

$$\mathcal{L}(t_1, \dots, t_n) = \frac{f^n \Psi(t_2, t_1) \prod_{i=2}^n \lambda(t_i) \Psi(s_{i,1}, t_i) \Psi(s_{i,2}, t_i)}{1 - \Phi(t_1)},$$

Condamine *et al.* Eco Lett 2013  
Lewitus *et al.* Syst Bio 2018

# Did past climatic changes affect diversification rates? How?

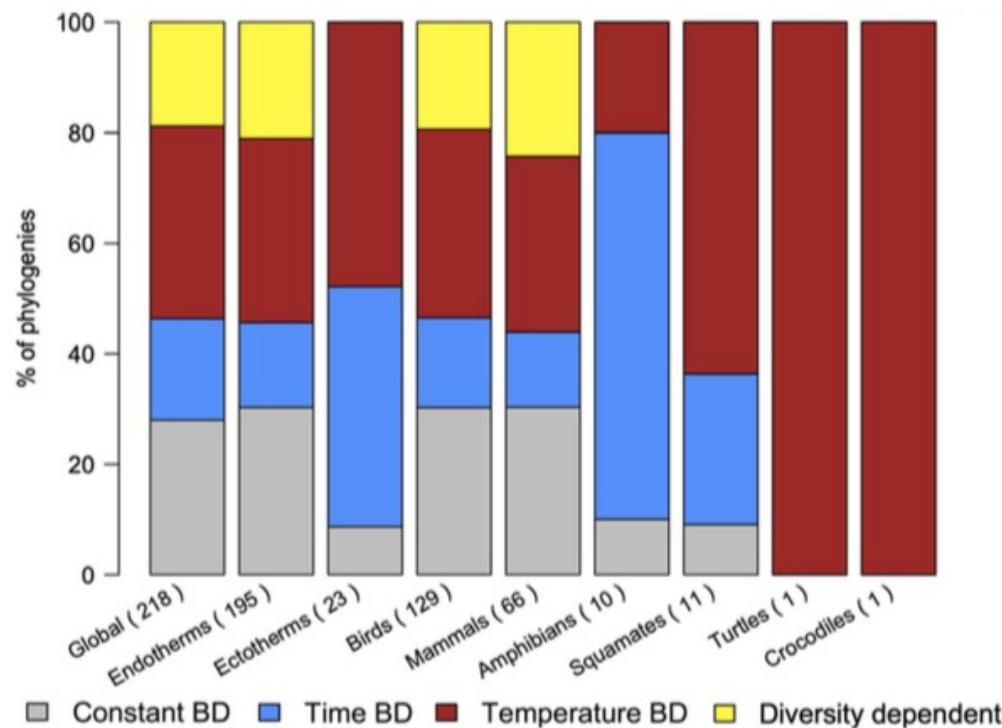
218 phylogenies of tetrapod families



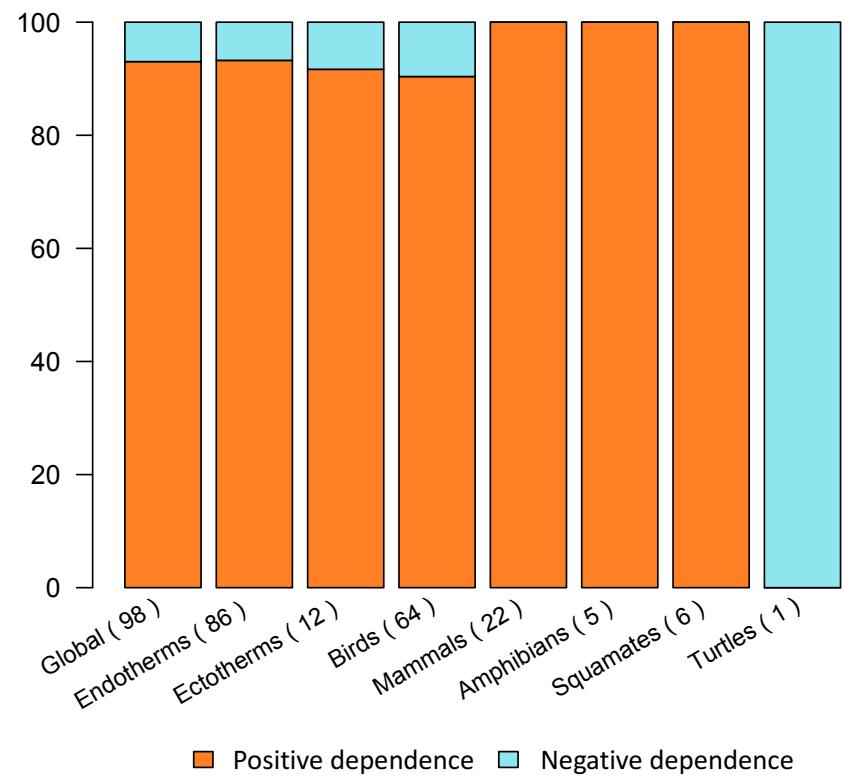
Comparison of 22 models including constant rate diversification models, models with time-varying rates, diversity-dependent rates, and temperature-dependent models

Condamine *et al.* Eco Lett 2019

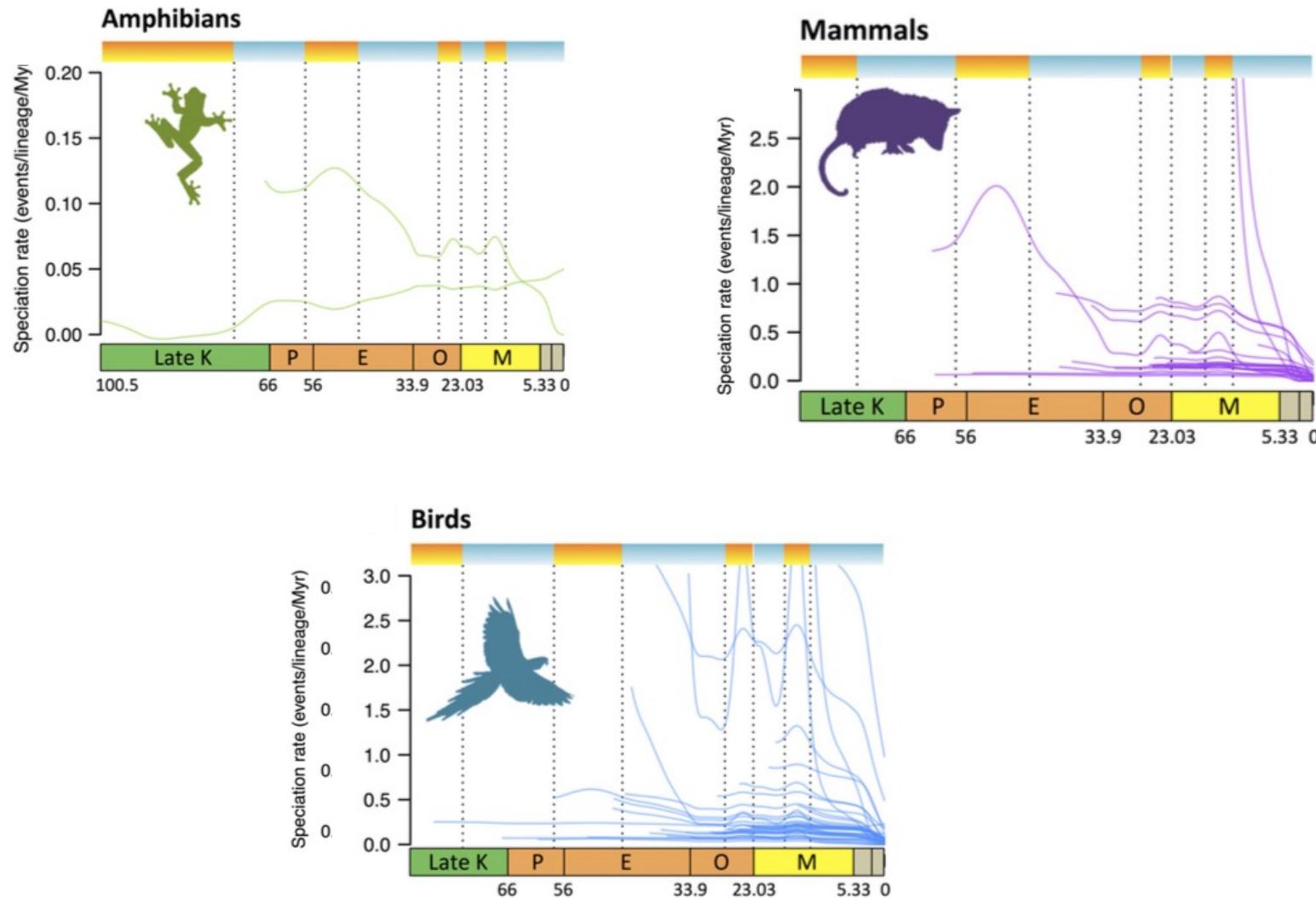
# Speciation rates often vary with temperature



# Speciation rates are higher during warm geological periods



# Climate cooling during the Cenozoic results in a slowdown in diversification



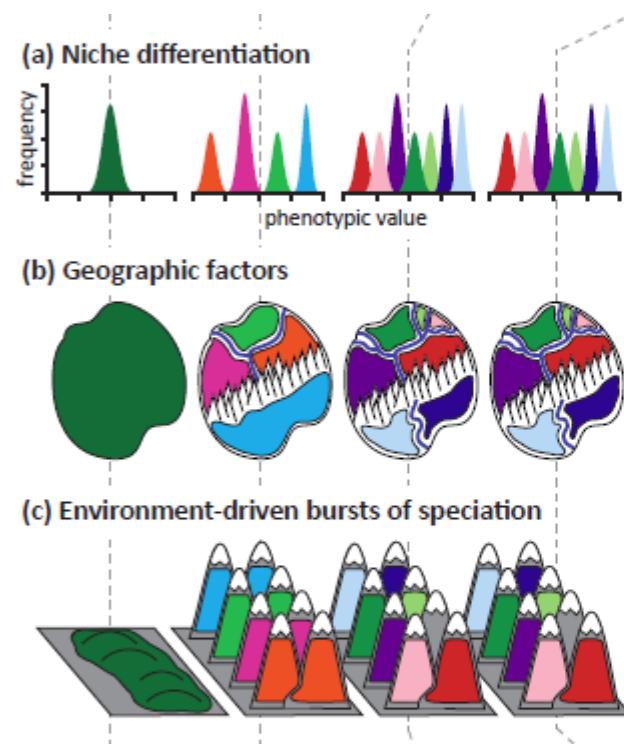
# Climate cooling provides a potential alternative explanation for speciation rates slowdowns to the often invoked filling of niche space

Opinion

CellPress

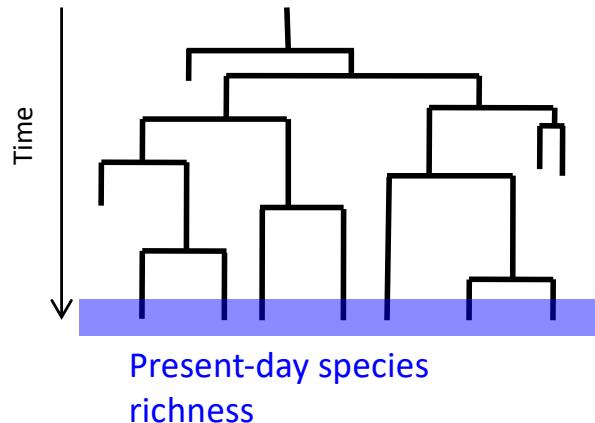
## Why does diversification slow down?

Daniel Moen and Hélène Morlon



Trends Ecol Evol 2014

# From estimates of speciation and extinction rates to estimates of past diversity



$$N(t) = N_0 e^{\int_0^t (-\lambda(s) + \mu(s)) ds}$$

↑

speciation rate      extinction rate

number of species today

Morlon *et al.* PNAS 2011

probability there were  $m$  species at time  $t$

given there were  $x$  species at time  $s$

and there are  $n$  species today

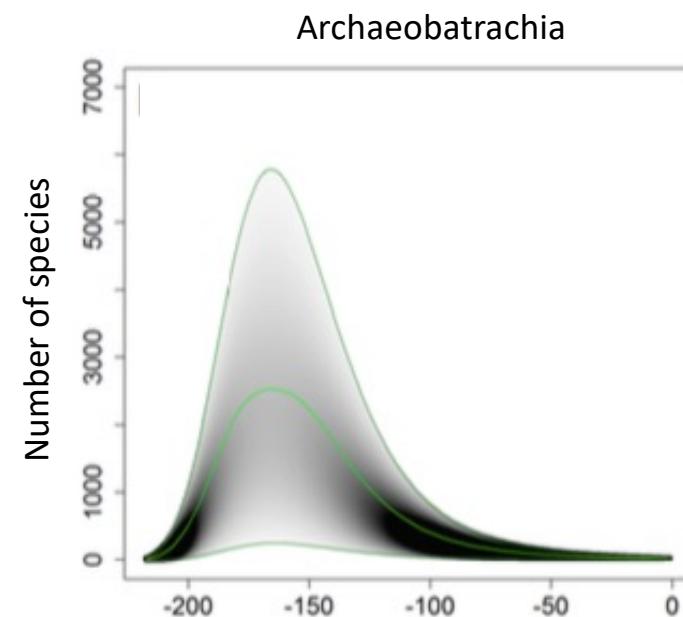
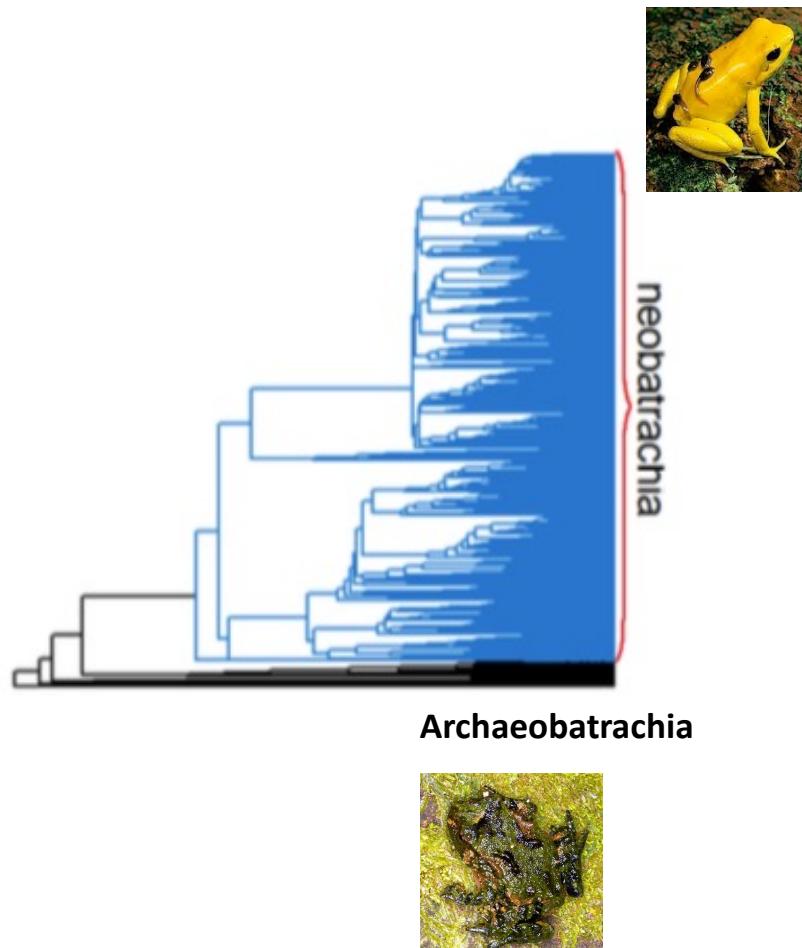
$\mathbb{P}(N(t) = m \mid N(s) = x, N(T_{pres}) = n)$



Olivier Billaud

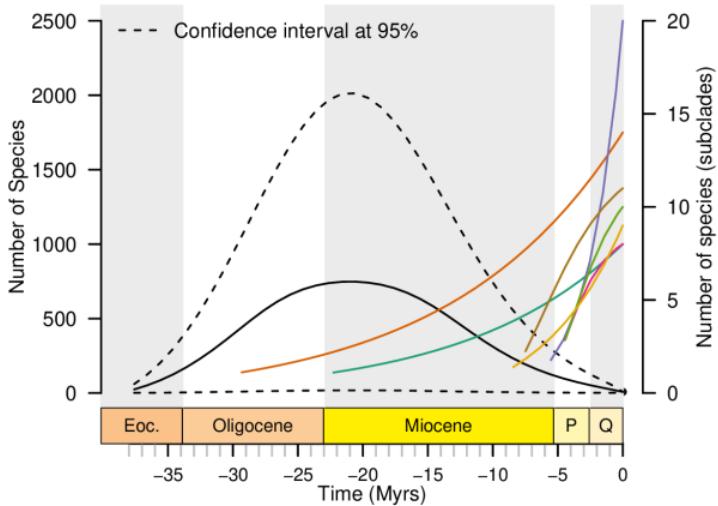
Billaud *et al.* Syst Bio 2019

# Are old and species-poor groups groups that have always be poor, or are they the remnants of a diverse past?

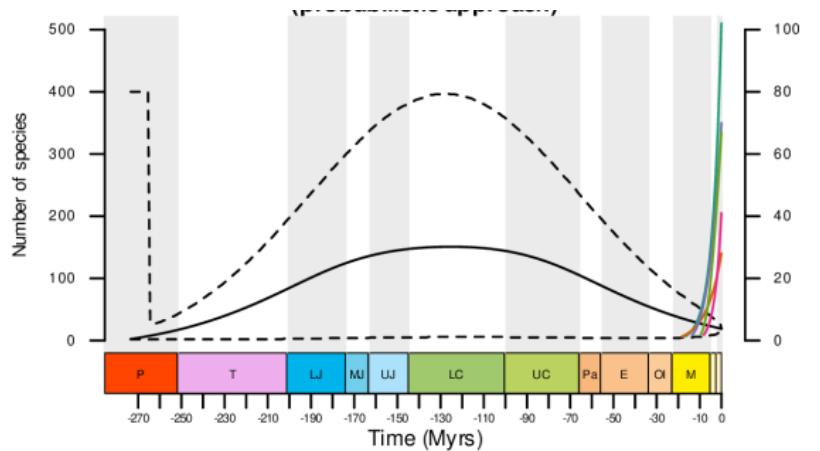
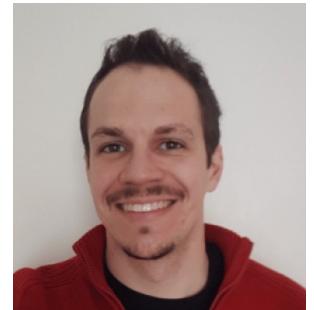


**Old and poor frog families are the remnant of a diverse past**

# Other examples of old and poor groups that are the remnant of a diverse past



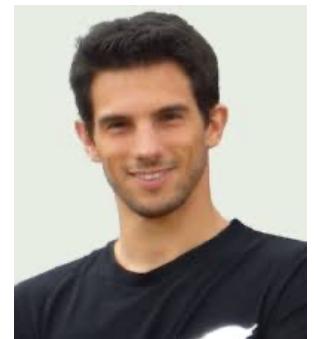
Nathan Mazet



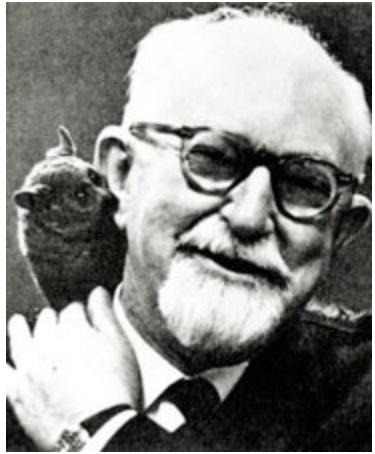
Pierre-Henri Fabre



Fabien Condamine



**Do rates of species diversification vary across lineages?  
How & Why?**

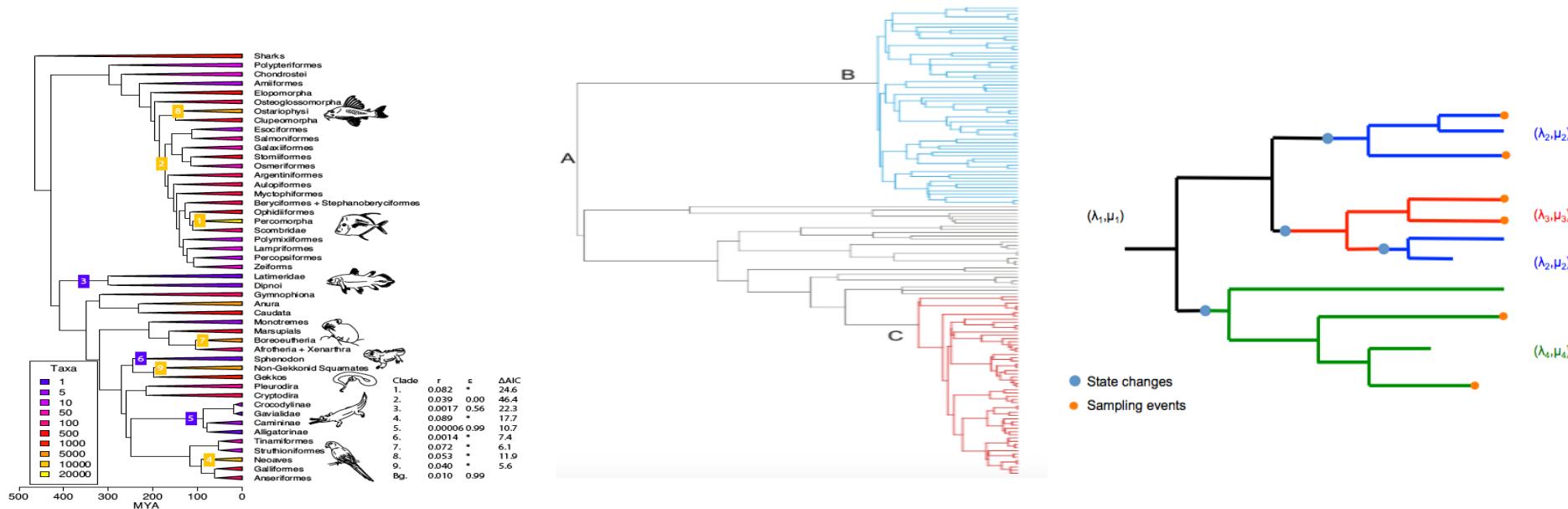


**Most diversity of life on Earth arises from adaptive radiations, the fast diversification of ecological traits in a rapidly speciating group of organisms**

**George Gaylord Simpson**

Under this hypothesis, bursts of diversification are clade-wide, linked to the rapid filling of a niche space that has been freed from other occupants (e.g. by major environmental changes) or opened by a major key innovation.

# Heterogeneous birth-death models with clade-wide rate variation: few rate shifts with large effects



**MEDUSA**  
Alfaro et al. PNAS 2009

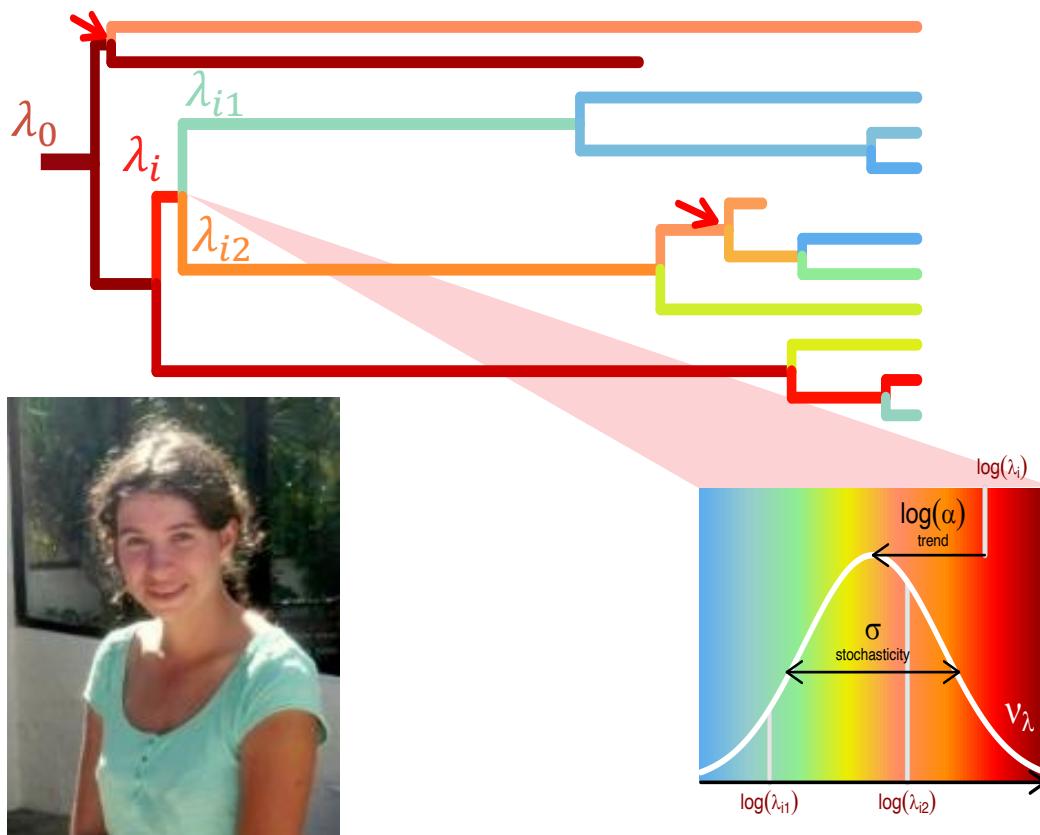
**BAMM**  
Rabosky PloS One 2014

**MSBD**  
Barido-Sottani et al. Syst Bio 2020

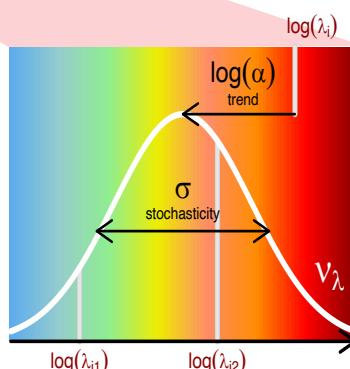
# Another view of diversification

The complex interplay between species evolving ecologies and their specific spatial and environmental context results in highly dynamic diversification rates

The Cladogenetic Diversification rate Shift model (ClaDS):  
a new model with lineage-specific rate variation

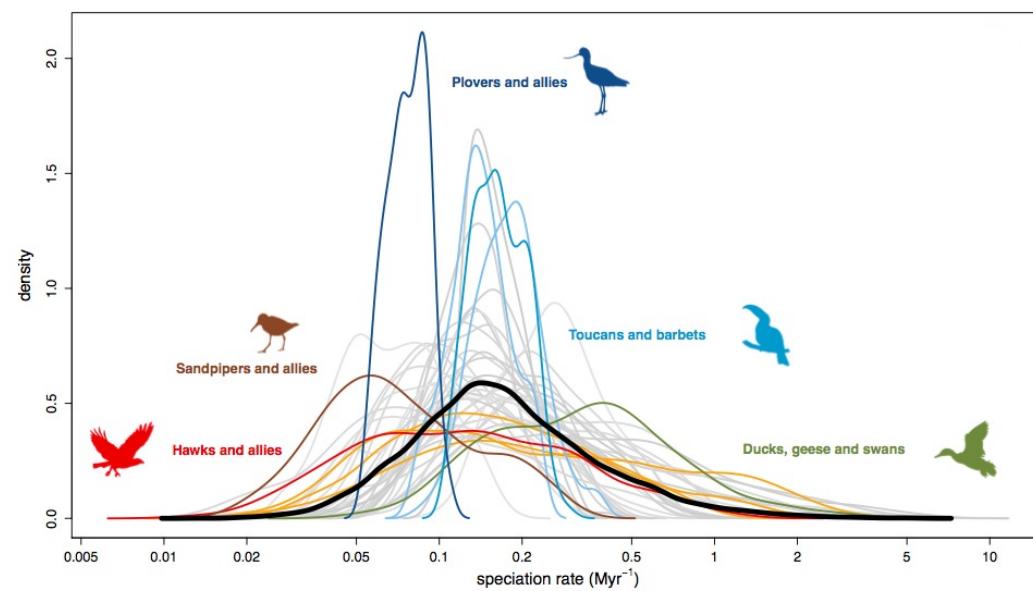
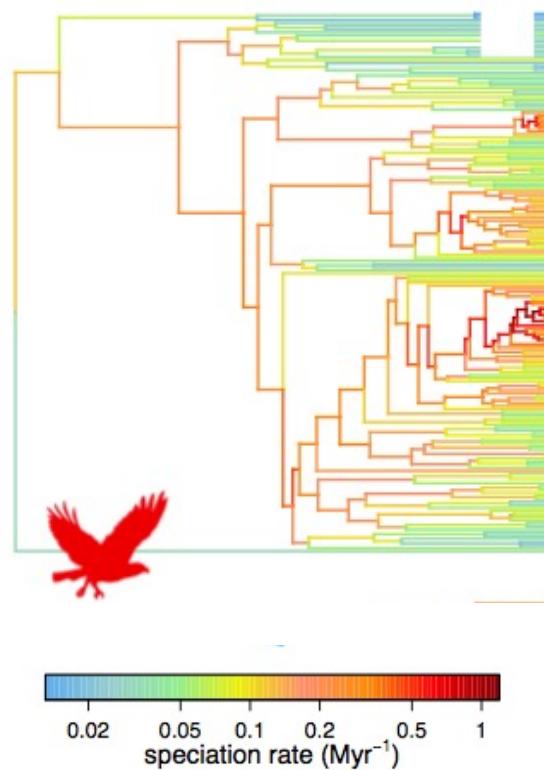


- $\lambda_0$  initial speciation rate  
 $\alpha$  deterministic trend  
 $\sigma^2$  stochastic variation  
 $\varepsilon = \mu_i / \lambda_i$  relative extinction rate

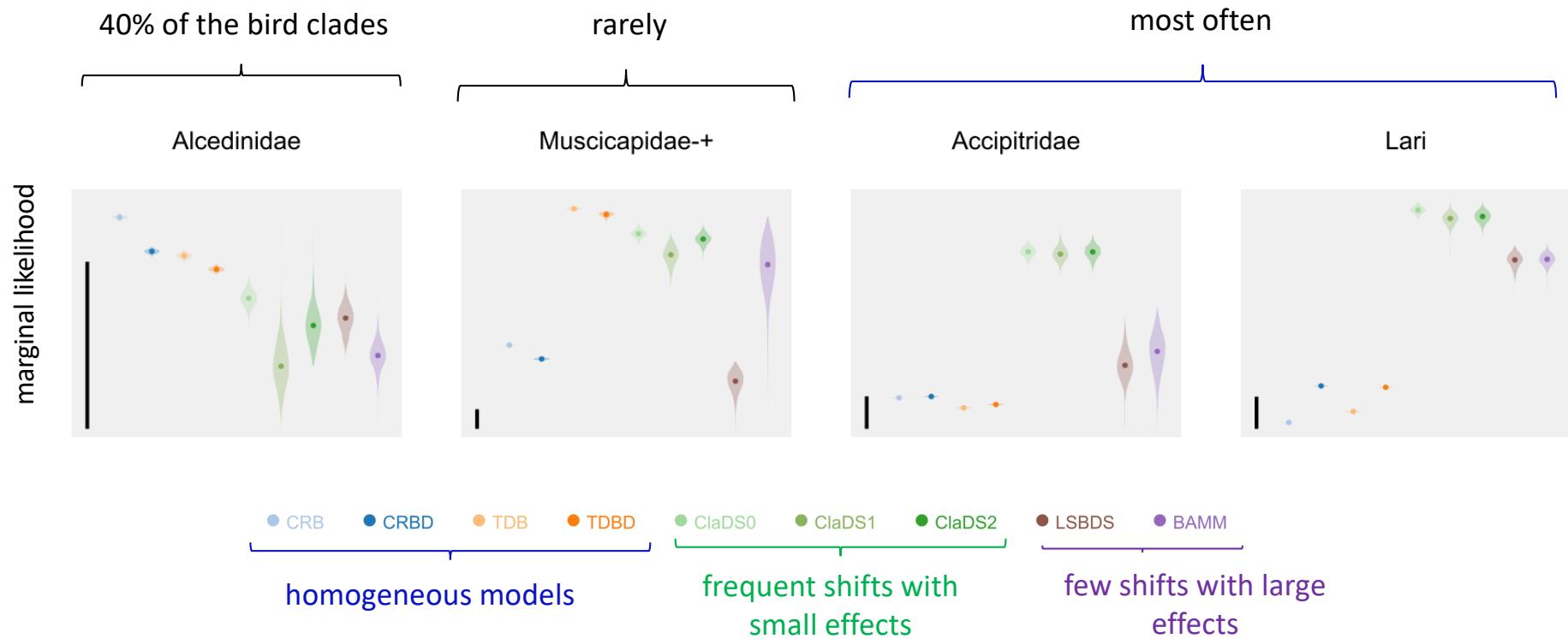


**Maliet et al.**  
*Nature Ecology & Evolution* 2019

# Speciation rates vary widely across lineages



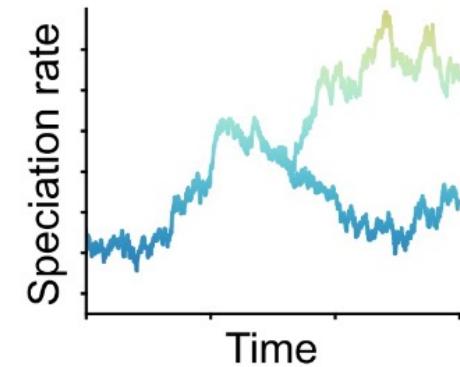
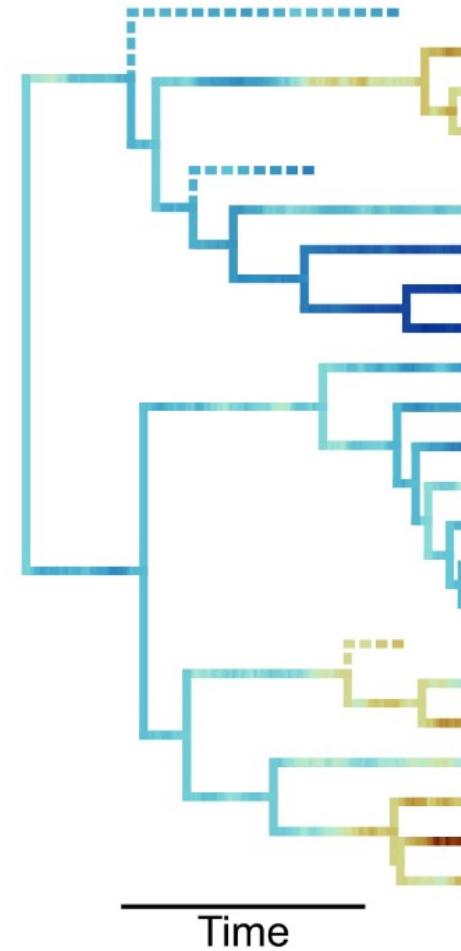
# Models with many small shifts are better supported than models with few large shifts



# The Birth-Death Diffusion model (BDD): continuous diffusion of diversification rates

Speciation

$$d\ln(\lambda_i(t)) = \alpha dt + \sigma_\lambda dW(t),$$



Quintero *et al.* BioRxiv 2022

# The Birth-Death Diffusion model (BDD): continuous diffusion of diversification rates

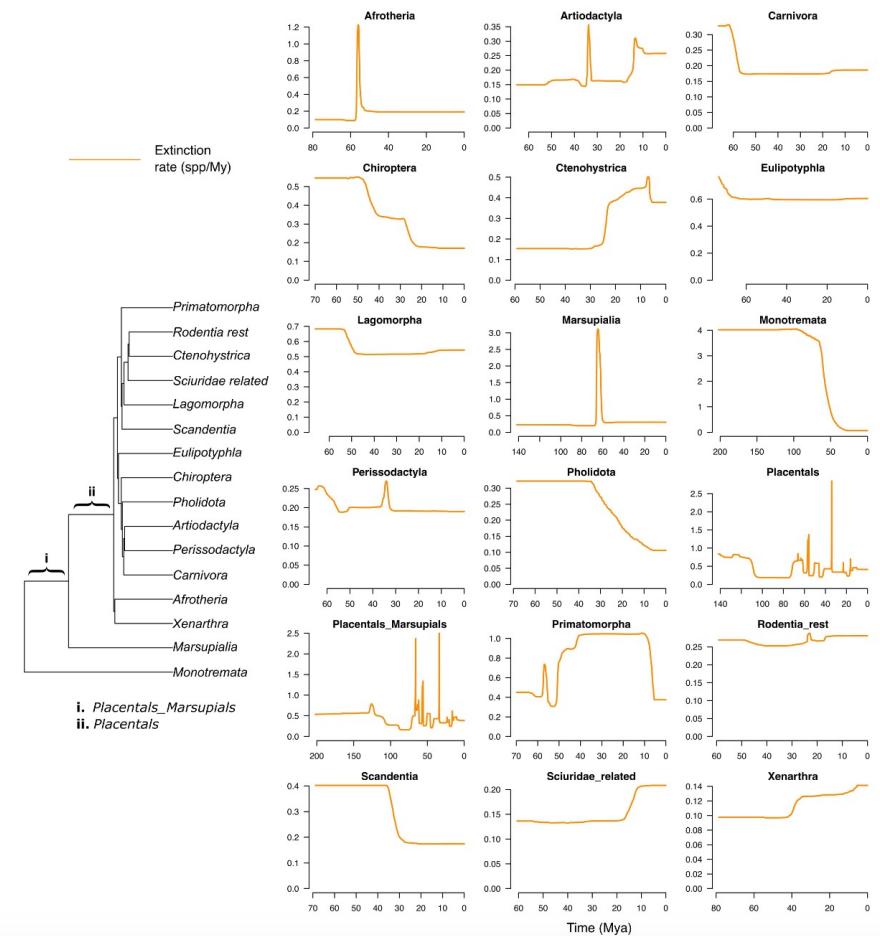
Extinction not constrained by fossil information

- No extinction
- Constant extinction
- Constant turnover
- Follows a Geometric Brownian Motion (GBM)

$$d\ln(\mu_i(t)) = \sigma_\mu dW(t),$$

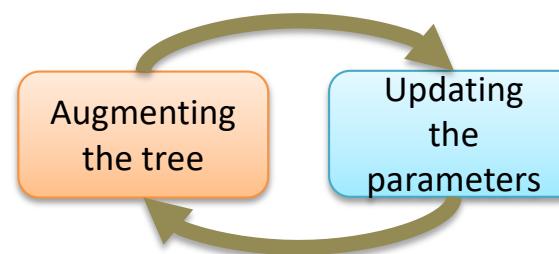
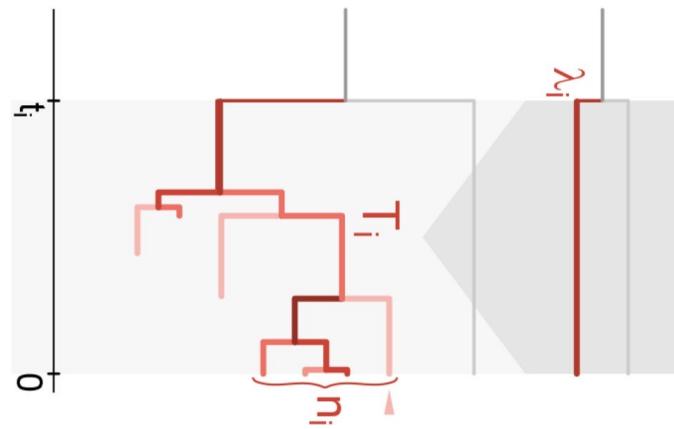
where  $W(t)$  denotes the Wiener process.

Extinction constrained by fossil information

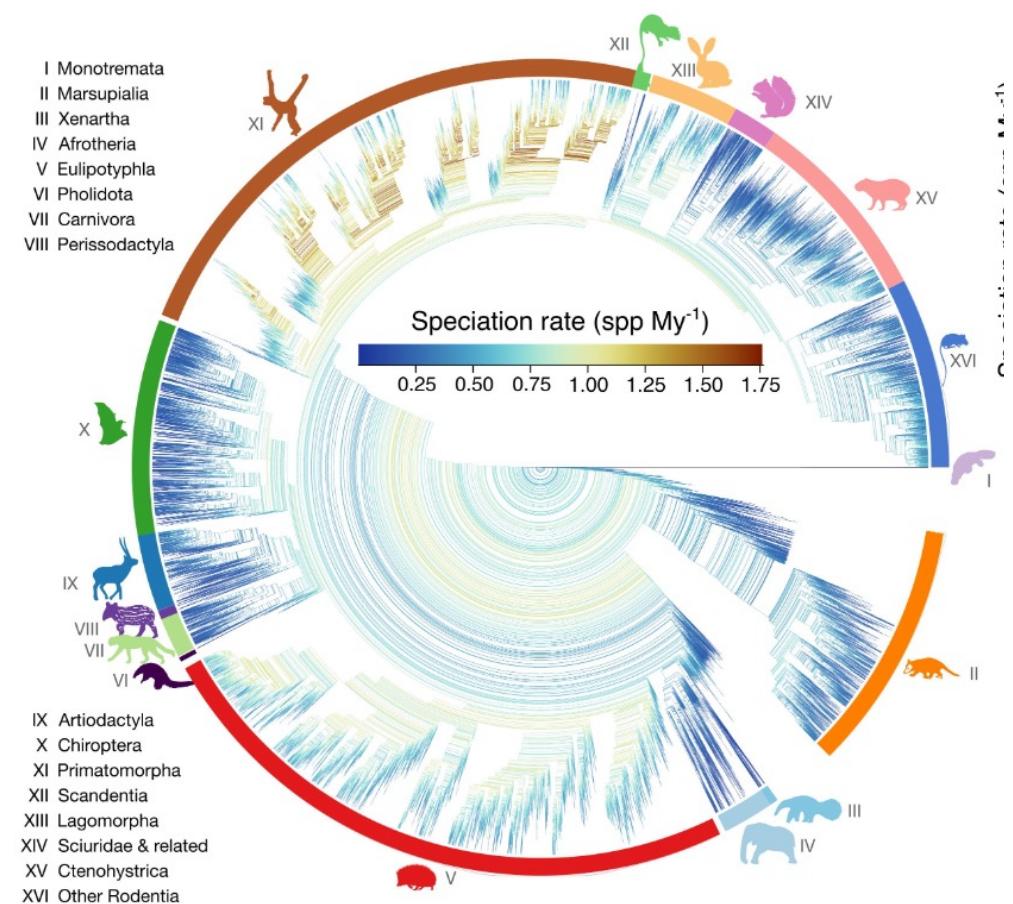


# Inference with data augmentation

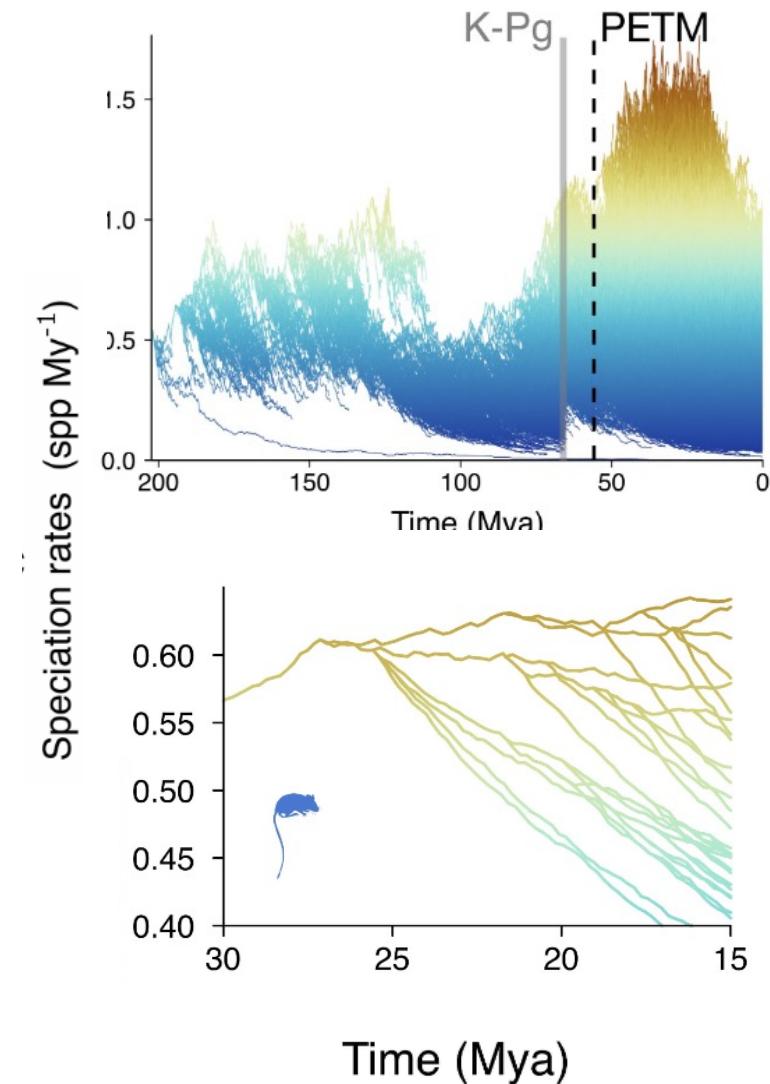
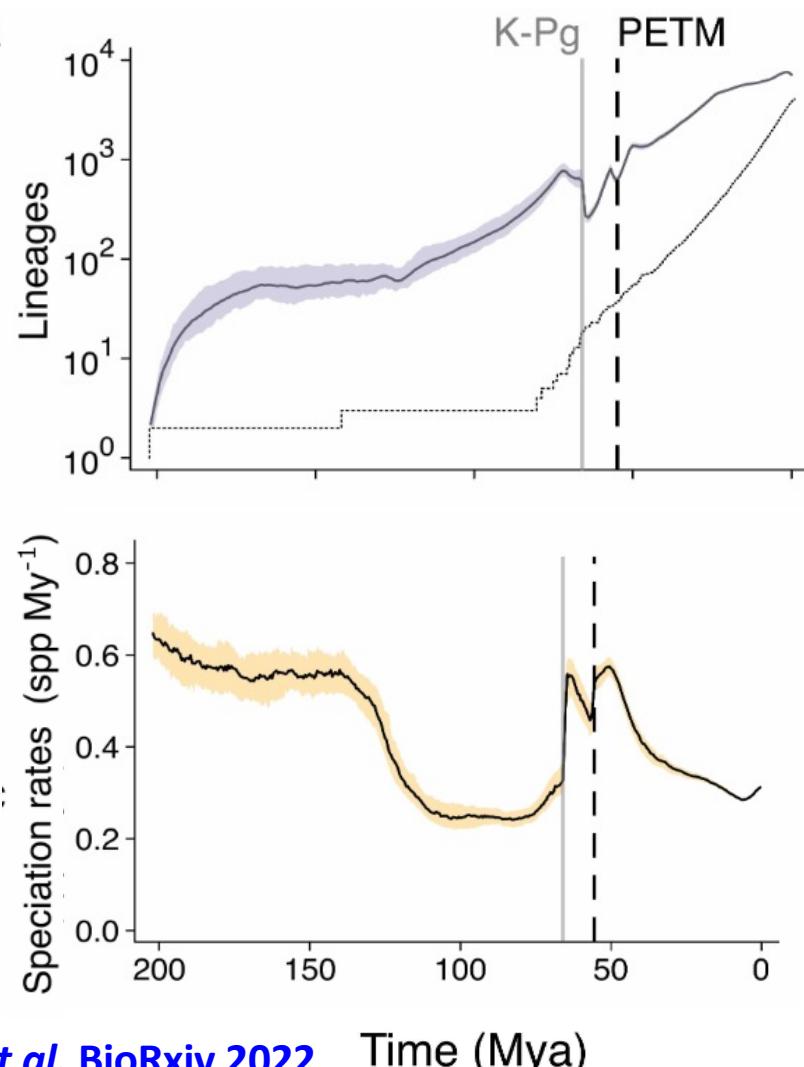
ClaDS

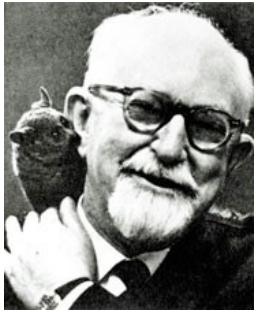


BDD

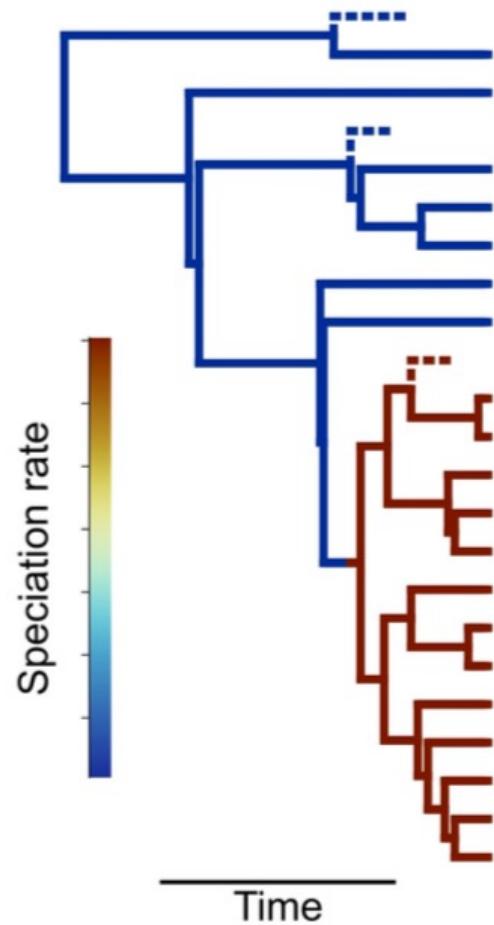


# Reconstruction of Mammals past diversification and diversity dynamics under the Birth-Death Diffusion model using data augmentation





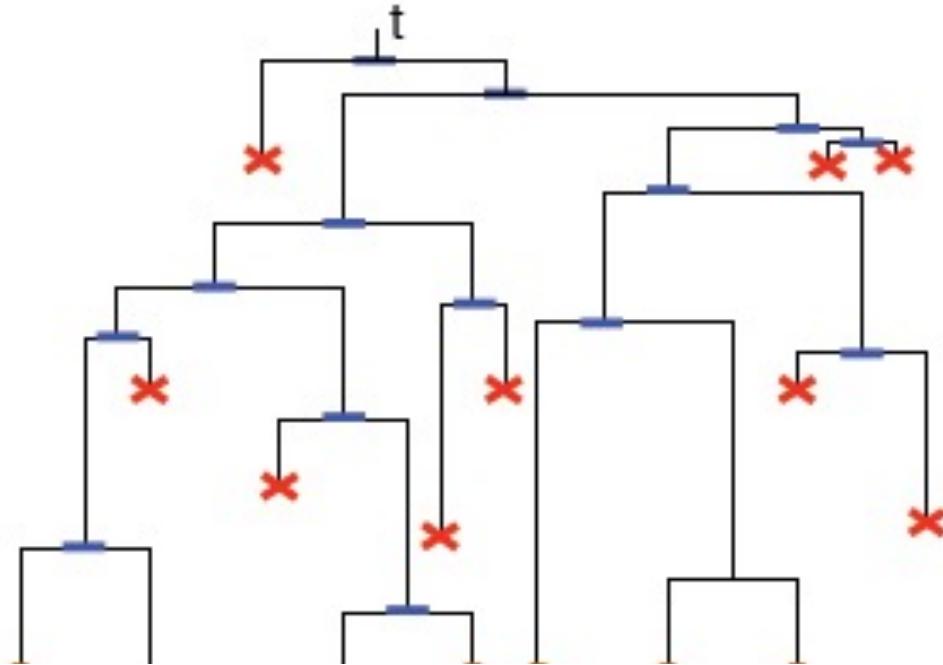
## Major key innovations Adaptive radiations



Complex interplay between species evolving ecologies and their specific spatial and environmental context



# Birth-death model for the analysis of diversification



Ici une lignée est  
une espèce

# Macroevolution: evolution above the species level

Macroevolution distinguished from microevolution, which refers to evolutionary change within a species or population.



[Yuri Filipchenko \(1927\)](#)

Large evolutionary transitions cannot be explained by Darwinian evolution

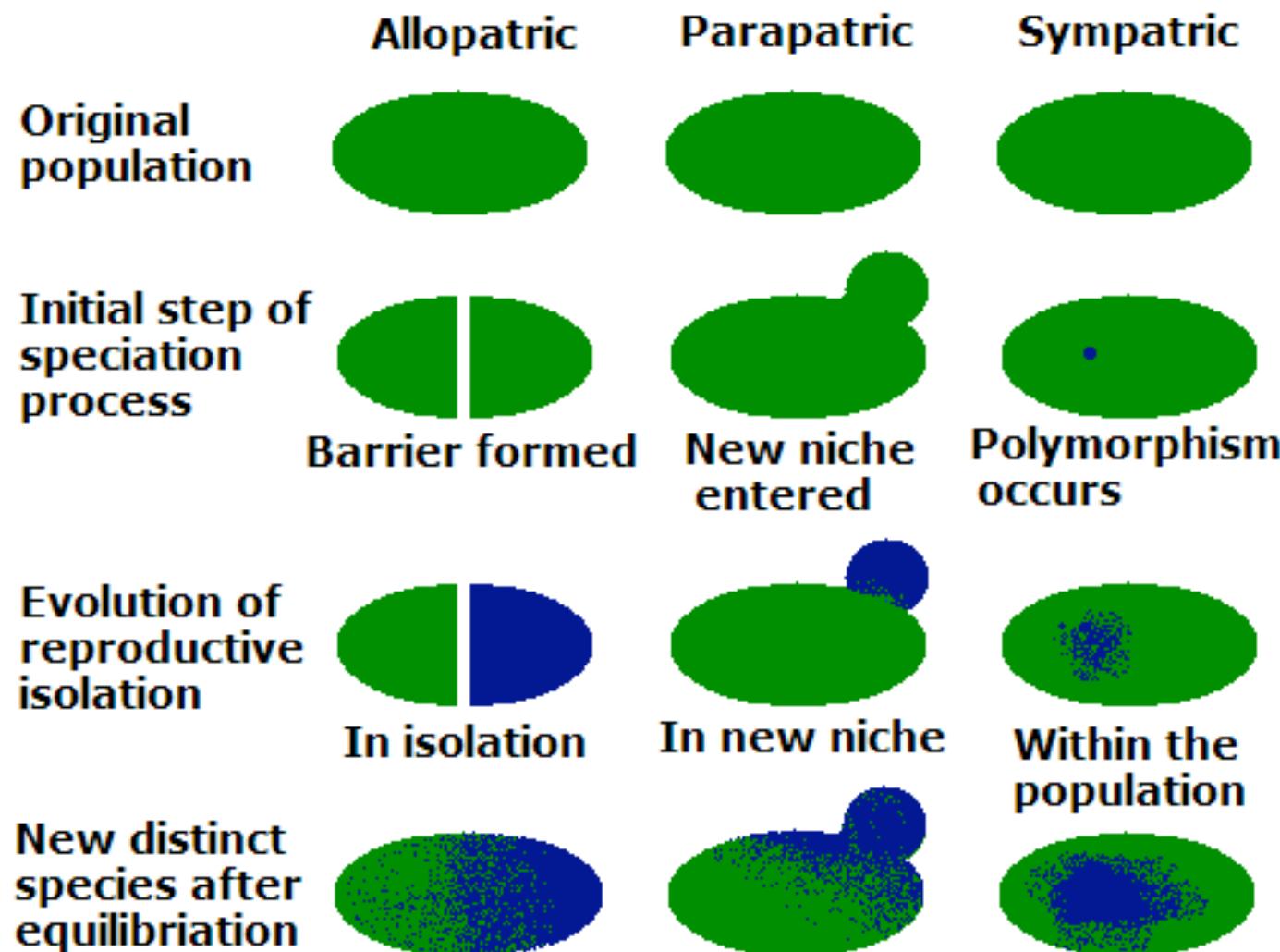
# Macroevolution as the sum of microevolutionary changes over geological times?



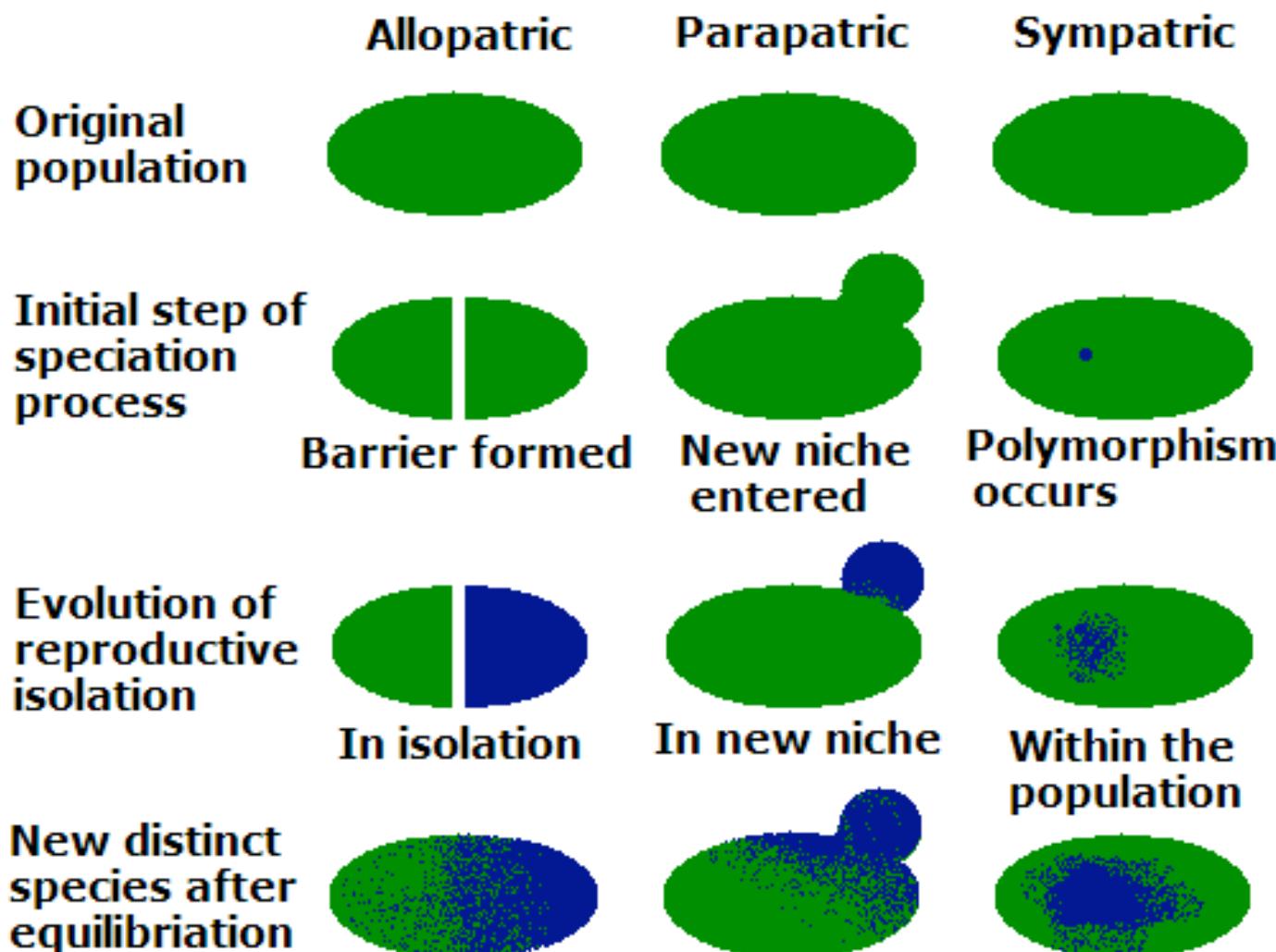
Theodosius Dobzhansky (1937)

**What are the microevolutionary processes that modulate speciation and extinction rates?**

# The speciation process



# Do we see a correlation between speciation rates (estimated from phylogenies) and intraspecific measures of differentiation?



# Mixed support for an association between speciation rates and population geographic structure, genetic differentiation, or evolution of reproductive isolation



Macroevolutionary speciation rates are decoupled from the evolution of intrinsic reproductive isolation in *Drosophila* and birds

Daniel L. Rabosky<sup>a,1</sup> and Daniel R. Matute<sup>b</sup>

updates

Positive association between population genetic differentiation and speciation rates in New World birds

Michael G. Harvey<sup>a,b,c,d,1</sup>, Glenn F. Seeholzer<sup>a,b</sup>, Brian Tilston Smith<sup>a,b,e</sup>, Daniel L. Rabosky<sup>c,d</sup>, Andrés M. Cuervo<sup>a,b,f</sup>, and Robb T. Brumfield<sup>a,b</sup>

AS

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No link between population isolation and speciation rate in squamate reptiles

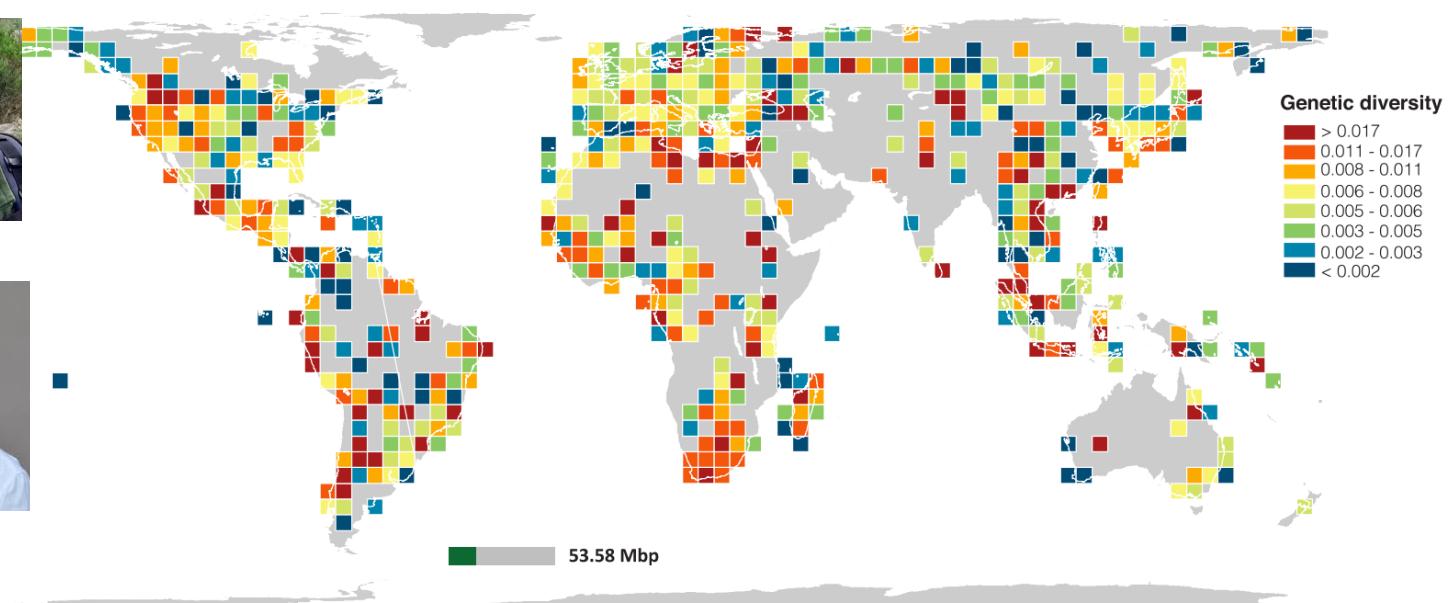
Sonal Singhal<sup>a,1</sup>, Guarino R. Colli<sup>b</sup>, Maggie R. Grundler<sup>c,d</sup>, Gabriel C. Costa<sup>e</sup>, Ivan Prates<sup>f,g</sup>, and Daniel L. Rabosky<sup>f,g,1</sup>

# Illustration: test of the link between genetic diversity and speciation rates in mammals



Genetic diversity: level of polymorphism of DNA sequences among individuals within a species

Genetic diversity has major implications for the evolution and conservation of species



# Genetic diversity: level of polymorphism of DNA sequences among individuals within a species

Watterson's theta

nombre de sites polymorphes

$$\widehat{\theta}_w = \frac{K}{a_n}, \quad a_n = \sum_{i=1}^{n-1} \frac{1}{i}$$

Tajima's theta

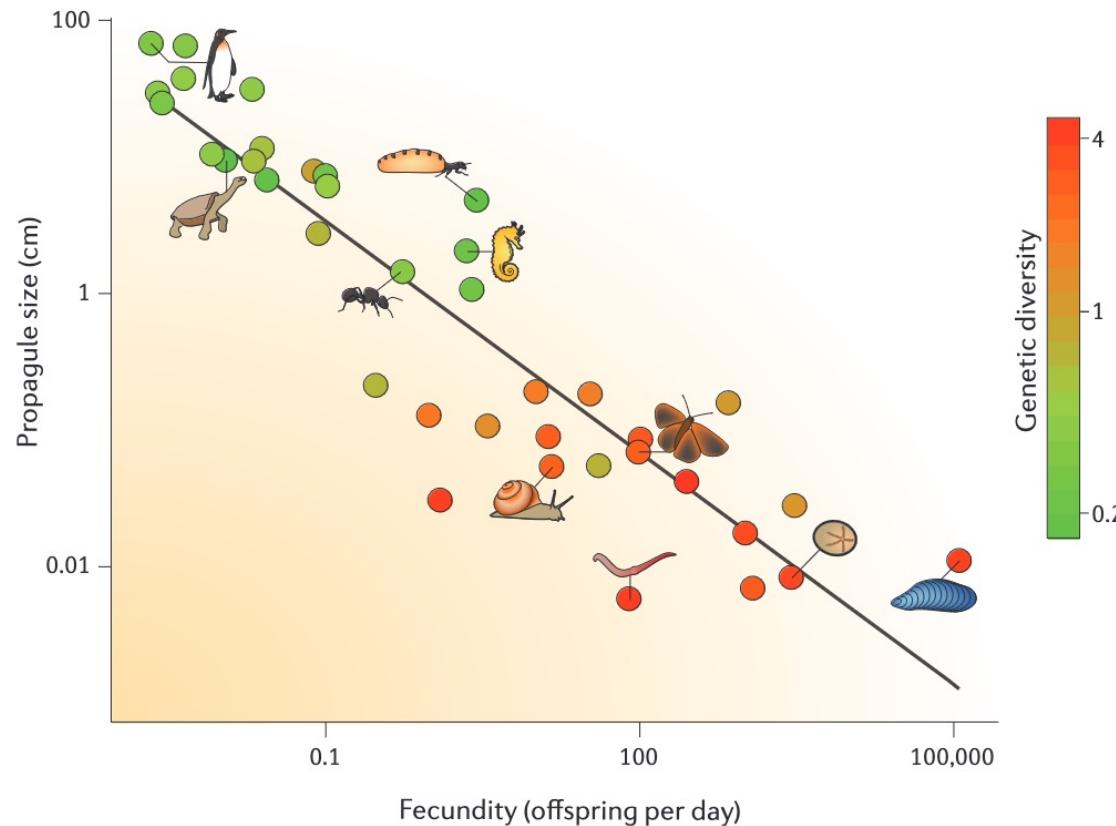
nombre de polymorphismes entre les séquences i et j

$$\widehat{k} = \frac{\sum \sum_{i < j} k_{ij}}{\binom{n}{2}}.$$

Under the Wright-Fisher model, these metrics are estimators of the expected number of polymorphisms between two DNA sequences

$$\vartheta = N_e \mu$$

# Studies on the correlates of genetic diversity have focused on life history traits



# Which correlation could we expect between genetic diversity and speciation rate?

**Genetic diversity**

$$\vartheta = N_e \mu$$

**Speciation rate**

Larger in species with:

Large population sizes

more likely hit by geographic barriers



High mutation rates



Geographic structure (depends on the details of migration process)



Favors:

Divergent selection if limited by the availability of polymorphic alleles



Favors:



Competition-mediated divergent selection

# Which correlation could we expect between genetic diversity and speciation rate?

Genetic diversity

$$\vartheta = N_e \mu$$

Speciation rate

Generates:  
Bottlenecks

Smaller in species with:

Small population sizes

faster accumulation of  
slightly deleterious  
mutations



Divergent selection



Geographic structure (depends on  
the details of migration process)



# Estimating intraspecific genetic diversity across mammals

GenBank

"Mammalia"[Organism] AND CYTB NOT "Homo sapiens"[Organism]

124,289 sequences of mammals Cytochrome b

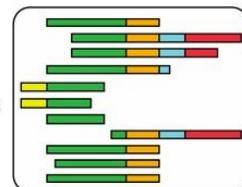
Split into 138 families for better alignments

SuperCRUNCH  
For Phylogenetic Data

Portik and Wiens  
(2019) MEE 2020

Reference\_Blast\_Extract.py

Input Sequences

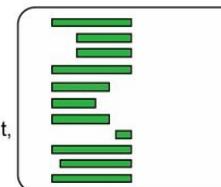


Step 2:  
BLAST to  
reference set  
(BLASTn)

Step 1:  
Create reference from user file  
(makeblastdb)

User-supplied  
reference set

Step 3:  
Process BLAST output,  
merge coordinates,  
trim sequences

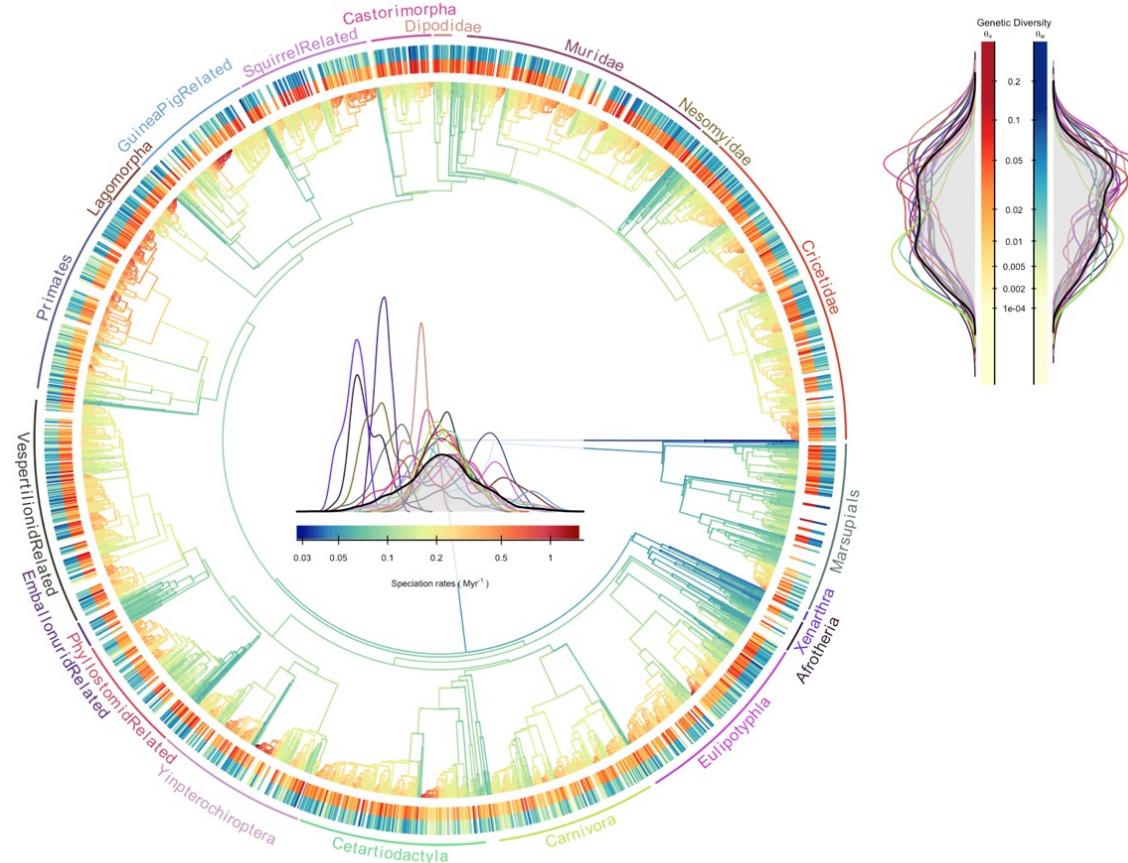


Output Sequences

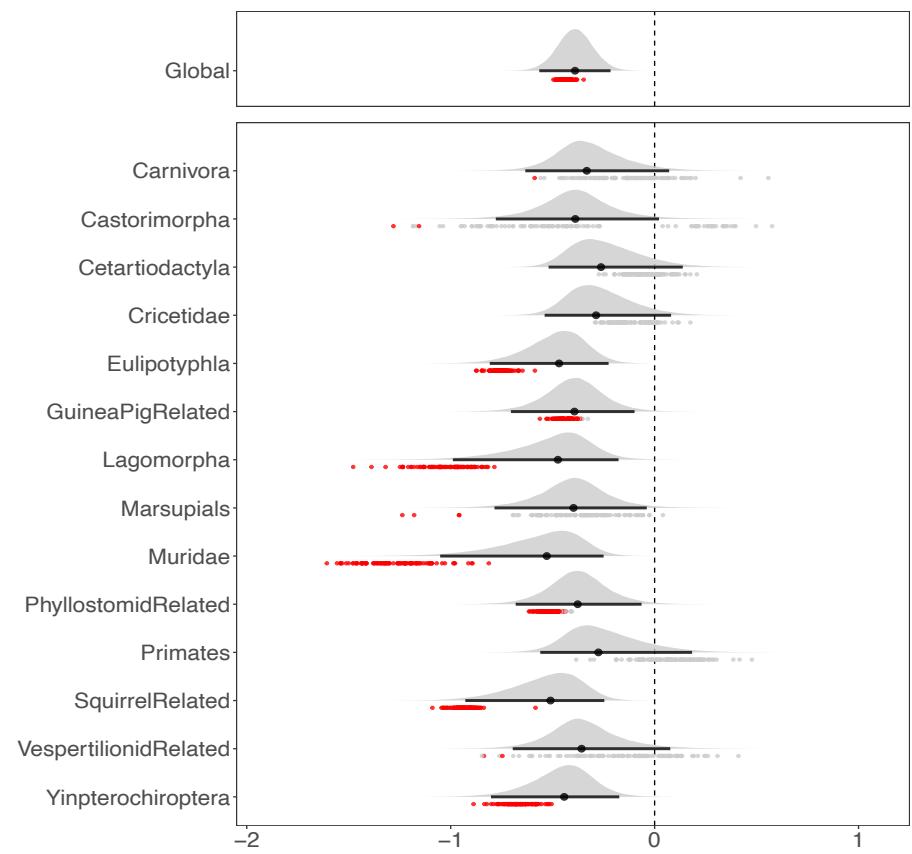
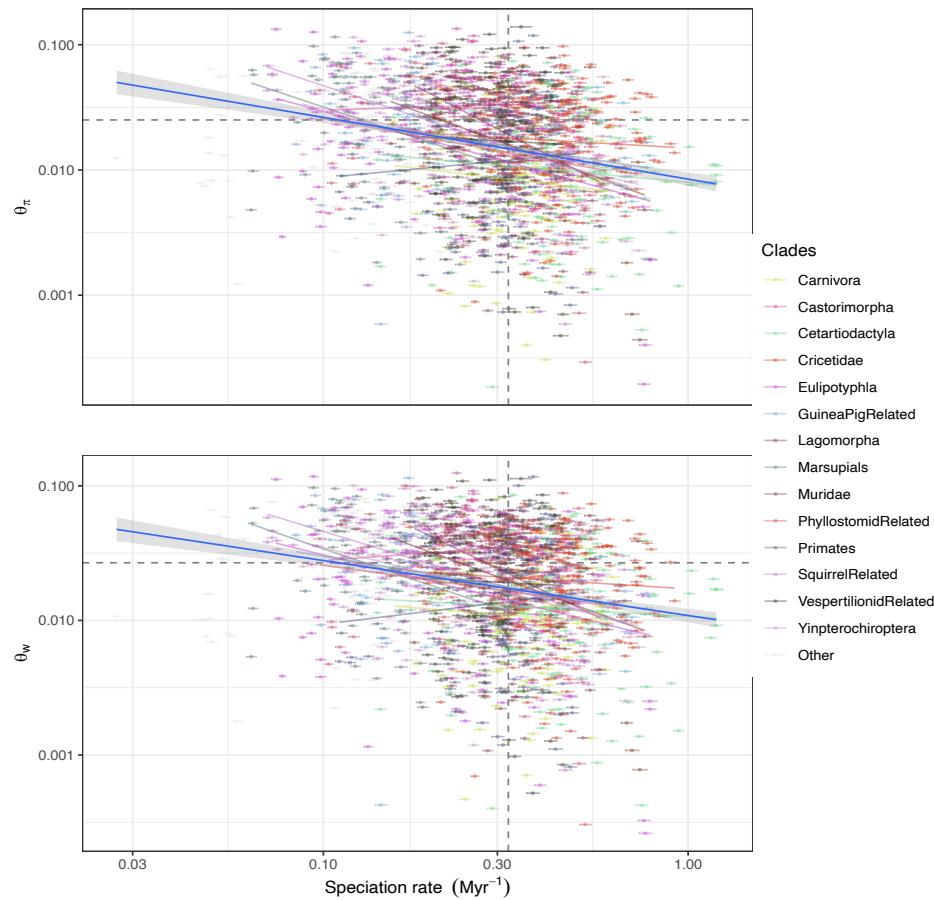
3899 species → 2004 species with at least 5 individuals → genetic diversity

# Estimating branch-specific speciation rates

ClaDS estimates on Upham's PLoS Biology 2019 mammals phylogeny



# Negative correlation between genetic diversity and speciation rates



# The negative correlation between genetic diversity and speciation rates is not linked to an indirect effect of covariates

term	$\theta_T \sim$ Traits			$\lambda \sim$ Traits			$\theta_T \sim \lambda +$ Traits						
	PGLS		BMLM		PGLS		BMLM		PGLS		BMLM		
	Estimate	SE	Estimate	95% CI		Estimate	SE	Estimate	95% CI		Estimate	95% CI	
$\lambda$										<b>-0.285</b>	0.078	<b>-0.273</b>	[-0.448; -0.078]
Mean latitude	<b>-0.113</b>	0.029	<b>-0.100</b>	[-0.174; -0.023]	-0.002	0.006	0.005	[-0.013; 0.023]	-0.104	0.029	<b>-0.096</b>	[-0.173; -0.018]	
Mean temperature	<b>0.226</b>	0.097	<b>0.218</b>	[0.005; 0.419]	-0.022	0.018	-0.020	[-0.055; 0.017]	<b>0.212</b>	0.096	<b>0.196</b>	[0.011; 0.392]	
Body Mass	<b>-0.129</b>	0.026	<b>-0.123</b>	[-0.189; -0.058]	0.004	0.009	0.011	[-0.01; 0.032]	<b>-0.124</b>	0.025	<b>-0.118</b>	[-0.182; -0.055]	
Generation length	-0.052	0.106	-0.105	[-0.353; 0.149]	-0.009	0.028	0.010	[-0.05; 0.074]	-0.068	0.103	-0.104	[-0.34; 0.136]	
Litter size	<b>-0.254</b>	0.093	<b>-0.370</b>	[-0.594; -0.15]	<b>0.055</b>	0.027	0.049	[-0.015; 0.111]	<b>-0.238</b>	0.091	<b>-0.359</b>	[-0.592; -0.125]	

# Which correlation could we expect between genetic diversity and speciation rate?

Genetic diversity

$$\vartheta = N_e \mu$$

Speciation rate

Generates:  
Bottlenecks

Smaller in species with:

Small population sizes

faster accumulation of  
slightly deleterious  
mutations



Divergent selection

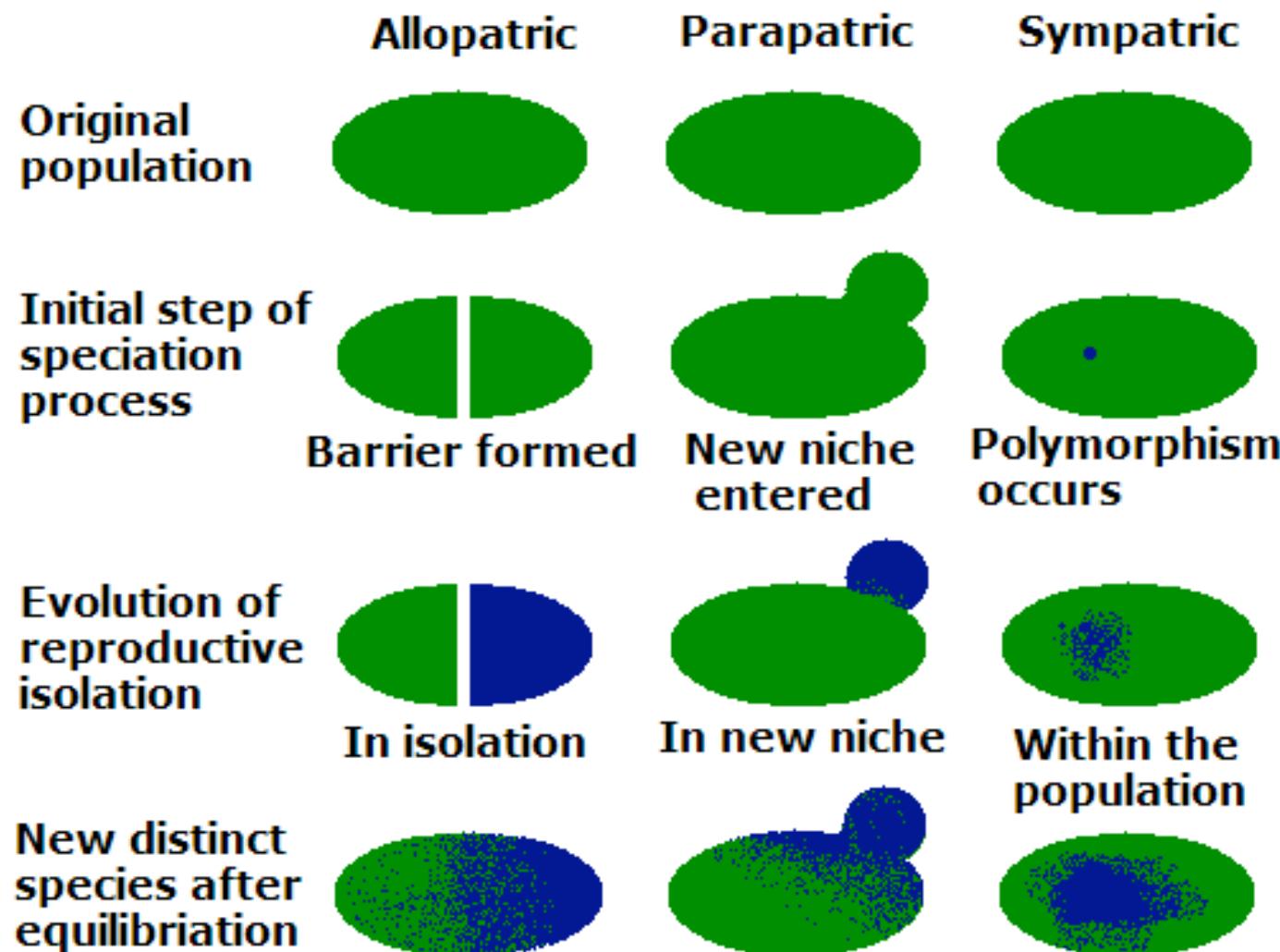


Geographic structure (depends on  
the details of migration process)



**What are the microevolutionary processes that modulate speciation rates?**

# The speciation process



# Which correlation between intraspecific measures of differentiation and speciation rates?



Macroevolutionary speciation rates are decoupled from the evolution of intrinsic reproductive isolation in *Drosophila* and birds

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Positive association between population genetic differentiation and speciation rates in New World birds

Michael G. Harvey<sup>a,b,c,d,1</sup>, Glenn F. Seeholzer<sup>a,b</sup>, Brian Tilston Smith<sup>a,b,e</sup>, Daniel L. Rabosky<sup>c,d</sup>, Andrés M. Cuervo<sup>a,b,f</sup>, and Robb T. Brumfield<sup>a,b</sup>

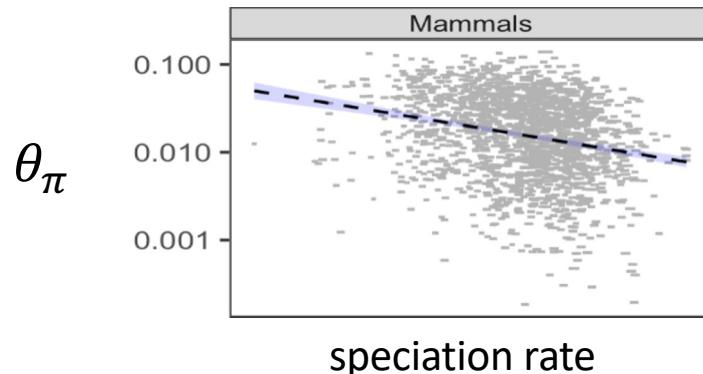
updates

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No link between population isolation and speciation rate in squamate reptiles

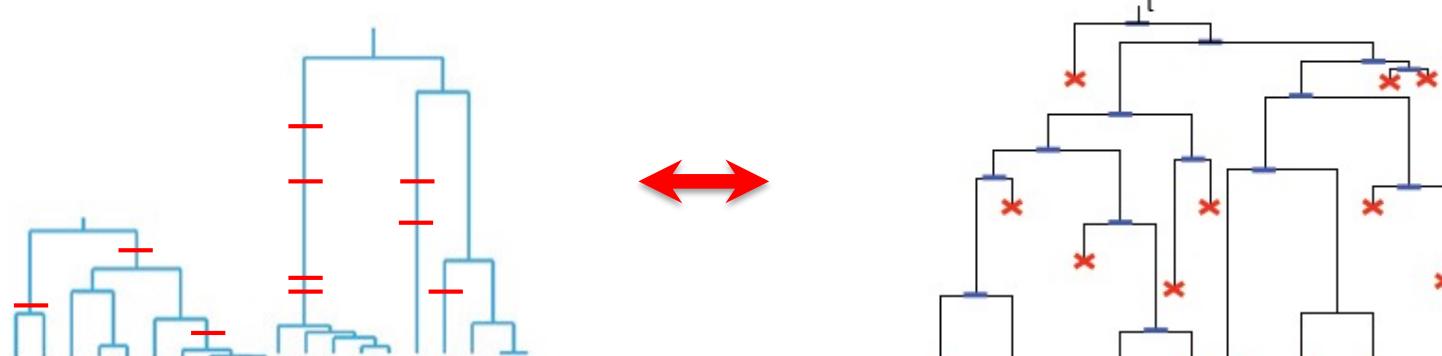
Sonal Singhal<sup>a,1</sup>, Guarino R. Colli<sup>b</sup>, Maggie R. Grundler<sup>c,d</sup>, Gabriel C. Costa<sup>e</sup>, Ivan Prates<sup>f,g</sup>, and Daniel L. Rabosky<sup>f,g,1</sup>

# Which correlation between intraspecific measures of differentiation and speciation rates?



Silva et al. (under revision for *Nature Comm*)

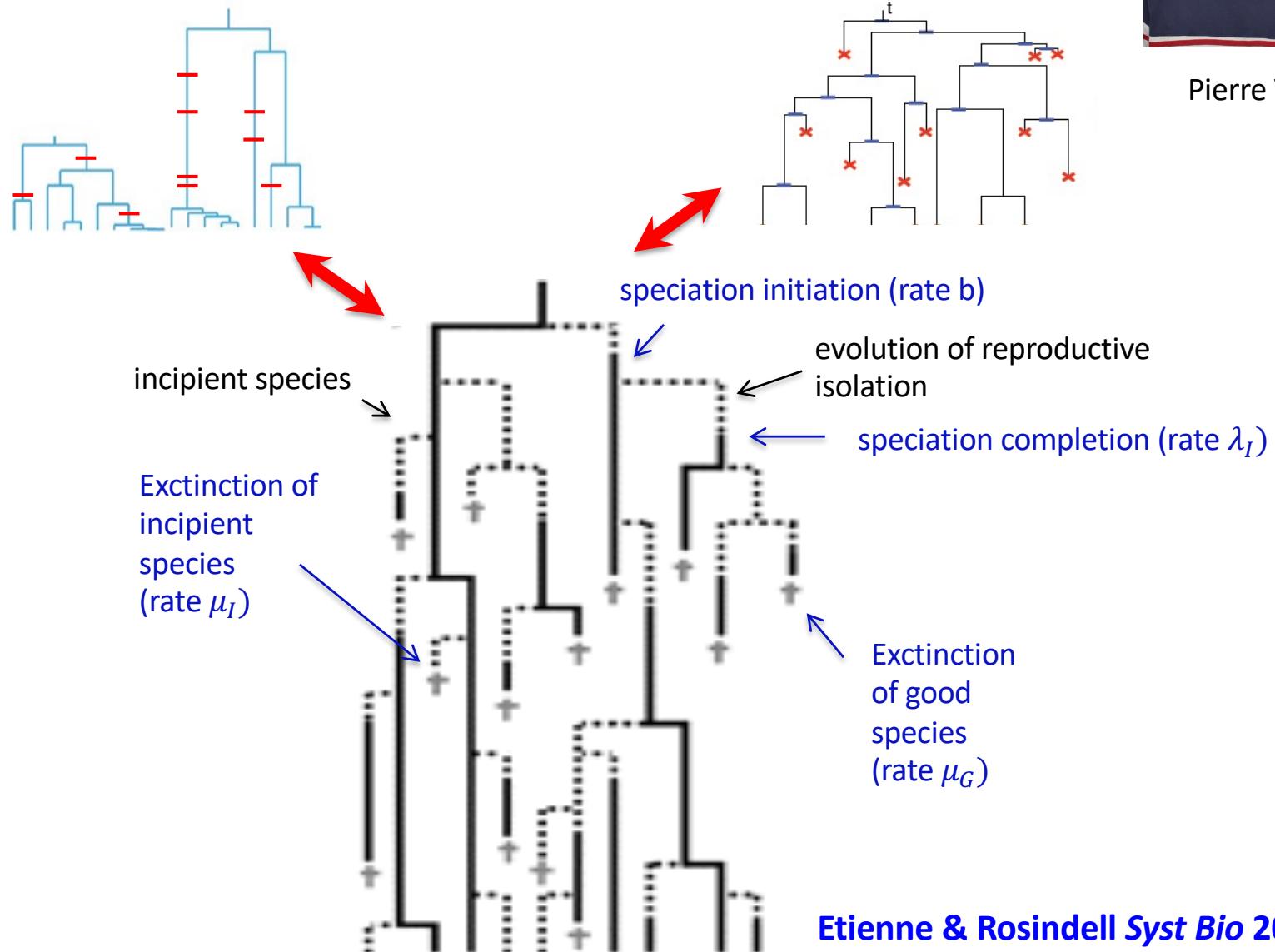
Need to go from verbal to quantitative predictions



# The protracted birth-death model as a way to bridge micro and macroevolutionary speciation research



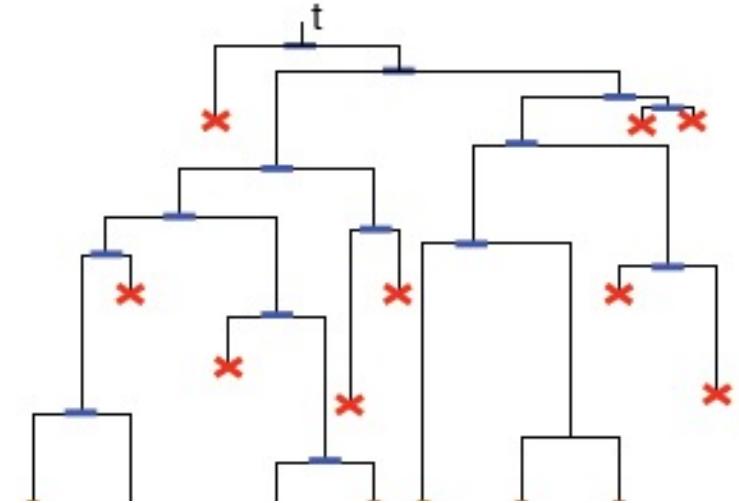
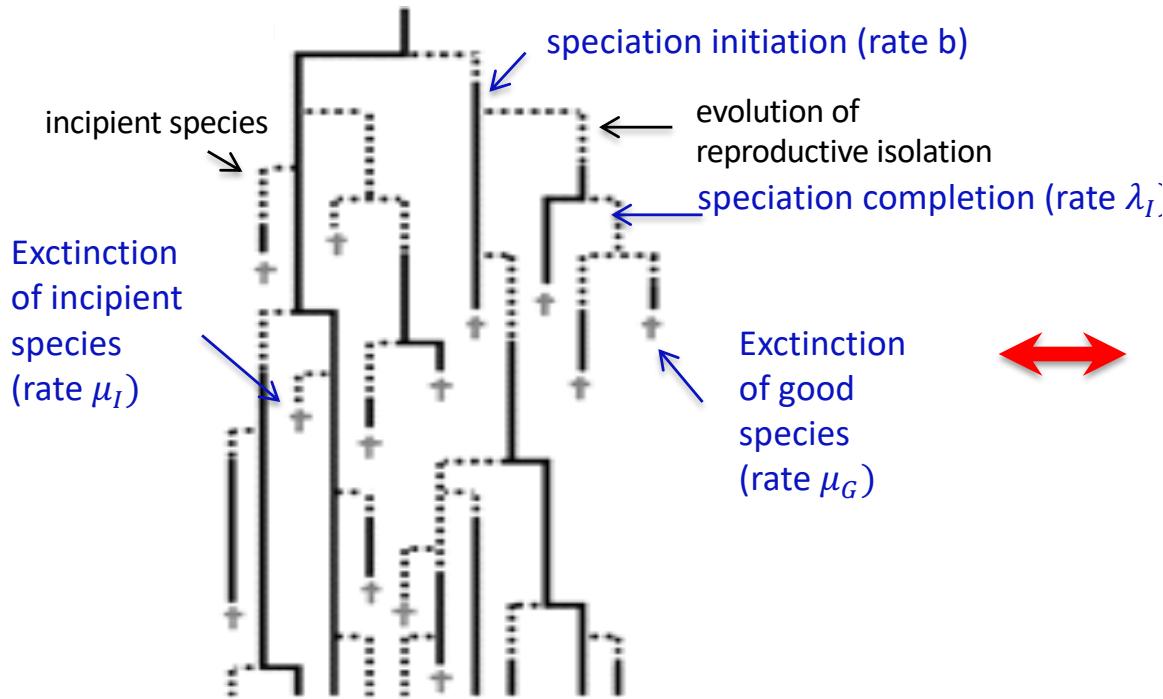
Pierre Véron



# Linking the protracted birth-death model and the birth-death model



Pierre Véron



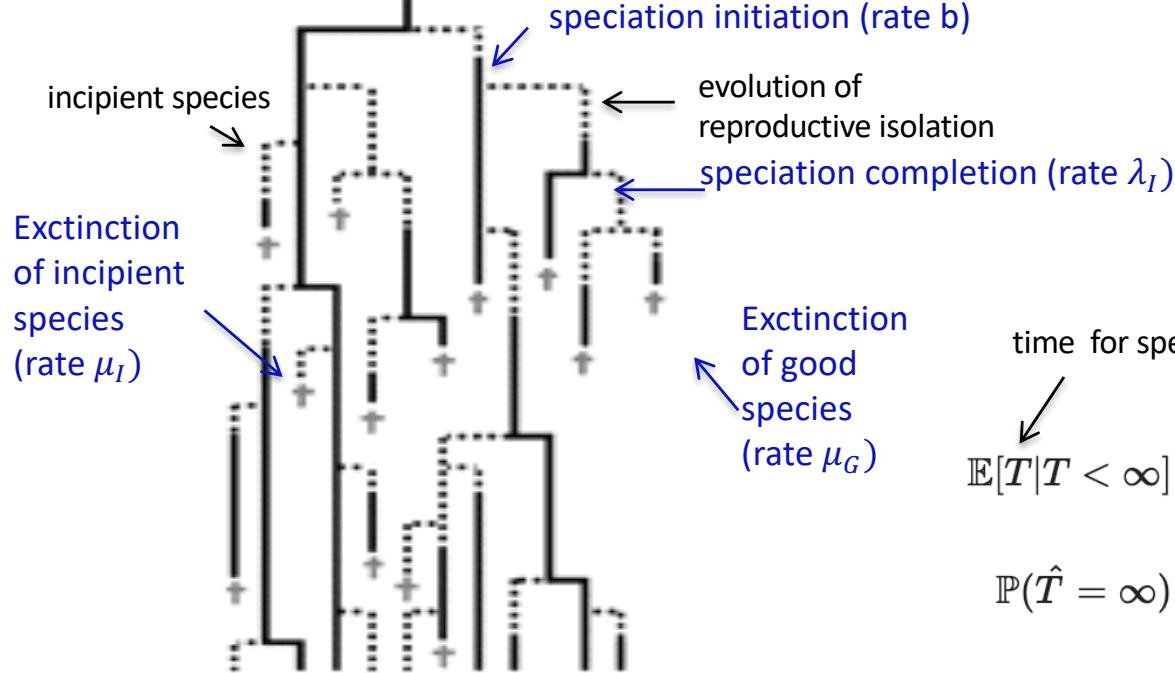
Etienne & Rosindell *Syst Bio* 2012

What are the 'speciation' ( $\hat{\lambda}$ ) and 'extinction' ( $\hat{\mu}$ ) rates that have the same expected time to speciation than under the PBD model with speciation initiation rate  $b$ , speciation completion rate ( $\lambda_I$ ) and extinction rates of the ancestral ( $\mu_G$ ) and incipient species ( $\mu_I$ )?

# 'Speciation' and 'extinction' rates under the protracted birth-death model



Pierre Véron



time for speciation

$$\mathbb{E}[T|T < \infty] = \frac{1}{\hat{\lambda} + \hat{\mu}} = \frac{bp + \lambda_I + \mu_I + 2\mu_G}{(bp + \mu_G)(\lambda_I + \mu_I + \mu_G)} \quad \text{and}$$

$$\mathbb{P}(\hat{T} = \infty) = \frac{\hat{\mu}}{\hat{\lambda} + \hat{\mu}} = \frac{\mu_G}{\mu_G + bp} \left( 1 + \frac{pb}{\lambda_I + \mu_I + \mu_G} \right).$$

$$\hat{\mu} = \mu_G \left( 1 - \frac{\mu_G}{bp + \lambda_I + \mu_I + 2\mu_G} \right)$$

$$\hat{\lambda} = bp \frac{\lambda_I + \mu_I}{bp + \lambda_I + \mu_I + 2\mu_G}.$$

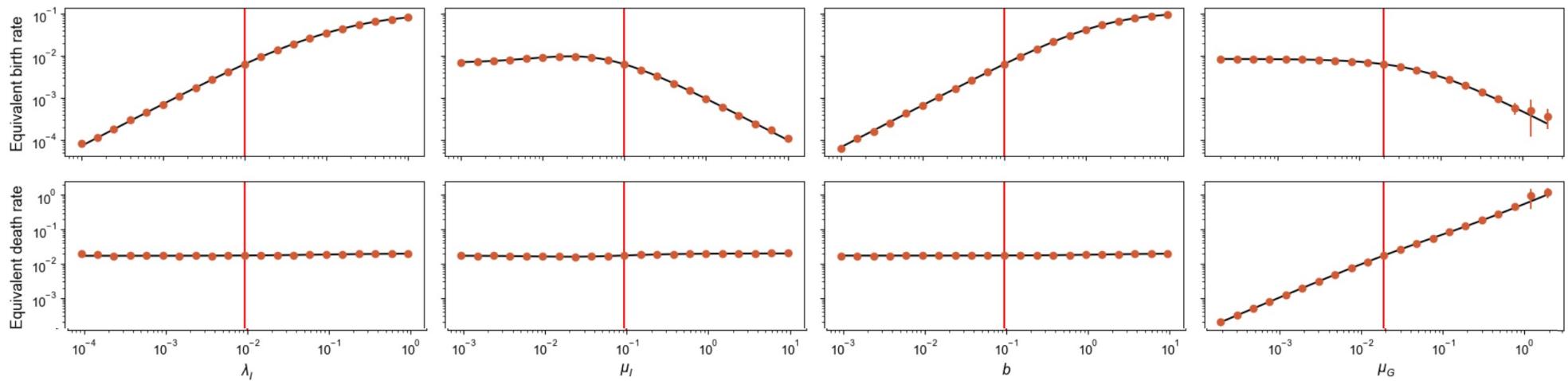
Etienne & Rosindell *Syst Bio* 2012

**The ‘speciation’ rate** is directly related to the rates of speciation initiation and completion; it decreases with increasing rates of extinction (for incipient and good species), but only when they are high compared with the rates of speciation initiation and completion



Pierre Véron

**The ‘extinction’ rate** is directly related to the rate of extinction of good species)



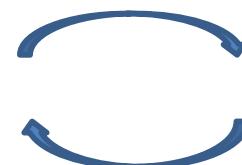
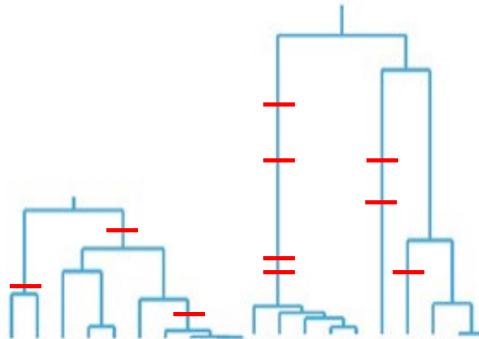
# Linking demographic and genetic processes to the protracted birth-death model



Pierre Véron

Demographic process

Population genetics



# Conclusions

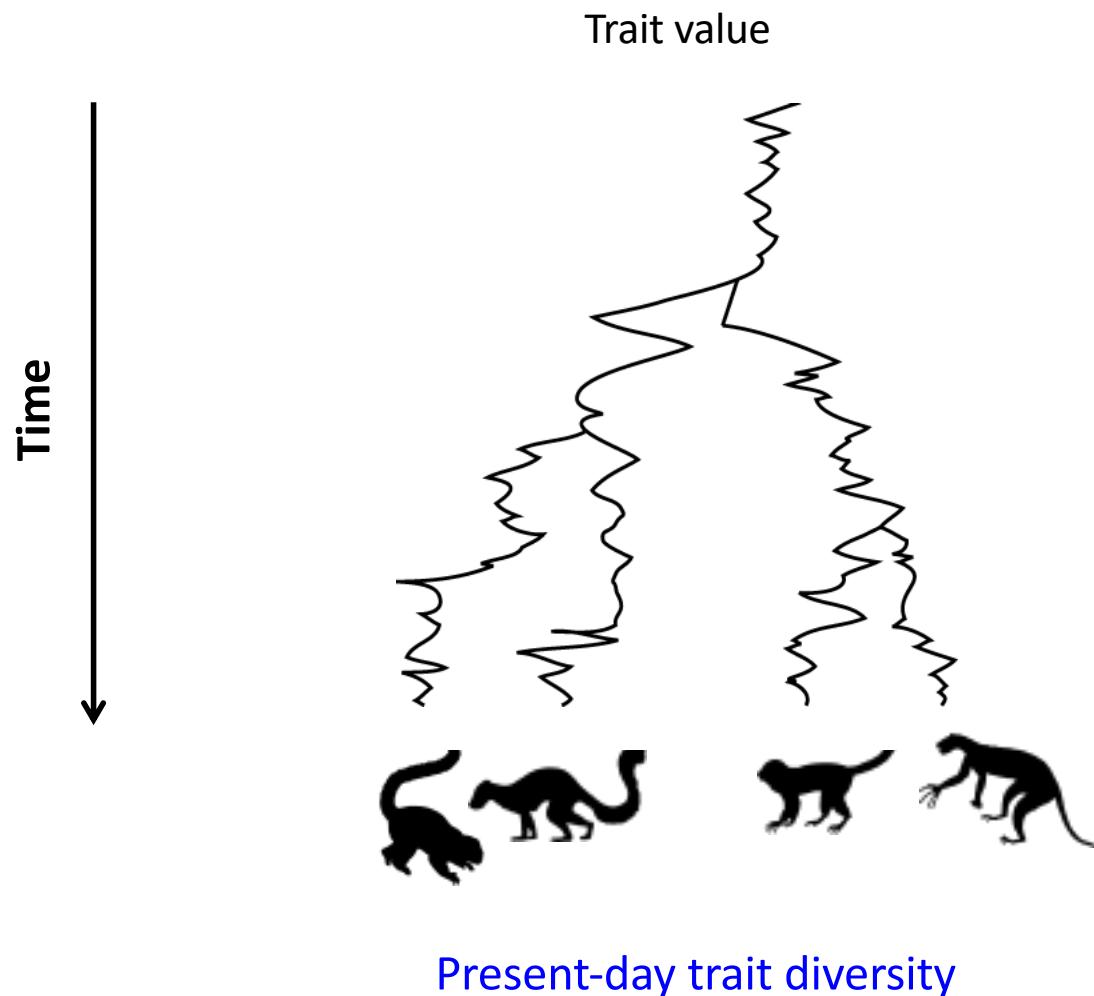
Speciation and extinction rates vary widely across lineages, explaining why some species groups are much more species rich than others

Differences in speciation and extinction rates can be linked to species specific traits as well as abiotic and biotic factors

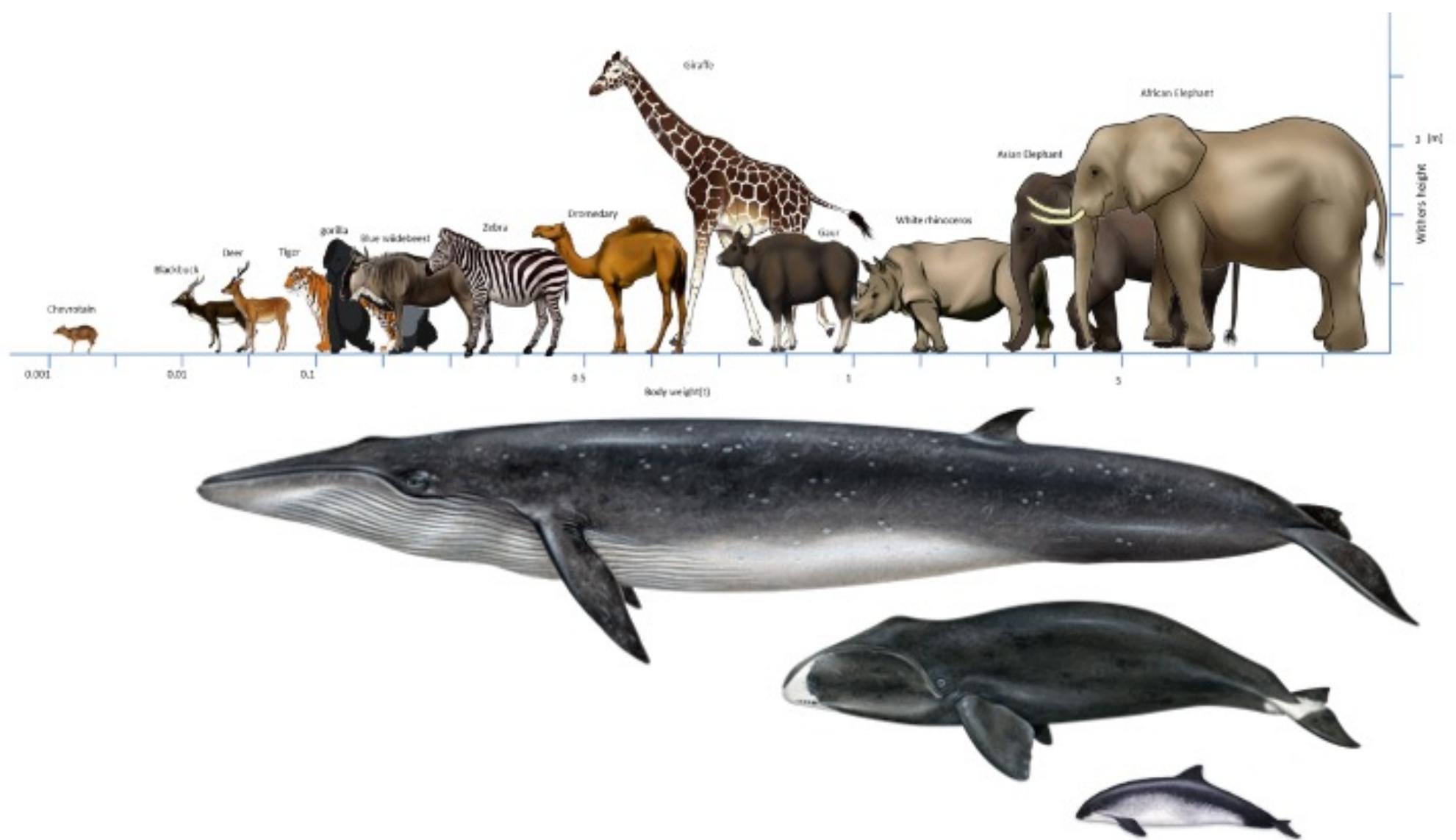
We have well-developed models to assess the effect of species-specific traits and abiotic factors on speciation and extinction rates

Understanding which microevolutionary processes act a rate-limiting step in speciation (and therefore drive present day species richness patterns) remains a major research frontier

# Application des modèles de diffusion à l'étude phylogénétique de l'évolution des phénotypes



# La diversité phénotypique

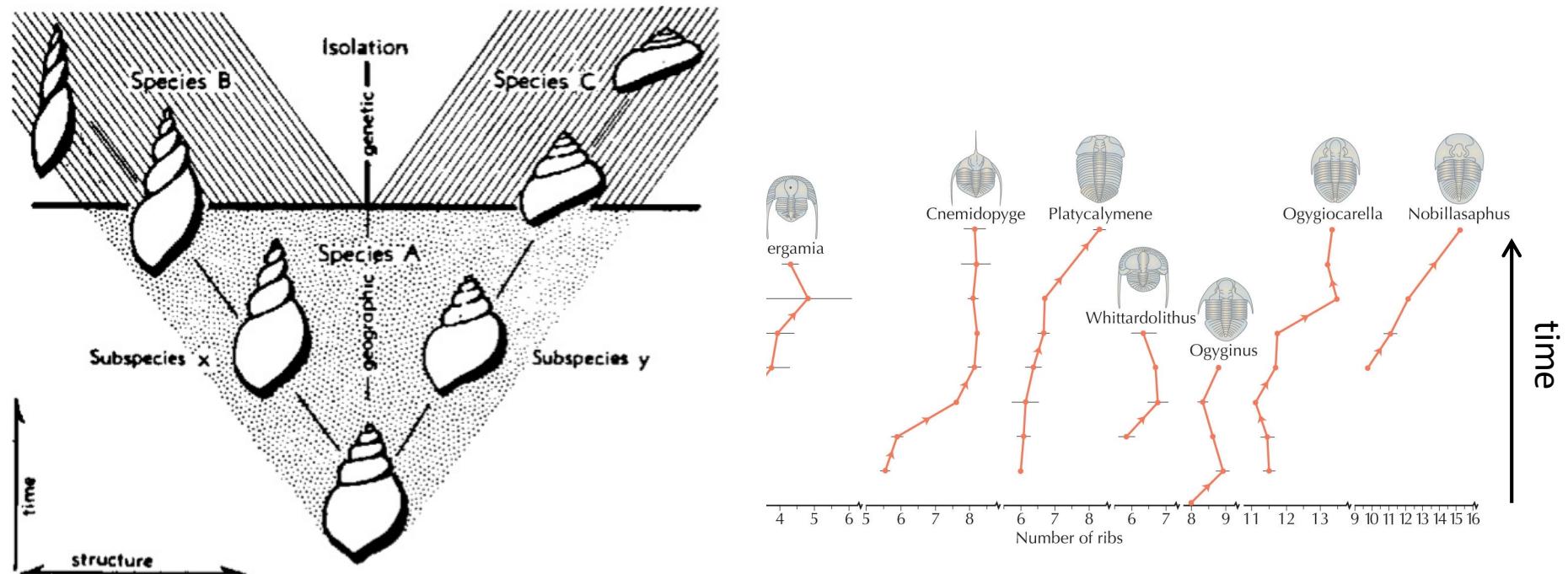


# La diversité phénotypique



# The mode and tempo of phenotypic evolution over geological time scales through the lens of fossil data

## Phyletic gradualism



Moore et al. 1952

Sheldon *Nature* 1987

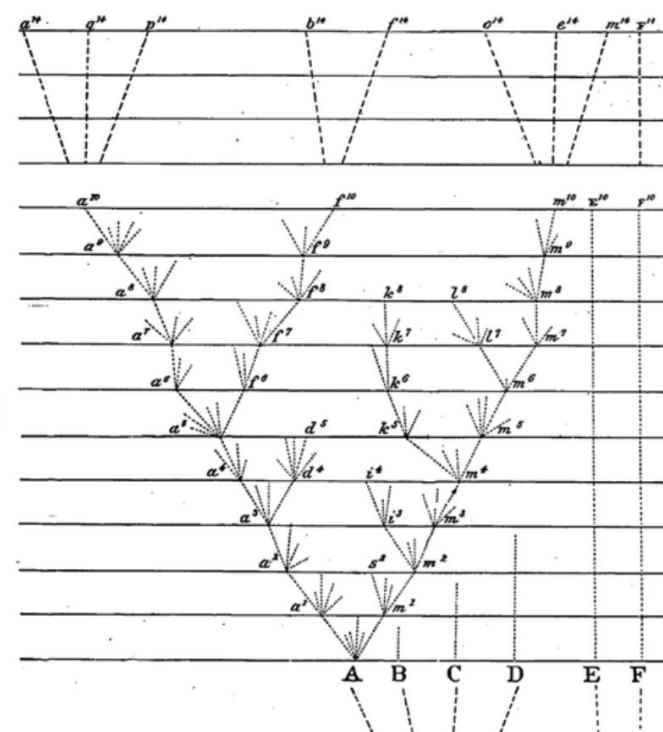
# **Phyletic gradualism and “gaps” in the fossil record**

*« Why do we not find the infinitely numerous transitional links that would illustrate the slow and steady operation of natural selection? Why is not every geological formation and every stratum full of such intermediate links? Geology assuredly does not reveal any such finely graduated organic chain; and this, perhaps, is the gravest objection which can be urged against my theory »*

*« The geological record is extremely imperfect and this fact will to a large extent explain why we do not find interminable varieties, connecting together all the extinct and existing forms of life by the finest graduated steps »*

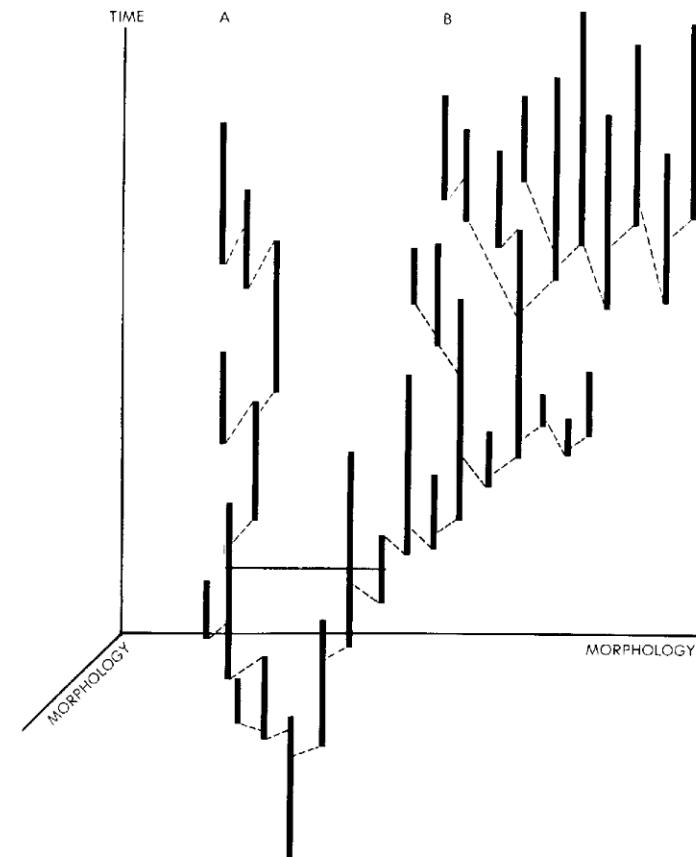
# Punctuated equilibria: an alternative to phyletic gradualism

Gradual changes

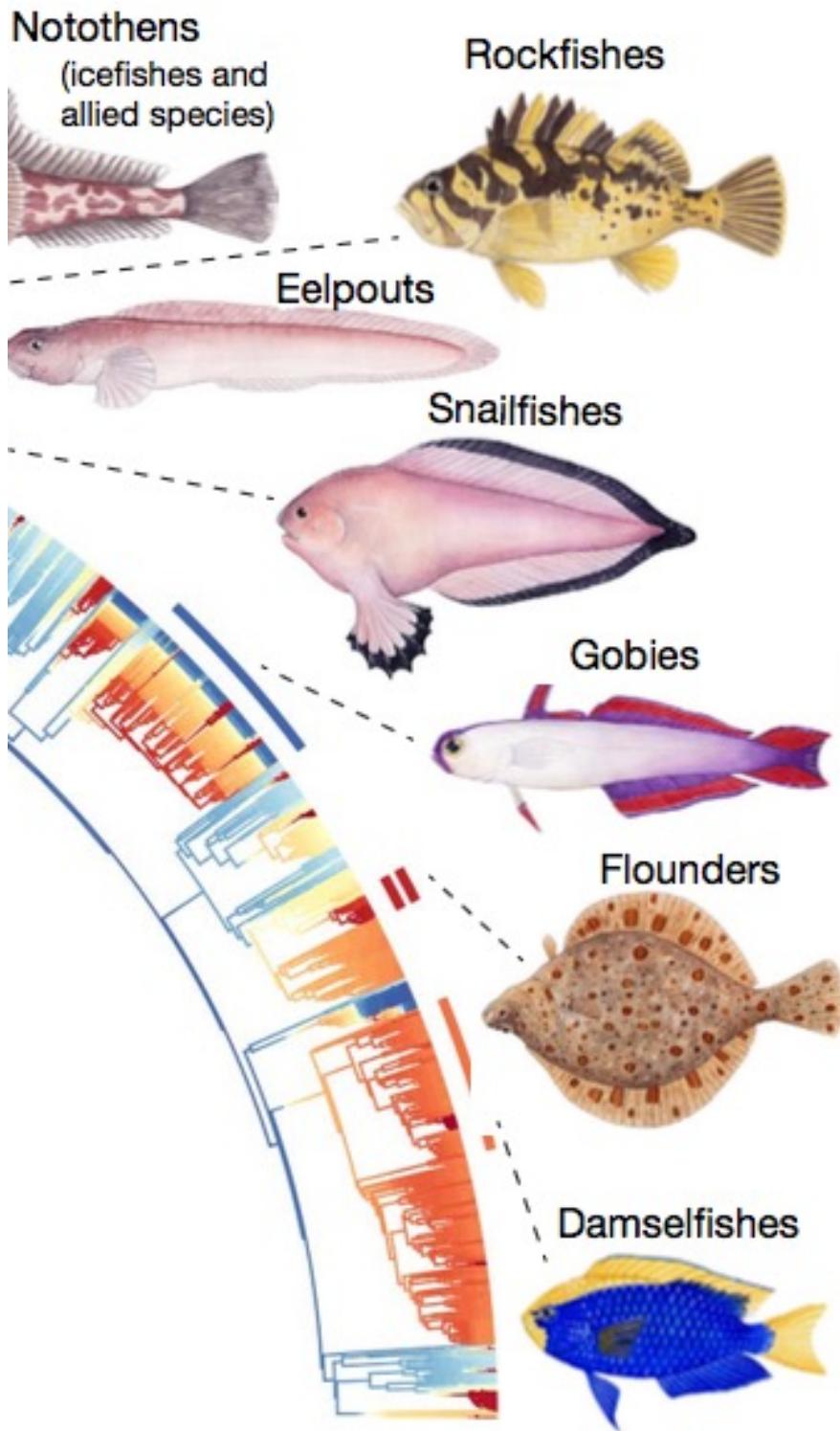


Darwin 1859

Periods of stases separated by periods  
of fast evolutionary change



Eldredge & Gould 1972



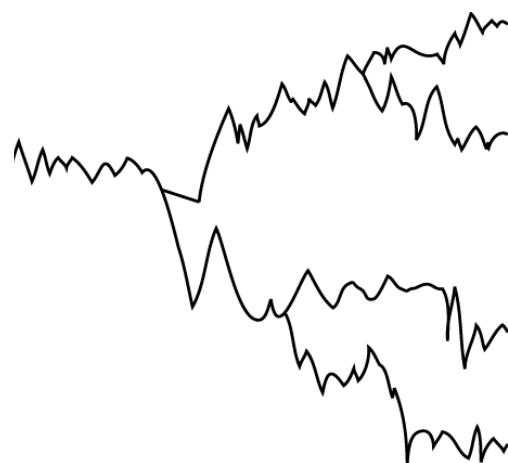
**L'évolution phénotypique peut être étudiée à partir des traits des espèces actuelles et d'une phylogénie datée de ces espèces**

Ici l'arbre phylogénétique est fixé, il n'est pas modélisé

# BUT

Développer des **modèles d'évolution phénotypique** ET des approches d'**inférence statistique** qui permettent d'ajuster les modèles à des **données phénotypiques actuelles** de façon à **étudier les modes et vitesse d'évolution des phénotypes**

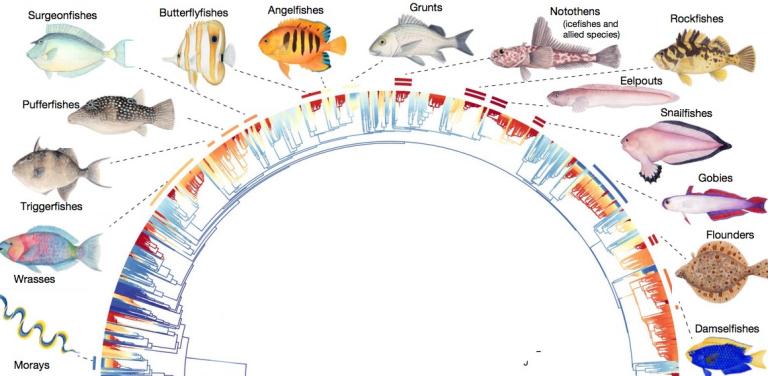
Modèle d'évolution  
phénotypique



Inférence  
Statistique



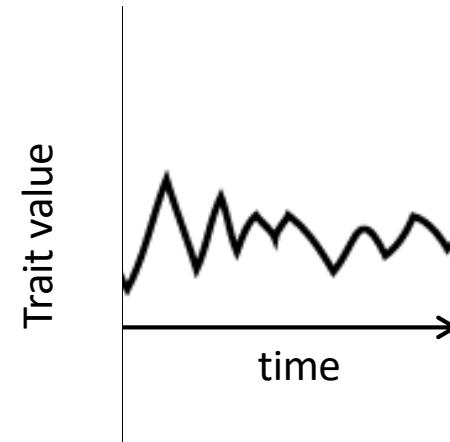
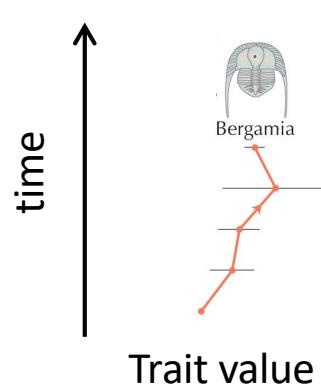
Données phénotypiques  
actuelles



Mode et vitesse d'évolution  
des phénotypes

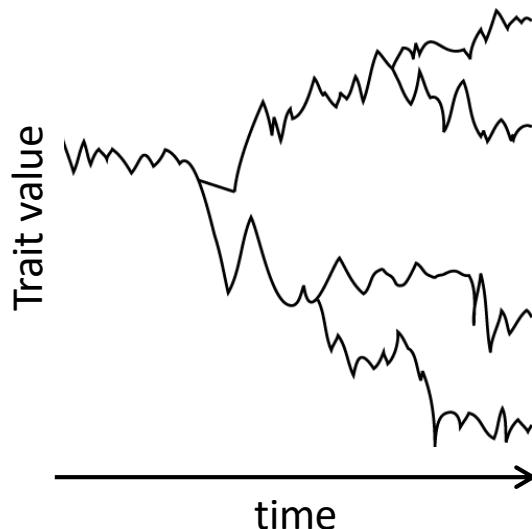
# Le mouvement Brownien pour étudier l'évolution phénotypique

Evolution phénotypique pendant la vie d'une espèce



$$dX(t) = \sigma dB(t)$$

Evolution phénotypique pendant la diversification d'un groupe d'espèces

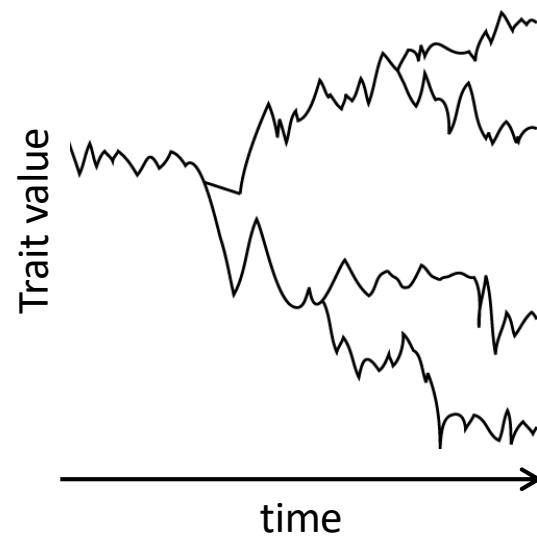


- Mouvement Brownien le long d'une lignée
- Evolution indépendante après la spéciation

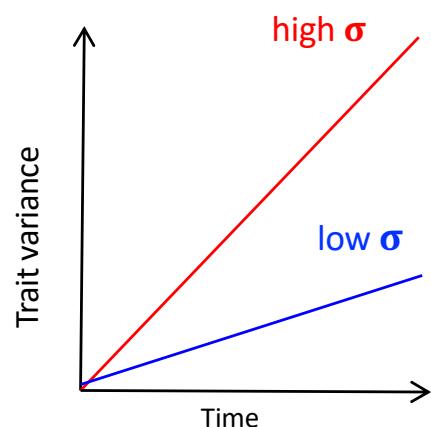


Ici une lignée est une espèce

# Le mouvement Brownien pour étudier l'évolution phénotypique



- Mouvement Brownien le long d'une lignée
- Evolution indépendante après la spéciation



La variance phénotypique entre espèces augmente linéairement avec le temps depuis leur divergence

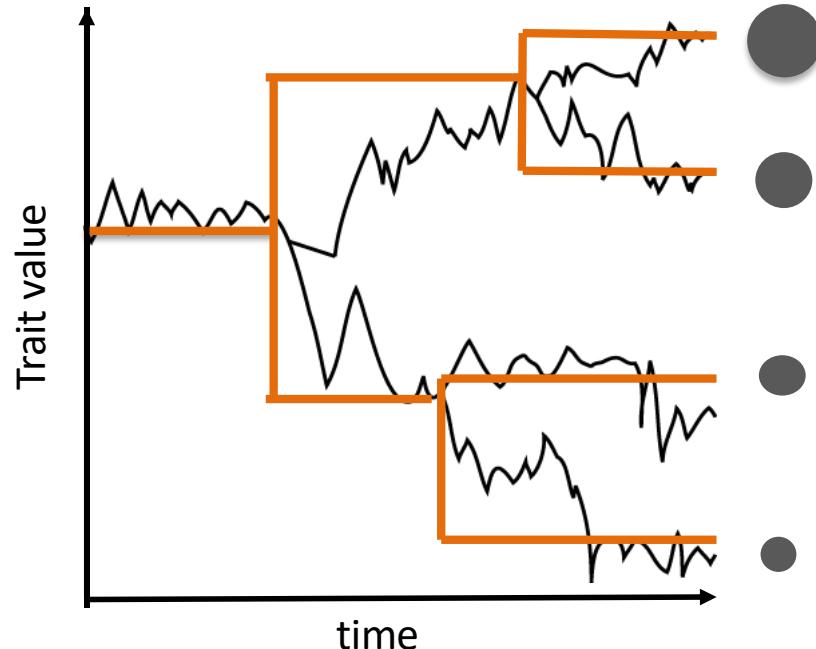
$$V = \sigma^2 t$$

$\sigma$  comme mesure de la vitesse d'évolution phénotypique

# Likelihood associated to the Brownian process

Let  $X$  be a quantitative trait assumed to evolve as a Brownian process with rate  $\sigma$  on a fixed, ultrametric, bifurcating species tree with branch lengths in unit of time, assumed to be known.

$$dX(t) = \sigma dB(t)$$



shared evolutionary history  
between species i and j

expected variance-  
covariance  
matrix

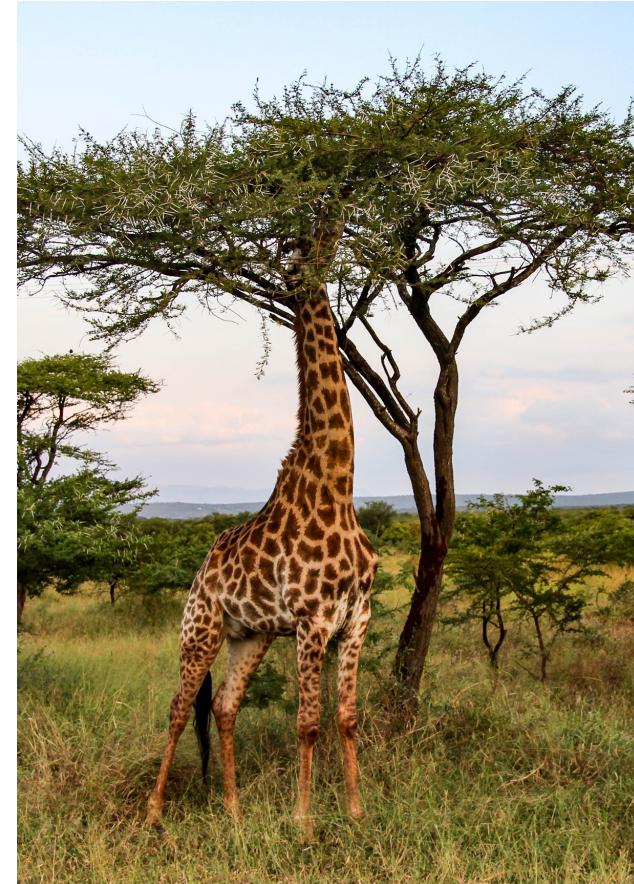
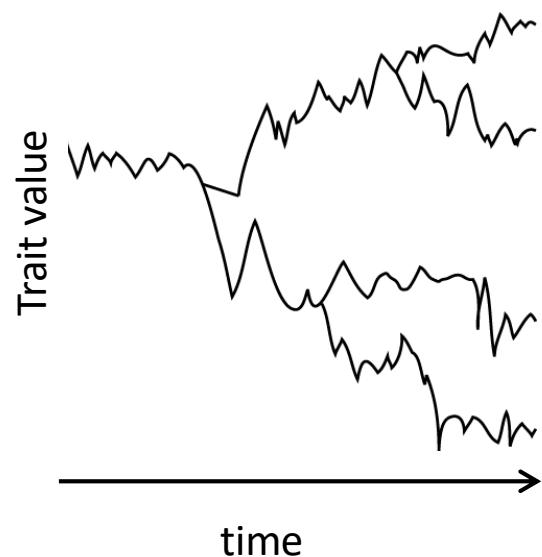
$$V_{ij} = \sigma^2 S_{ij}$$

$$L = \frac{\exp\left\{-\frac{1}{2} [\mathbf{X} - \mathbf{E}(\mathbf{X})]' (\mathbf{V}^{-1}) [\mathbf{X} - \mathbf{E}(\mathbf{X})]\right\}}{\sqrt{(2\pi)^N * \det(\mathbf{V})}}$$

Felsenstein 1973

→  $\sigma$  estimated by maximum likelihood or Bayesian inference

# Les traits évoluent-ils comme un mouvement Brownien?



# Le processus d'Orstein-Uhlenbeck

$$dX(t) = \boxed{\alpha[\theta - X(t)]dt} + \boxed{\sigma dB(t)}$$

where  $\alpha$  = strength of "selection"  
 $\theta$  = adaptive optimum

Selection component      Drift (BM) component

$$L = \frac{\exp\left\{-\frac{1}{2} [\mathbf{X} - \mathbf{E}(\mathbf{X})]' (\mathbf{V}^{-1}) [\mathbf{X} - \mathbf{E}(\mathbf{X})]\right\}}{\sqrt{(2\pi)^N * \det(\mathbf{V})}}$$

expected covariance  
between species i and j

total height of the tree

shared evolutionary history  
between species i and j

$$V_{ij} = \frac{\sigma^2}{2\alpha} e^{-2\alpha(T-s_{ij})} (1 - e^{-2\alpha s_{ij}})$$

# Models of phenotypic evolution with time-dependent rates

$dX(t)$  : change in  $X(t)$  in a small amount of time

The « Early Burst » model: trait evolution is fast in the initial phase of an evolutionary radiation, and slows down later on as an effect of limited ecological opportunity

$$dX(t) = \sigma(t) dB(t) \quad \text{with } \sigma^2(t) = \sigma_0^2 e^{rt} \quad \text{where } r \text{ is the rate of decline}$$

Blomberg *et al.* Am Nat 2003

The « Diversity-dependent » model: trait evolution slows down as species pile up in a clade, therefore reducing ecological opportunity

$$dX(t) = \sigma(t) dB(t) \quad \text{with } \sigma^2(t) = \sigma_0^2 e^{bn(t)} \quad \text{where } n(t) \text{ is the number of lineages in the clade at time } t$$

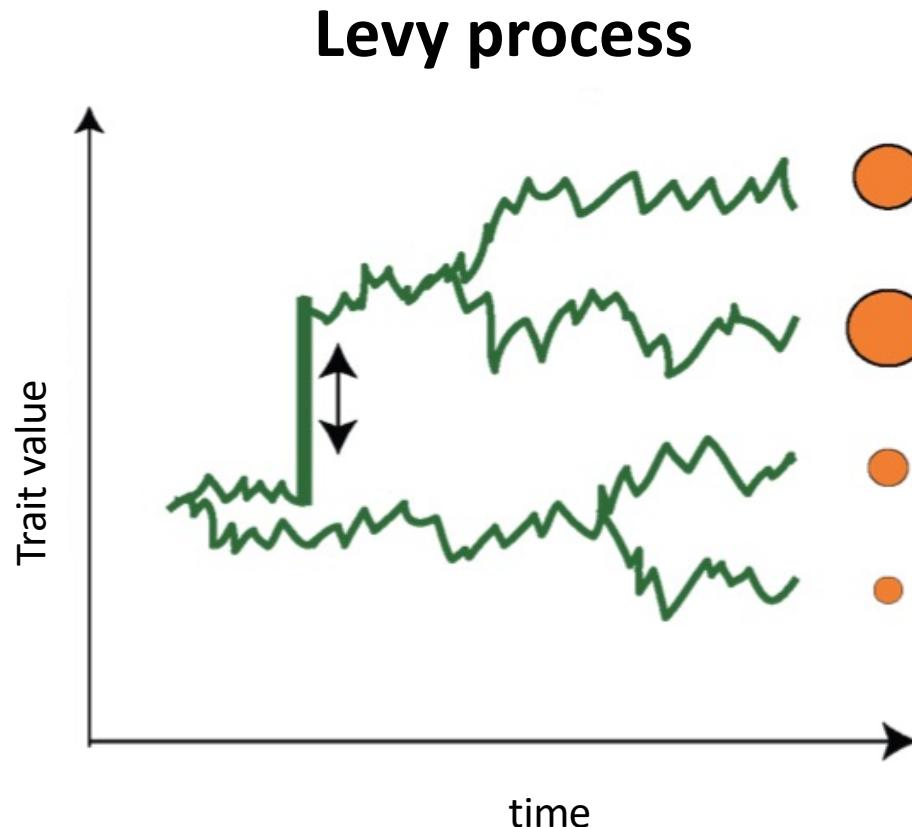
Weir & Mursleen Evolution 2013

The « Environment-dependent » model: the rate of trait evolution depends on past environmental variables

$$dX(t) = \sigma(t) dB(t) \quad \text{with } \sigma^2(t) = f(t, E_1(t), E_2(t), \dots, E_k(t))$$

Clavel & Morlon PNAS 2017

# Models of phenotypic evolution with jumps (punctuated equilibrium)

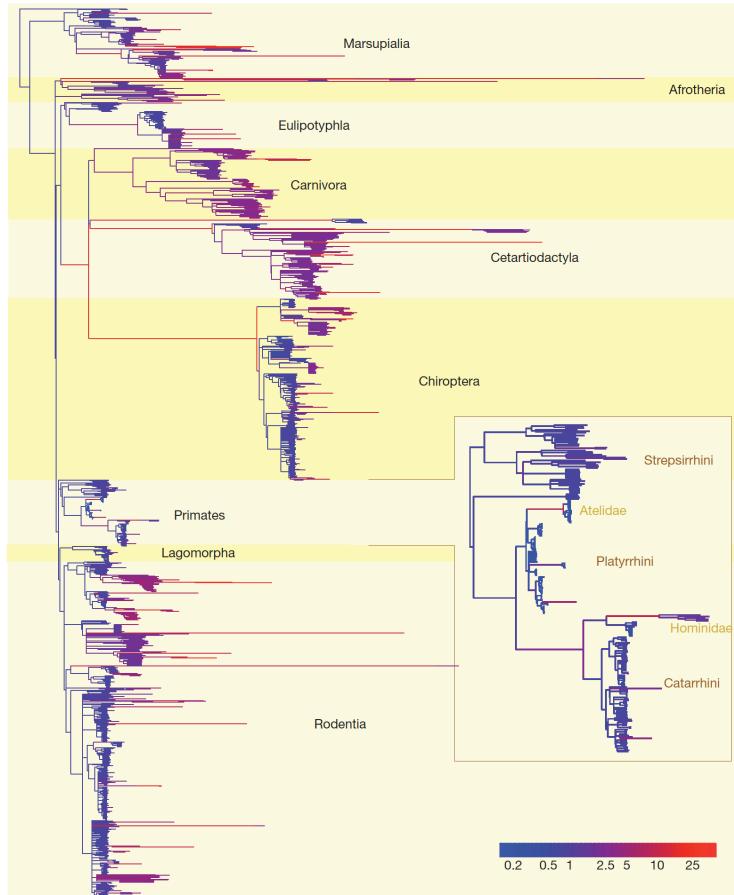


Bokma 2008, 2009

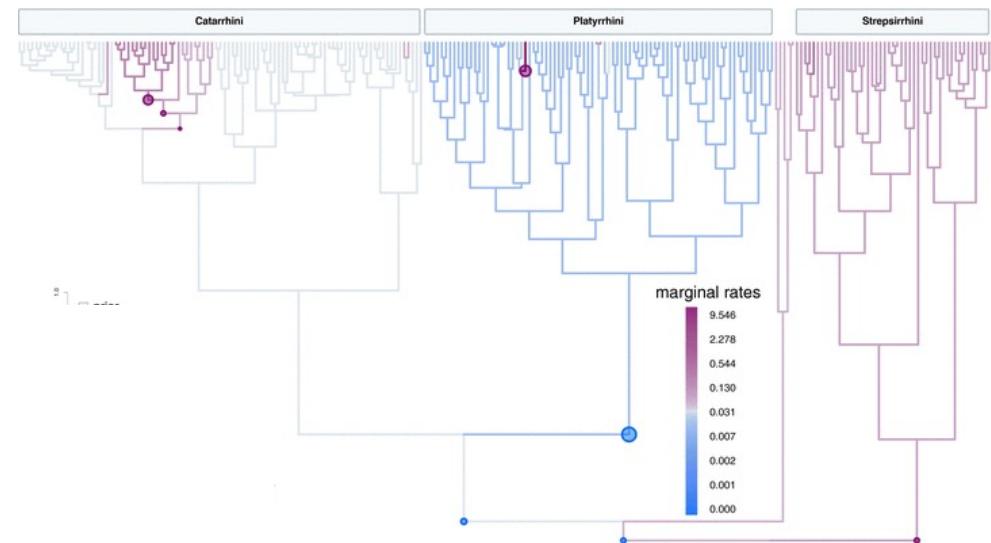
Landis et al. 2013

Duchen et al. 2017

# Models of phenotypic evolution with rates that vary across lineages



Venditti et al. *Nature* 2011



Eastman et al. *Evolution* 2011

# Models of phenotypic evolution with rates that vary according to interspecific interactions

*Syst. Biol.* 65(4):700–710, 2016  
© The Author(s) 2016. Published by Oxford University Press, on behalf of the Society of Systematic Biologists. All rights reserved.  
For Permissions, please email: journals.permissions@oup.com  
DOI:10.1093/sysbio/syw020  
Advance Access publication March 9, 2016

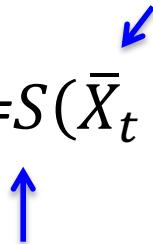


Jonathan Drury

## Estimating the Effect of Competition on Trait Evolution Using Maximum Likelihood Inference

JONATHAN DRURY\*, JULIEN CLAVEL, MARC MANCEAU, AND HÉLÈNE MORLON

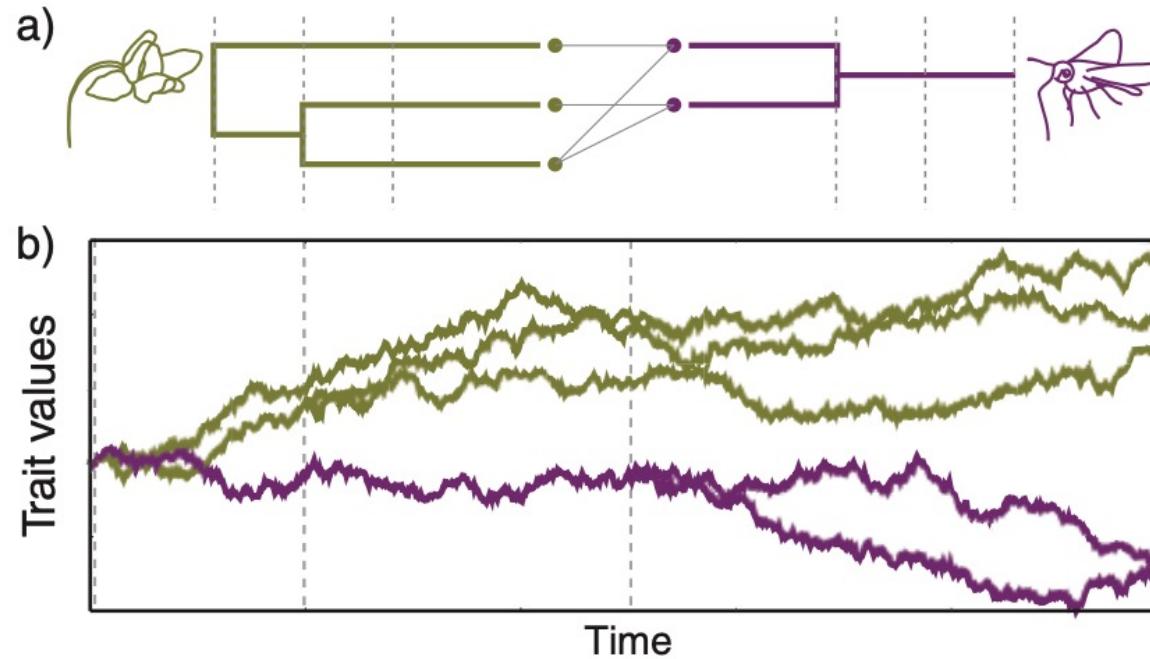
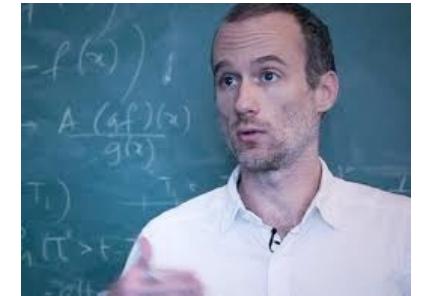
$$dX(t) = S(\bar{X}_t - X_t)dt + \sigma dB(t)$$



average trait value in the clade at time t

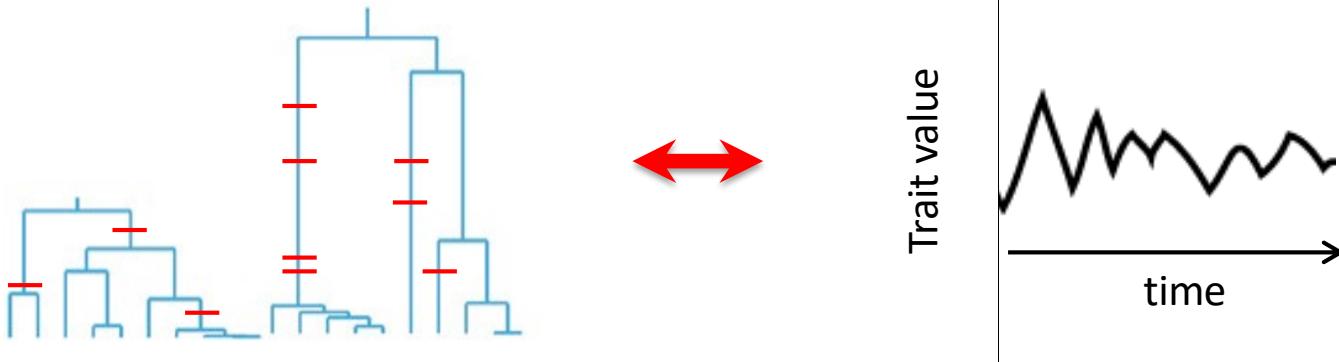
strength of interaction  
 $S < 0$  : matching competition (beak shape in competition for food)  
 $S > 0$  : matching mutualism (Mullerian mimicry)

# Models of phenotypic evolution with rates that vary according to interspecific interactions



**What are the microevolutionary processes that modulate phenotypic evolution on macroevolutionary timescales?**

# A microscopic model of phenotypic evolution with macroevolutionary predictions



Lande (*Evolution* 1976)

Hypothesis 1: trait distribution is Gaussian with constant variance

$$p(z, t) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left\{-\frac{[z - \bar{z}(t)]^2}{2\sigma^2}\right\}$$

Hypothesis 2: fitness function is Gaussian

$$W(z) = \exp\left\{-\frac{(z - \vartheta)^2}{2w^2}\right\}$$

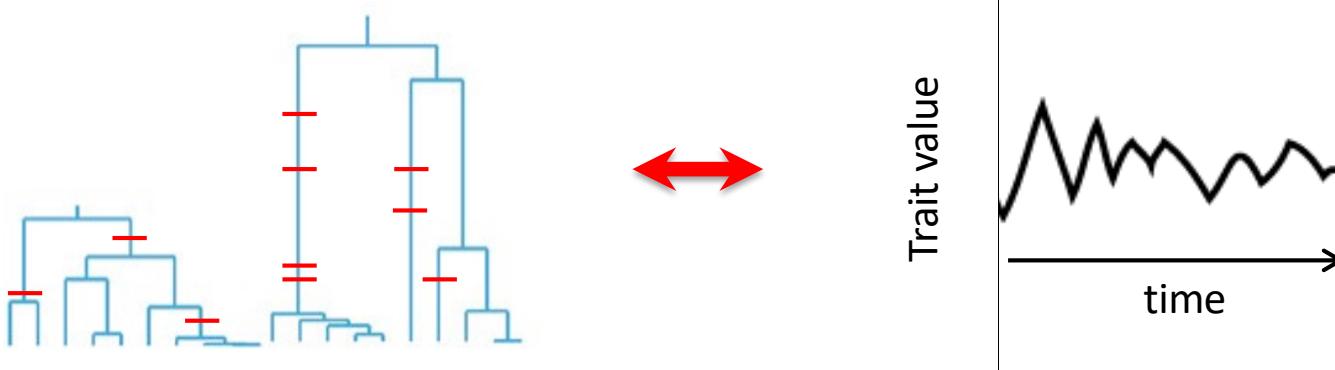
Hypothesis 3: constant population size N

$$d\bar{z}(t) = A[\theta - \bar{z}(t)]dt + \Sigma dB(t)$$

$$A = \frac{\sigma^2}{w^2 + \sigma^2}$$

$$\Sigma = \frac{\sigma^2}{N}$$

# A microscopic model of phenotypic evolution with macroevolutionary predictions



In the framework of adaptive dynamics?

*The Annals of Applied Probability*  
2007, Vol. 17, No. 1, 102–155  
DOI: 10.1214/105051606000000628  
© Institute of Mathematical Statistics, 2007

## EVOLUTION OF DISCRETE POPULATIONS AND THE CANONICAL DIFFUSION OF ADAPTIVE DYNAMICS<sup>1</sup>

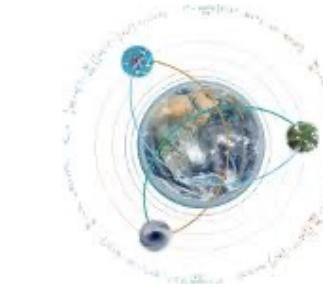
BY NICOLAS CHAMPAGNAT AND AMAURY LAMBERT

Birth-death model + rare mutations + artificially avoid extinction

→ Diffusion equation for the trait

# Phenotypic evolution in a Moran model

- N individuals following a Moran process
- individuals characterized by quantitative trait  $x$
- at rate  $c(x,y)$ , an individual of trait  $x$  dies and is replaced by an individual of trait  $y$

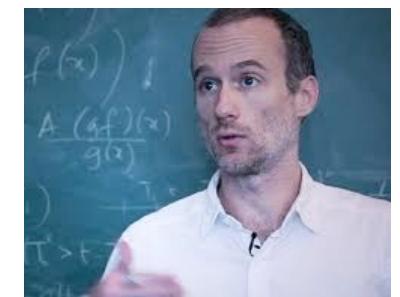


Thuy Vo

- quantitative trait  $z$  results from genetic architecture
- $$z^i = \frac{1}{L} \sum_{l=1}^L w_l \eta_l^i$$
- number of loci      ↓  
                            ↑  
                            allelic state  
                            genetic effect
- mutations occur at rate  $\gamma\mu$  with  $\gamma$  between 0 and 1 ; when they occur, each nucleotide mutates with proba  $\alpha$



Hélène Leman



Amaury Lambert

# Phenotypic evolution in a Moran model



First result Accelerate time  $t \mapsto t/\gamma$   
Take the limit of rare mutations  $\gamma \rightarrow 0$

Trait evolves as jump process  
with a rate that depends on N and c

Thuy Vo



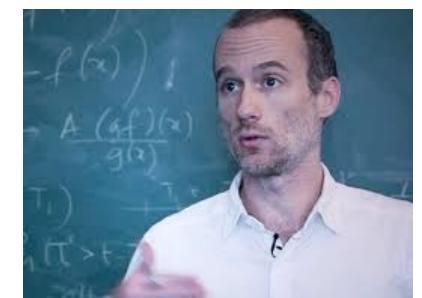
Second result Accelerate time  
Take the limit of small mutational effect  $L \rightarrow \infty$

Canonical diffusion equation

Hélène Leman

$$dZ_t = \frac{1}{2} N^2 \sigma^2 \mu \partial_2 f_N(Z_t, Z_t) dt + \sigma(Z_t) \sqrt{N \mu c_N(Z_t, Z_t)} dB_t$$

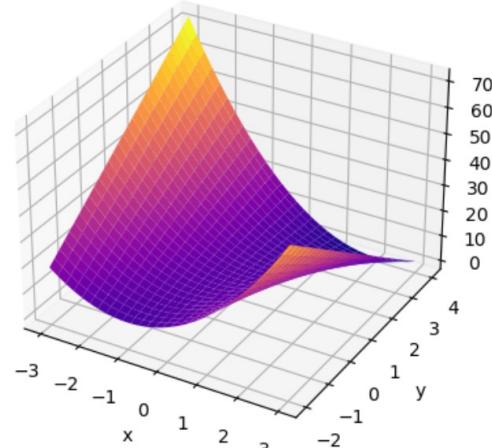
with  $f_N(x, y) := c_N(y, x) - c_N(x, y)$ . the fitness



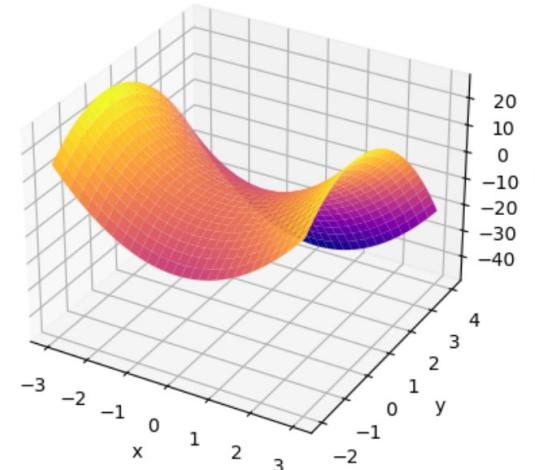
Amaury Lambert

# Phenotypic evolution in a Moran model

Case that leads to the Orstein-Uhlenbeck



$$c_N(x,y) = \frac{1}{N} (b(x-a)(x-y) + k_1) + k_2$$



$$f_N(x,y)$$

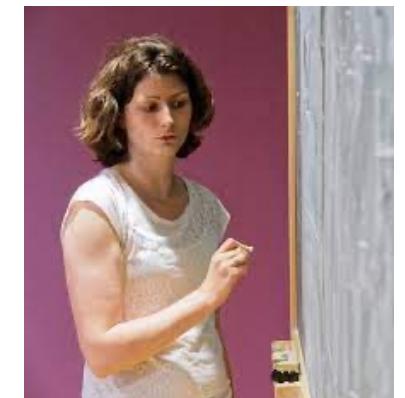
$$d\tilde{Z}_u = \underbrace{\sigma^2 \mu b(a - \tilde{Z}_u) du}_{\text{strength of selection}} + \underbrace{\sigma \sqrt{\mu \left( \frac{k_1}{N} + k_2 \right)}}_{\text{drift}} dB_u.$$

strength of selection

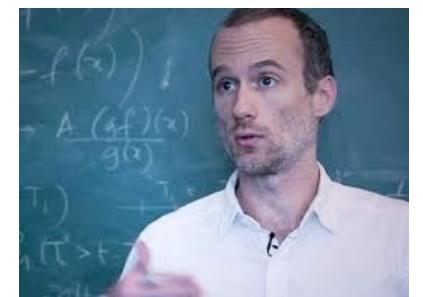
drift



Thuy Vo



Hélène Leman



Amaury Lambert

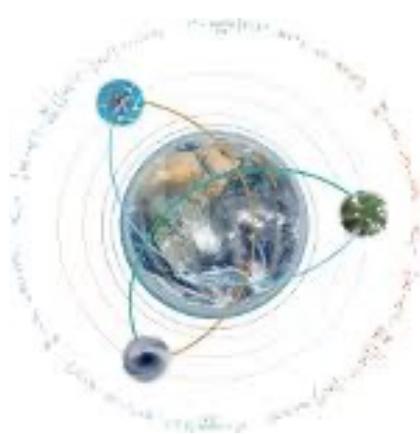
→ Can be estimated by fit of the OU model to phylogenetic comparative data



**Thuy Vo**



**Hélène Leman**



**Amaury Lambert**



Fabien Condamine



Olivier Billaud



Joelle Barido-Sottani

# THANKS!



Nathan Mazet



Ignacio Quintero



Jakub Voznica



Jonathan Rolland



Dan Moen



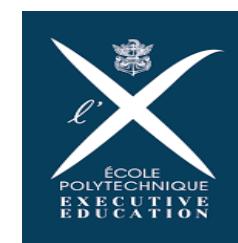
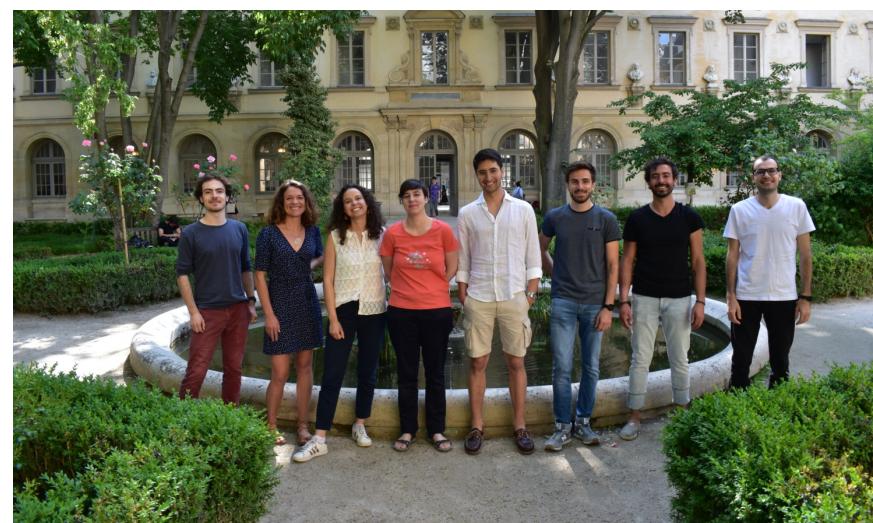
Jérémie  
Andréoletti



Sophia Lambert



Odile Maliet



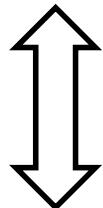
# What are the factors that modulate rates of species diversification?



The Court Jester

**Abiotic factors**  
climatic variation  
geological context

EXTRINSIC



The Red Queen

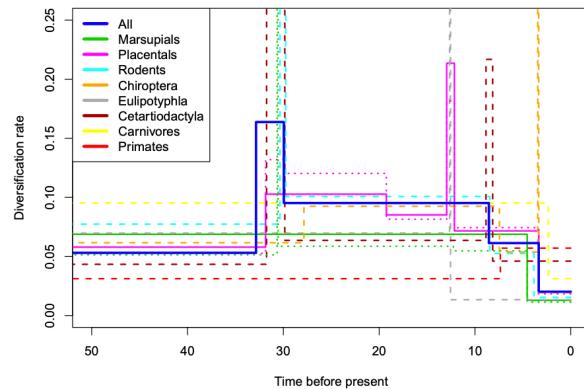
**Biotic factors**  
competition  
mutualistic and antagonistic interactions

INTRINSIC

**Species-specific traits**  
reproduction mode  
life-history traits  
dispersal capacity  
developmental constraints

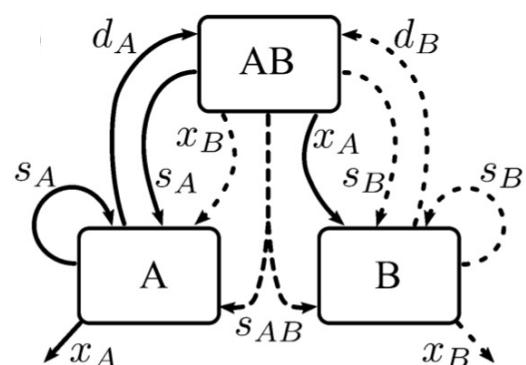
# Phylogenetic birth-death models allow testing if and how diversification rates vary:

## Through time



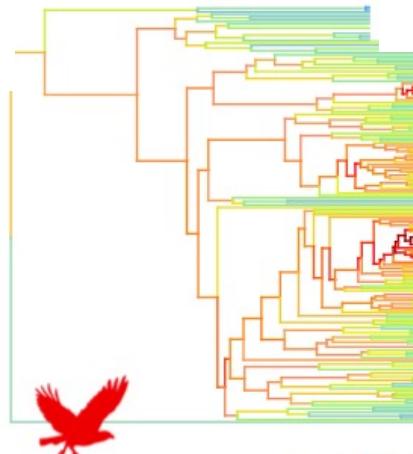
Stadler *et al.* PNAS 2011,  
Morlon *et al.* PNAS 2011,  
May *et al.* MEE 2016, etc...

## Across geographic regions



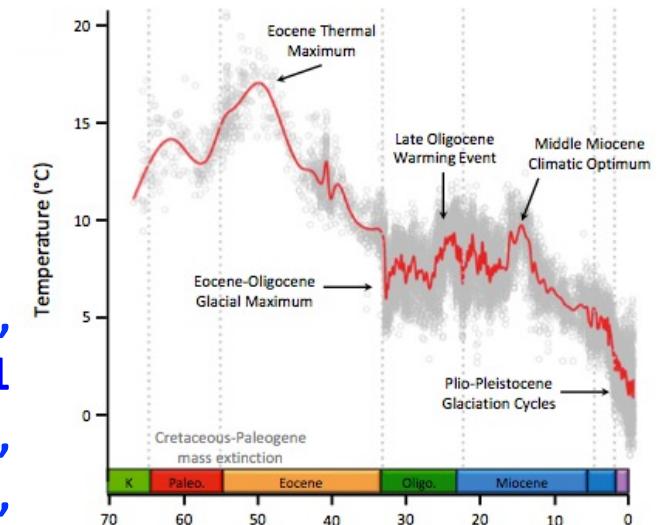
Barido-Sottani *et al.* Syst Bio 2020, etc...

## Across lineages



Alfaro *et al.* PNAS 2009,  
Morlon *et al.* PNAS 2011  
Rabosky *et al.* PloS One 2014,  
Maliet *et al.* NEE 2019,

## With past environmental changes



Condamine *et al.* Eco Lett 2013,  
Lewitus *et al.* Syst Bio 2017

Goldberg *et al.* Syst Bio 2011,  
Quintero *et al.* in press,  
etc...

**REVIEW AND  
SYNTHESIS**

**Phylogenetic approaches for studying diversification**

---

**Abstract**

Hélène Morlon\*

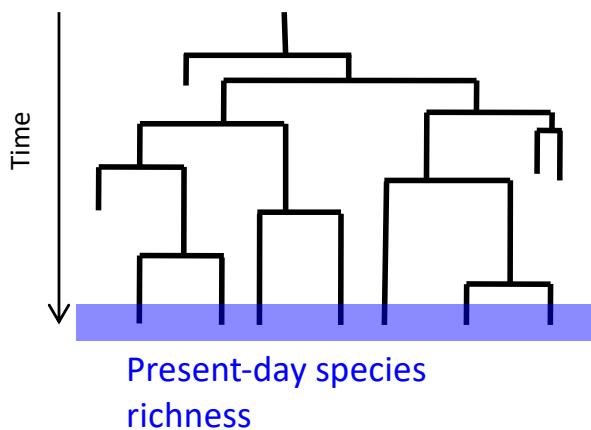
Estimating rates of speciation and extinction, and understanding how and why they vary over evolutionary time, geographical space and species groups is a key to understanding how ecologi-

## Conclusions

**Stochastic models are powerful for understanding modes and rates of diversification and trait evolution, i.e. how biodiversity evolves**

**This is fundamental for understanding current patterns of species and phenotypic diversity**

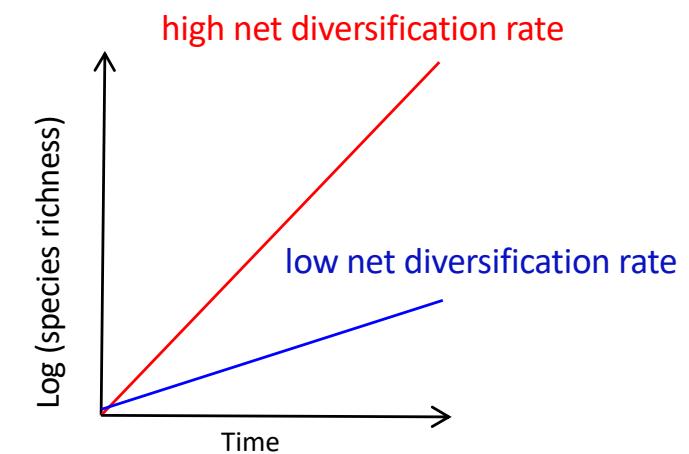
# Current levels of species richness result from the balance of speciation and extinction events



Speciation rate  
average number of  
speciation events per  
Myr per lineage

Extinction rate  
average number of  
extinction events per  
Myr per lineage

Net diversification rate  
speciation rate – extinction rate



# Illustration: the diversification of cetaceans

We can test the statistical support of models where diversification rates “shift” at the base of major families

Support for a 4-shift rate model in the cetacean phylogeny

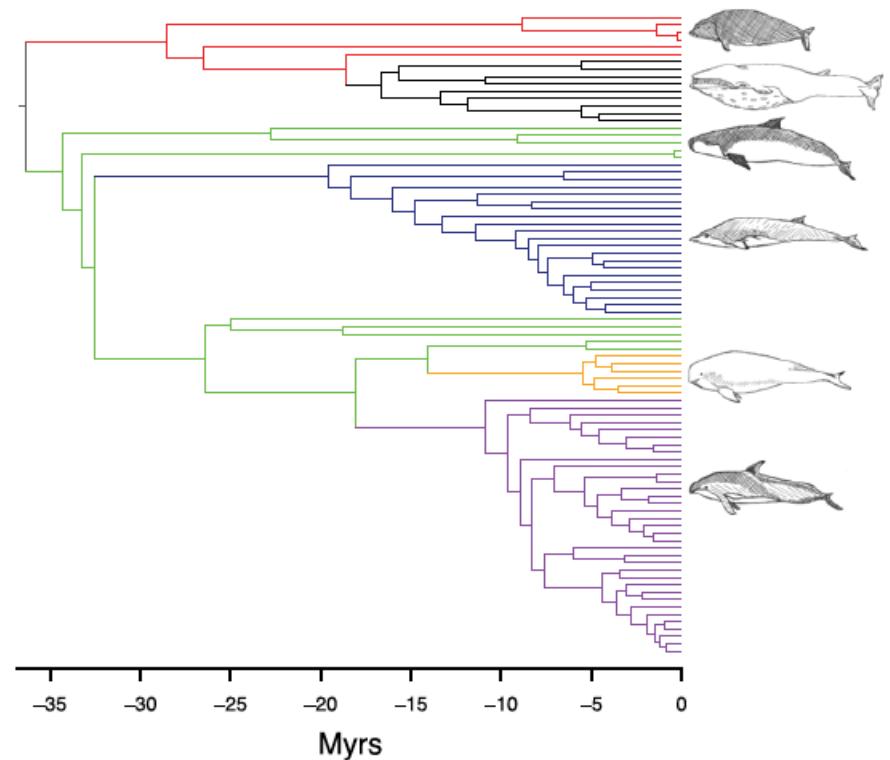
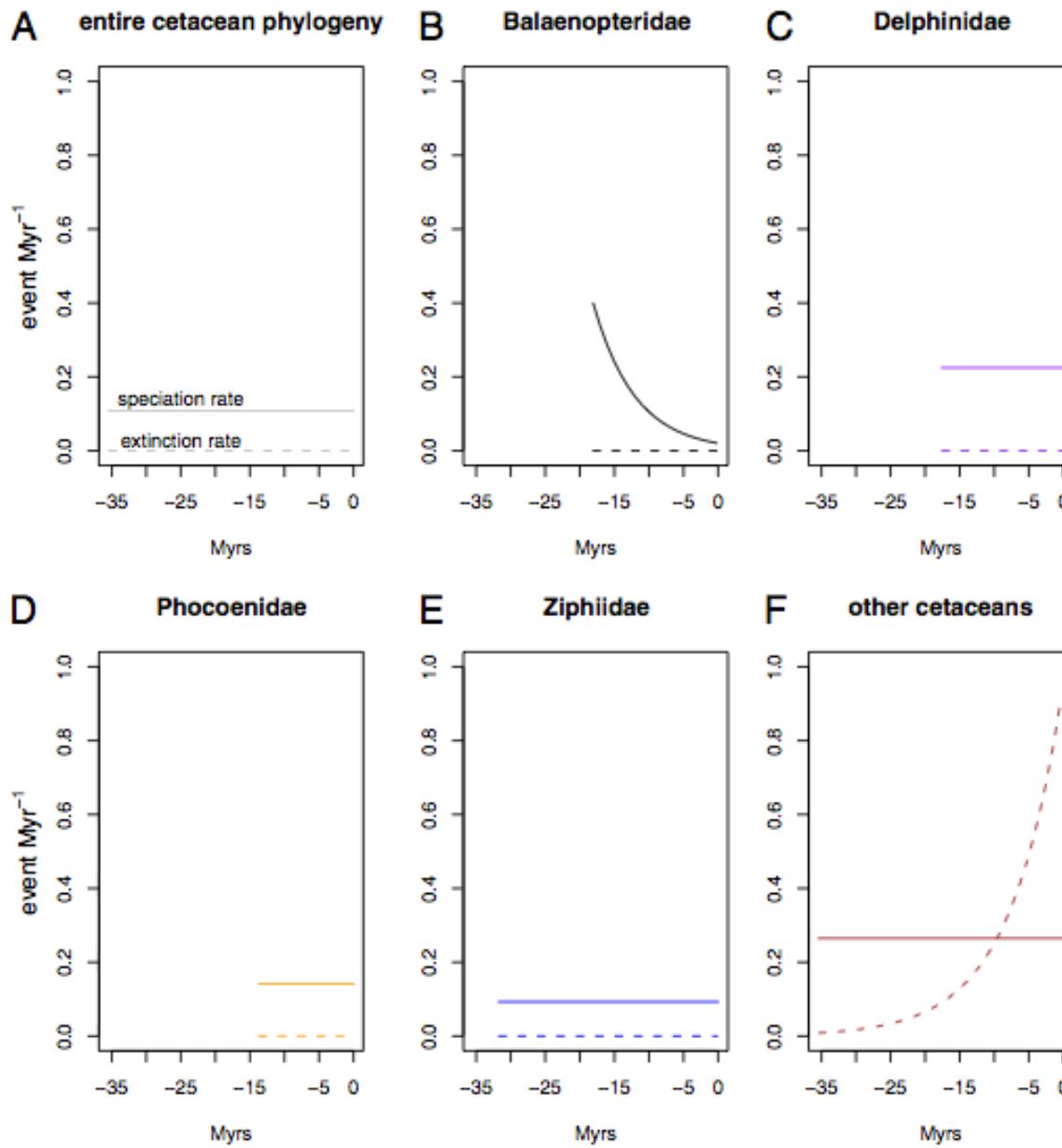


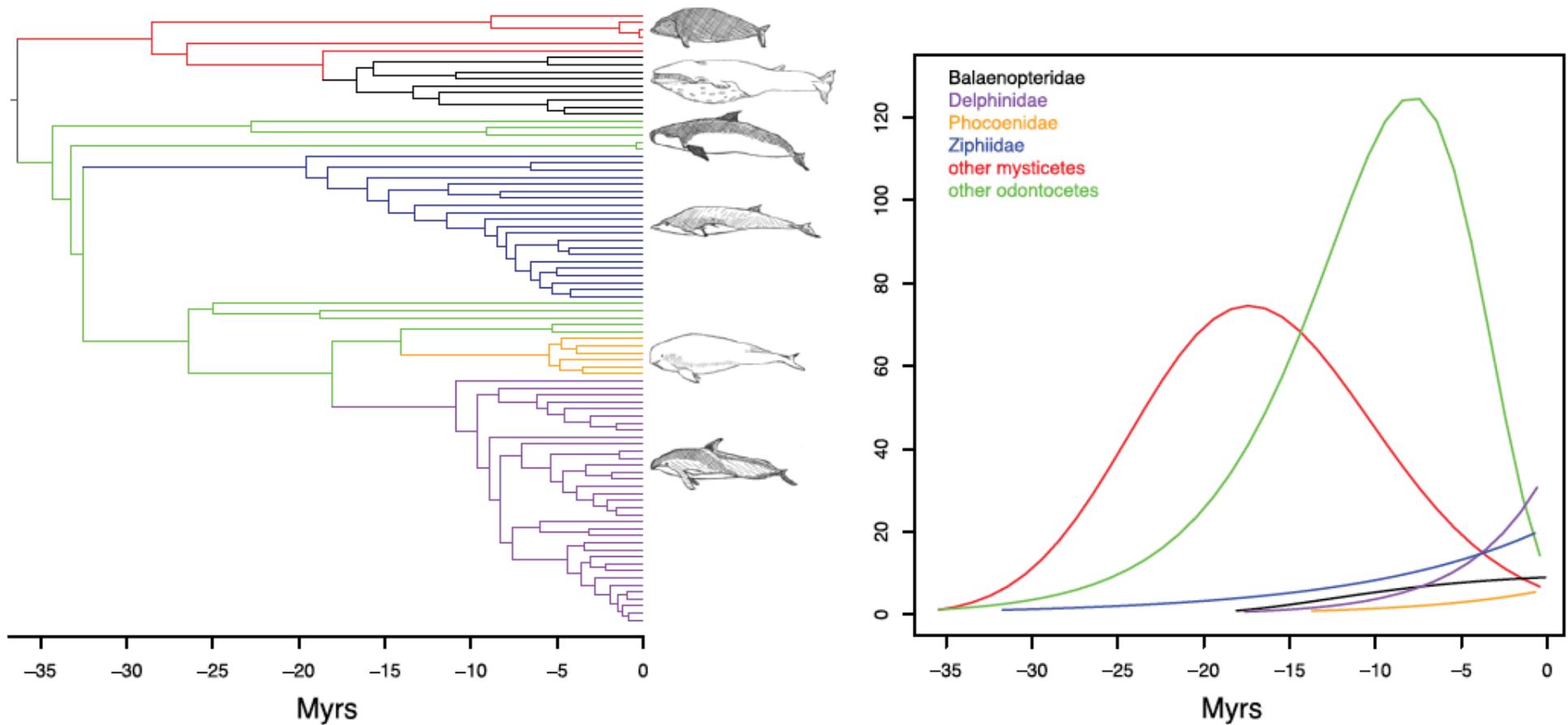
Table S2. Statistical support for rate shifts in the cetacean phylogeny

Model	nb	Description	LogL	AIC <sub>c</sub>
No shift	1	Best fit model	-279.03	560.08
One shift	5	Best fit model: shift in the Delphinidae	-262.93*	536.22
Two shifts	6	Best fit model: shifts in the Delphinidae and Phocoenidae	-260.17†	532.85
Three shifts	7	Best fit model: shifts in the Delphinidae, Phocoenidae and Ziphiidae	-256.13‡	526.94
Four shifts	8	Best fit model: shifts in the Delphinidae, Phocoenidae, Ziphiidae, and Balaenopteridae	-250.13	517.14

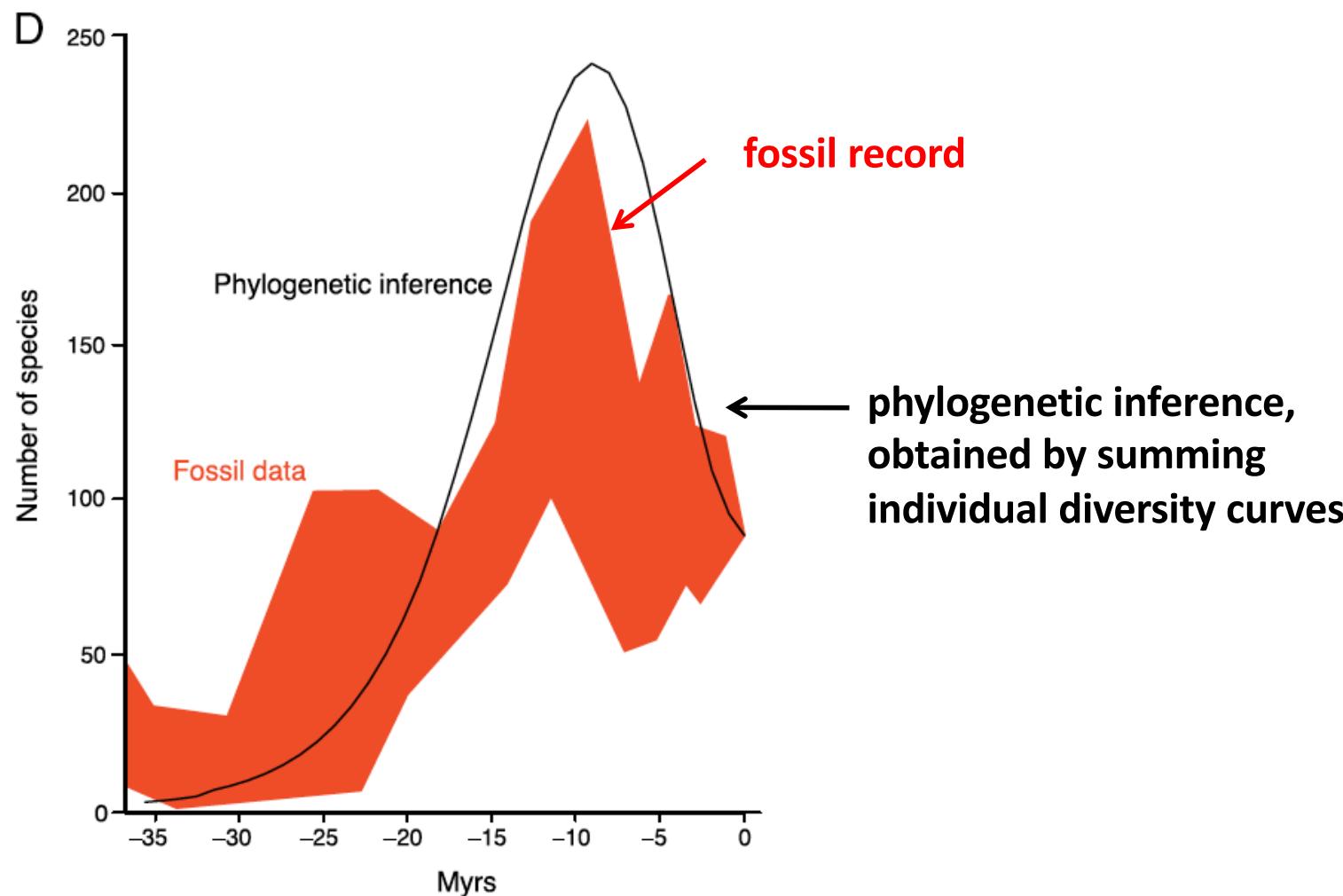
# We can compute estimates of speciation and extinction rates through time



# Resulting estimates of diversity through time : boom-then-bust diversity dynamics



# The resulting diversity curve is consistent with the fossil record

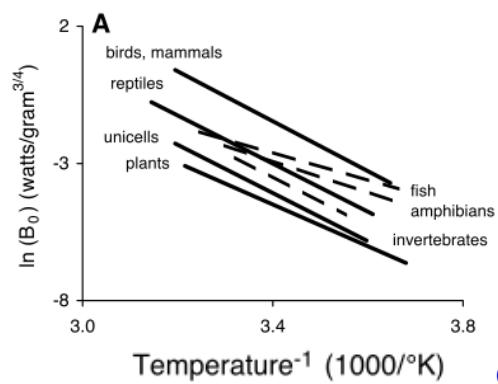


# Temperature affects major aspects of biology through its effect on metabolic rates, body-size, and productivity

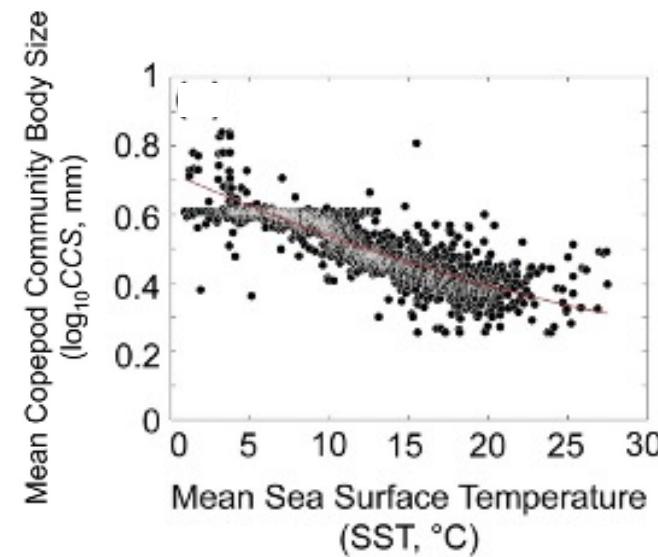
## Kleiber's law

$$B \sim M^{3/4} e^{-E_i/kT}$$

metabolic rate      activation energy      Boltzmann's constant  
body-size



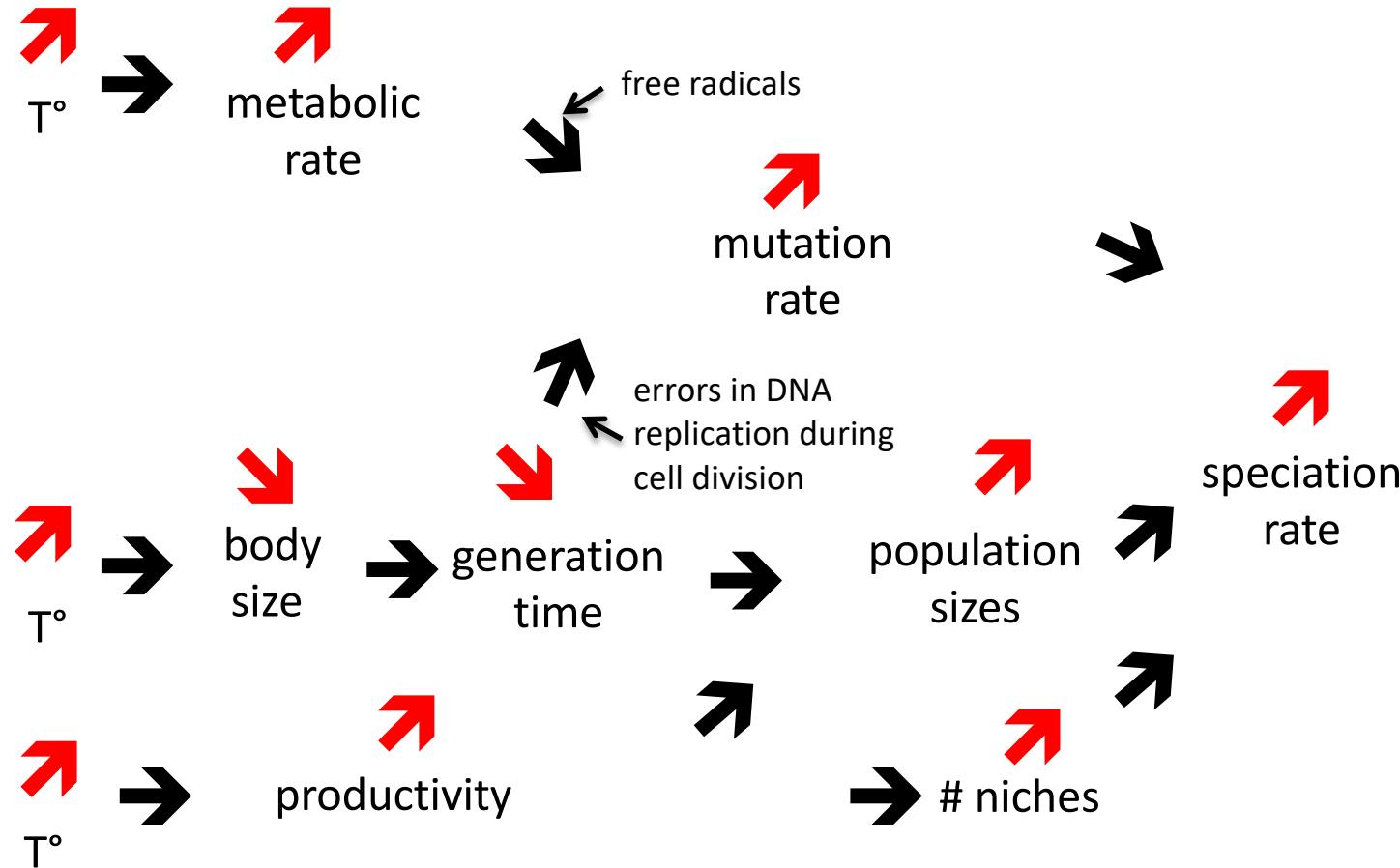
## Bergmann's rule



Evans et al. *Ecography* 2019

Gillooly et al. *Science* 2001

Based on the metabolic, body-size and productivity hypotheses, temperature should (positively) affect speciation rates



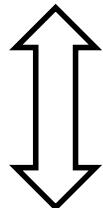
# What are the factors that modulate speciation and extinction rates?



The Court Jester

**Abiotic factors**  
climatic variation  
geological context

EXTRINSIC



The Red Queen

**Biotic factors**  
competition  
mutualistic and antagonistic interactions

INTRINSIC

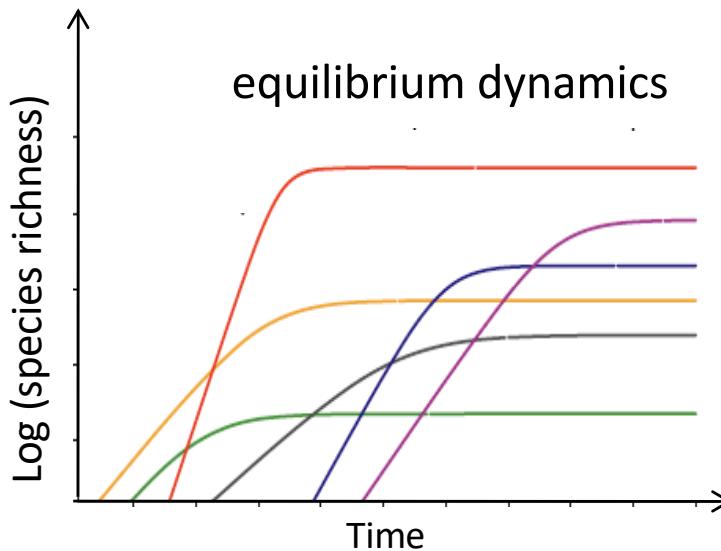


**Species-specific traits**  
reproduction mode  
life-history traits  
dispersal capacity



Biotic factors  
competition

## Diversity-dependent birth-death models



PROCEEDINGS  
OF  
THE ROYAL  
SOCIETY **B**

*Proc. R. Soc. B* (2012) **279**, 1300–1309  
doi:10.1098/rspb.2011.1439  
Published online 12 October 2011

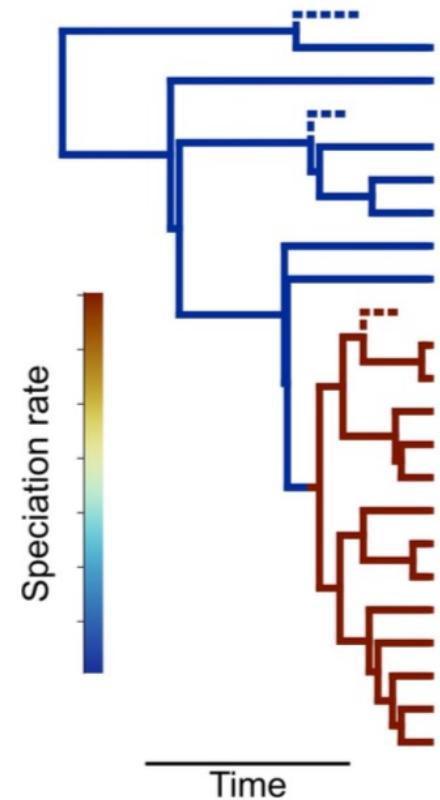
### Diversity-dependence brings molecular phylogenies closer to agreement with the fossil record

Rampal S. Etienne<sup>1,\*</sup>, Bart Haegeman<sup>2</sup>, Tanja Stadler<sup>3</sup>, Tracy Aze<sup>4</sup>,  
Paul N. Pearson<sup>4</sup>, Andy Purvis<sup>5</sup> and Albert B. Phillimore<sup>5</sup>

<sup>1</sup>Community and Conservation Ecology, Centre for Ecological and Evolutionary Studies,

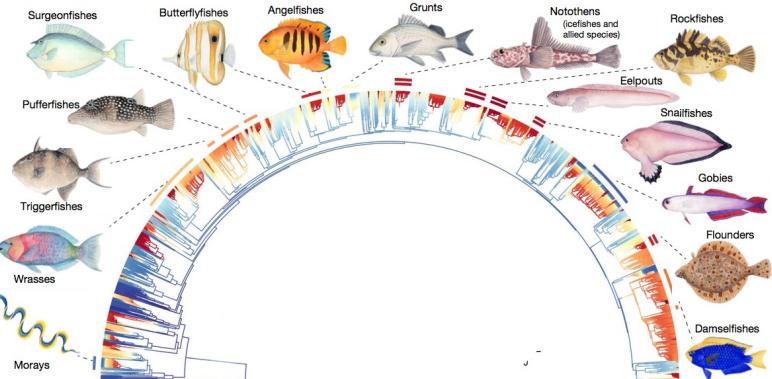
# Les modèles de naissance-mort, combinés à une approche d'inférence statistique, permettent d'estimer les taux de spéciation et d'extinction et les variations passées de la biodiversité

Modèle de diversification

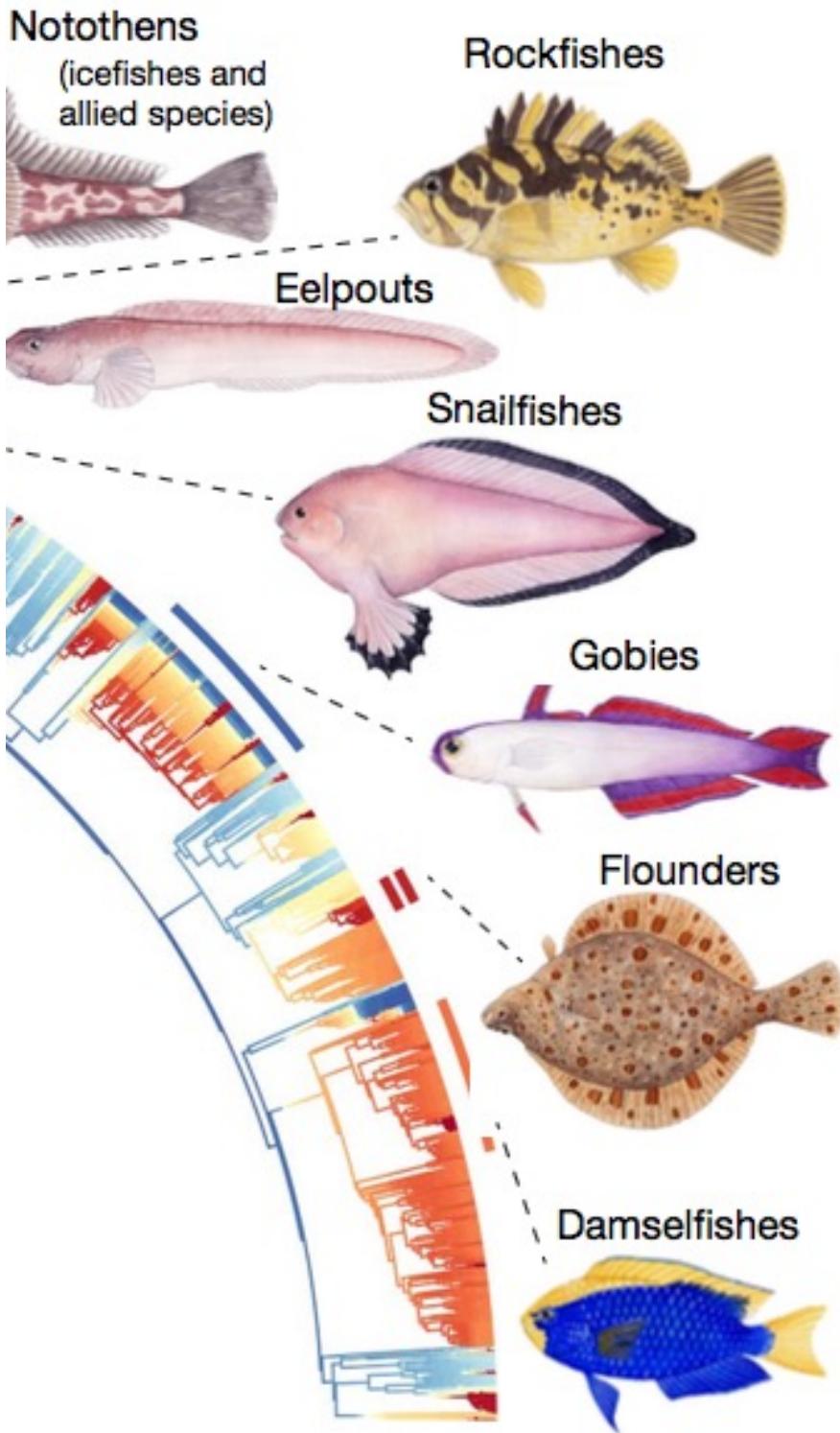


Inférence  
Statistique

Arbre phylogénétique



Estimation des taux de spéciation et extinction, et de la diversité passée

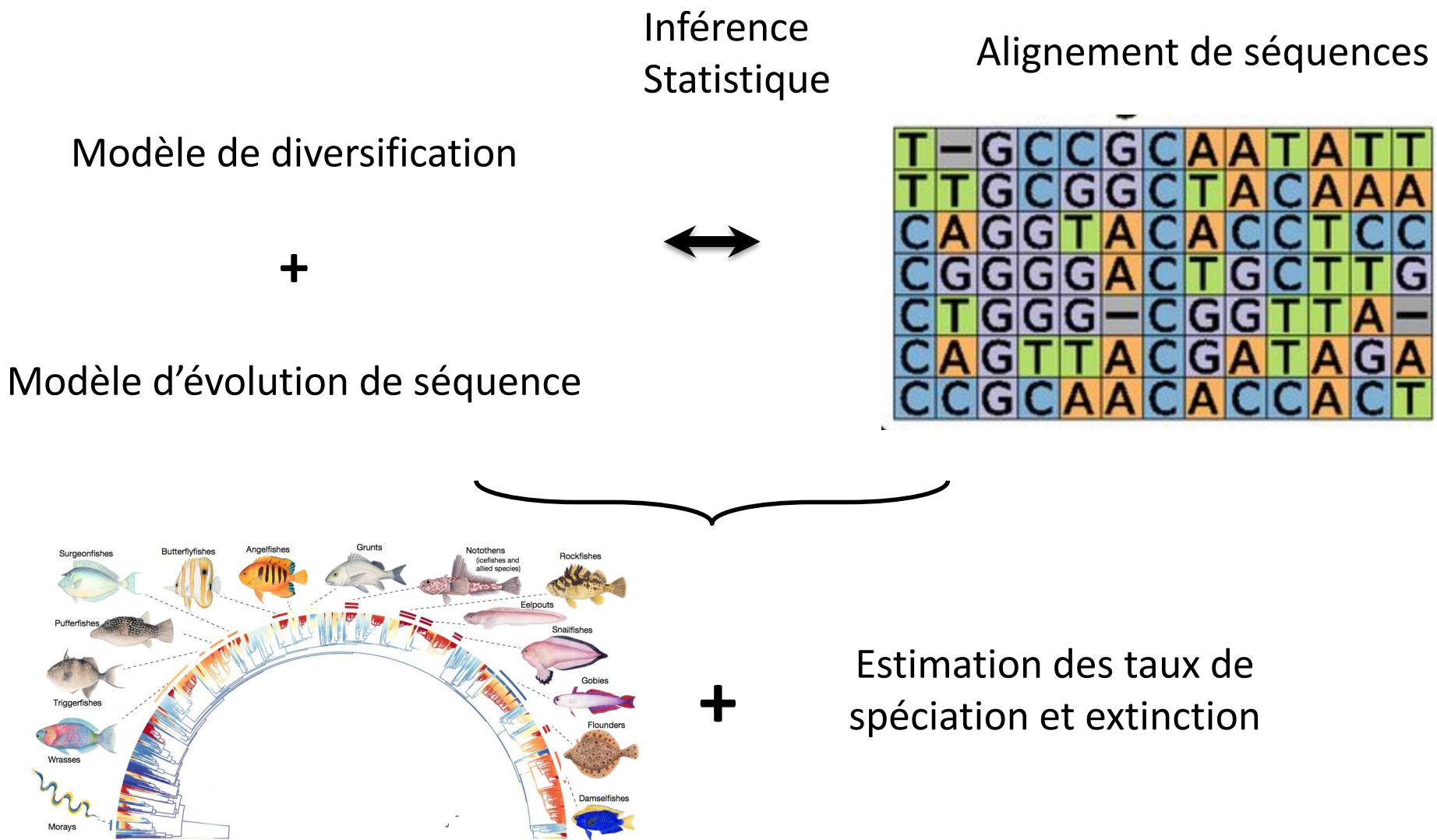


Dans ces approches, nous considérons l'arbre phylogénétique (daté) comme une donnée

L'arbre est en fait construit à partir d'un modèle d'évolution des séquences

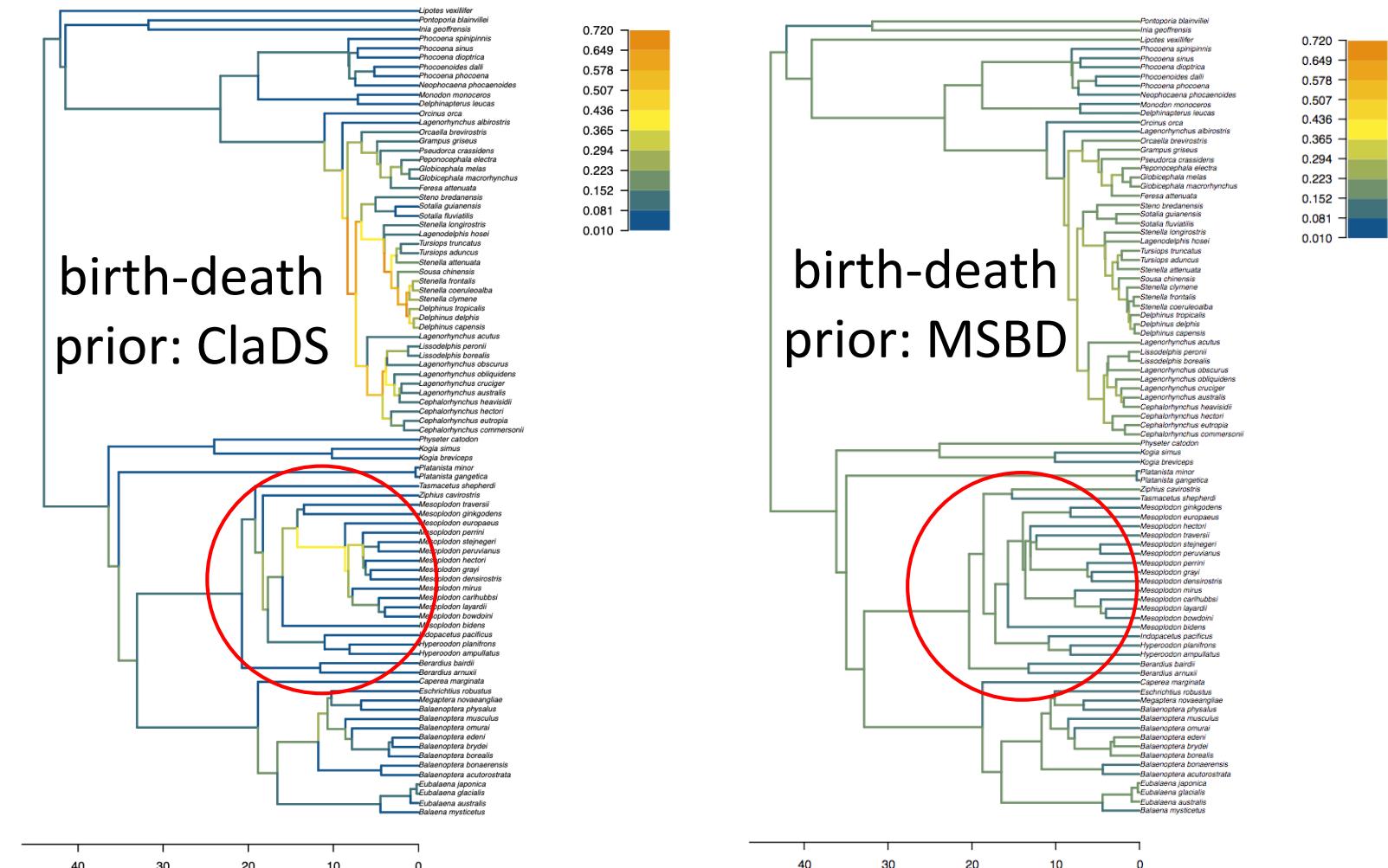
Des les approches bayésiennes de reconstruction phylogénétique, le modèle de naissance-mort est utilisé comme un prior

# Inférence bayésienne « complète »





# ClaDS now integrated in BEAST2 for full Bayesian phylogenetic inference



Available for ClaDS<sub>2</sub> (constant turnover) and extinction also following a lognormal variation at speciation

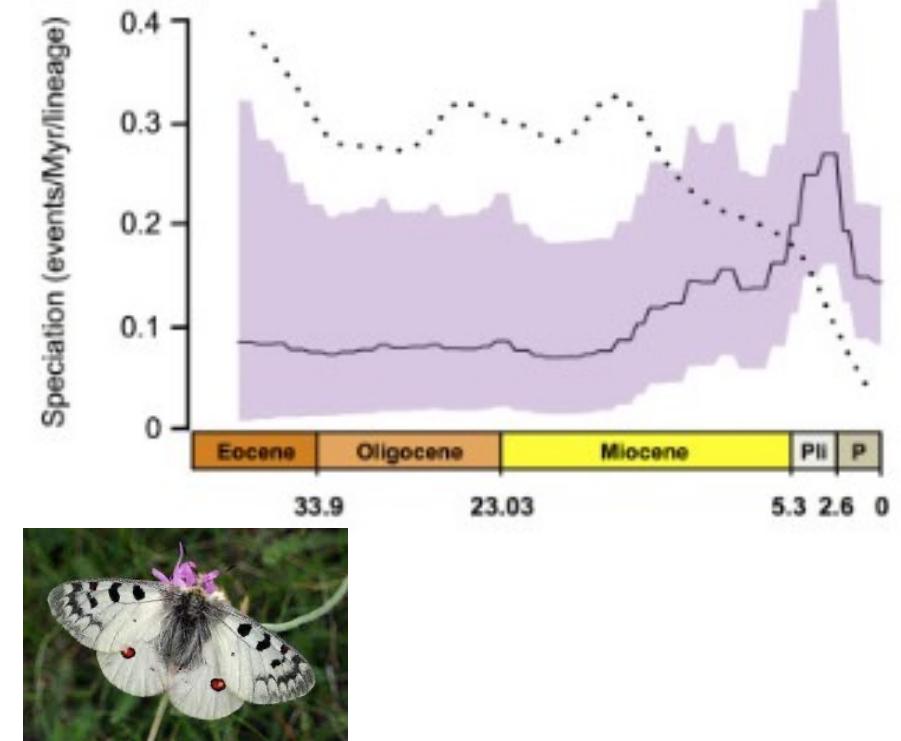
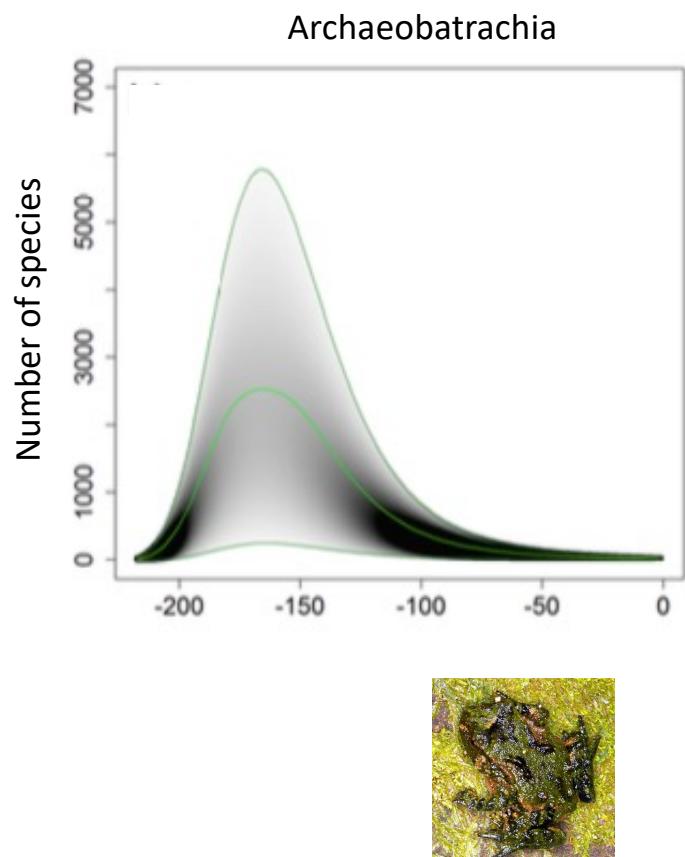


**Beast2**

Bayesian evolutionary analysis by sampling trees

Barido-Sottani & Morlon  
Syst Bio (2023)

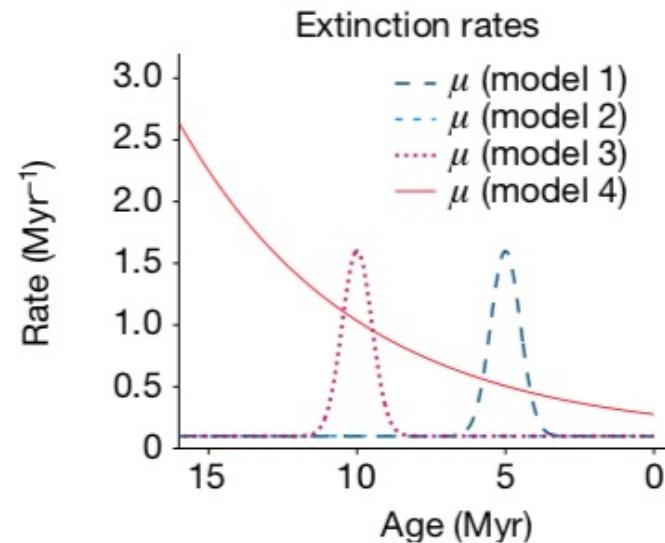
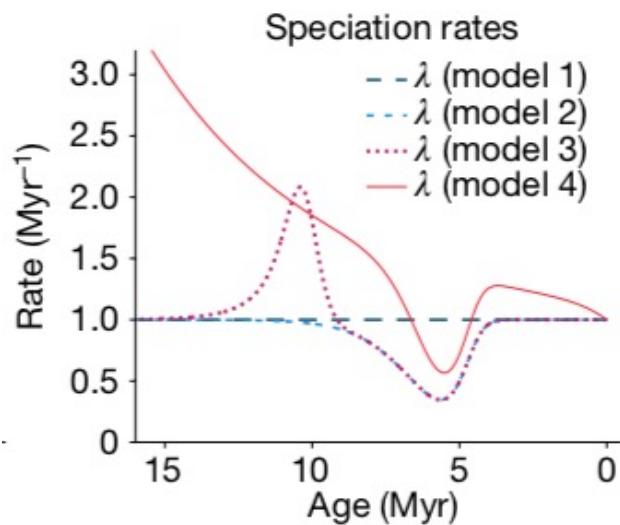
# Quelle confiance dans ces inférences?



# Problèmes d'identifiabilité?

**Extant timetrees are consistent with a myriad of diversification histories**

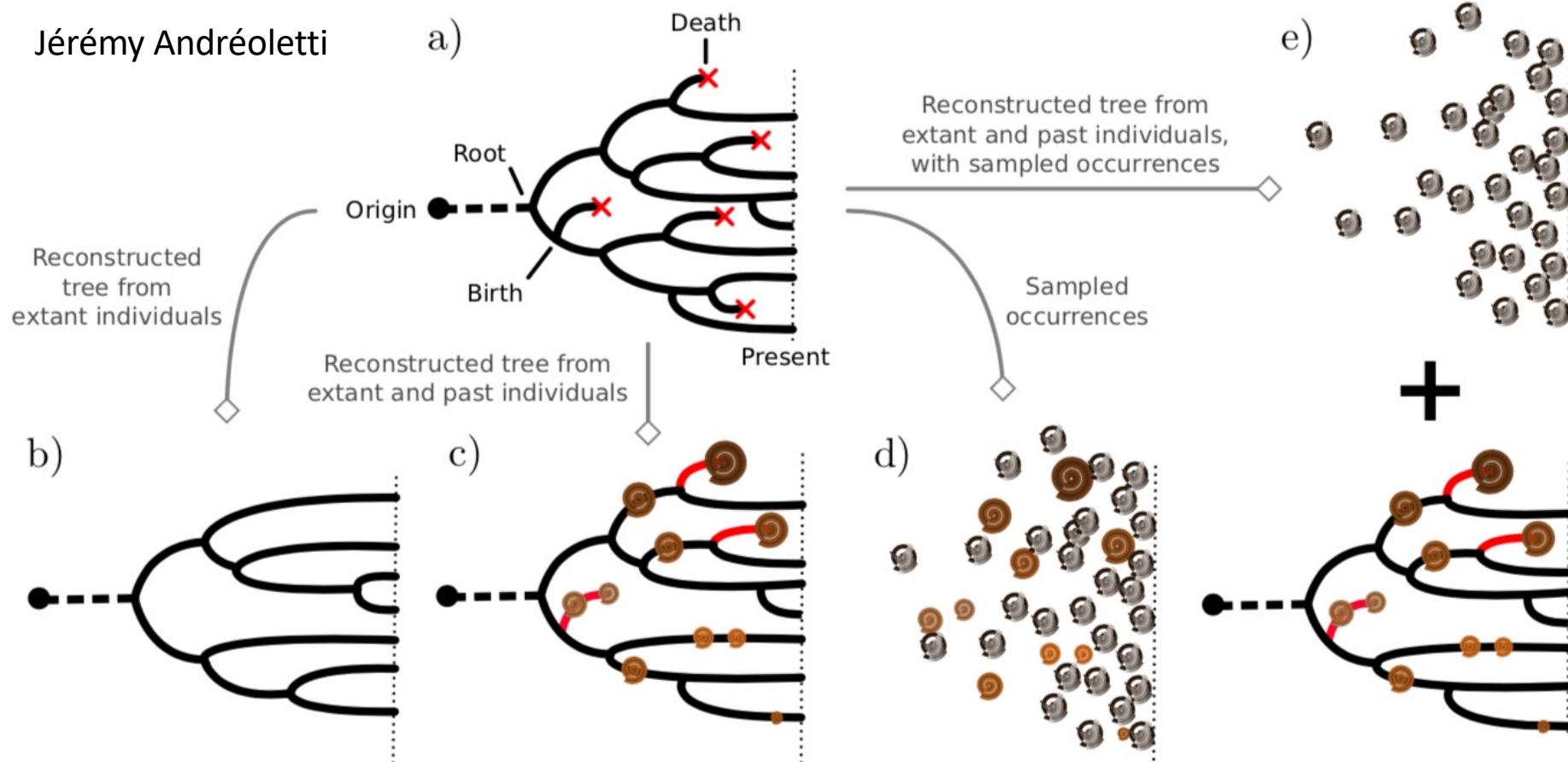
Louca & Pennell Nature 2020





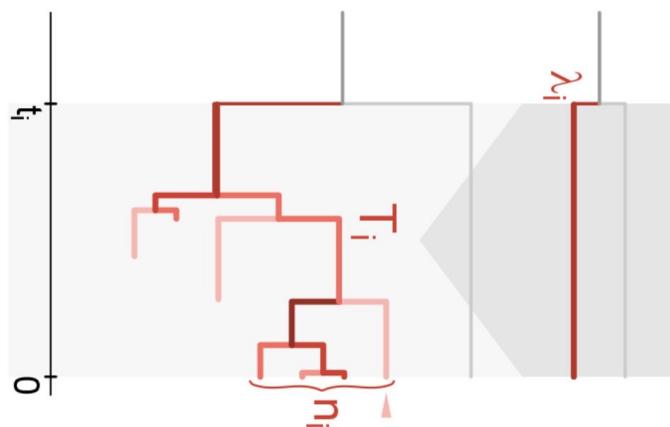
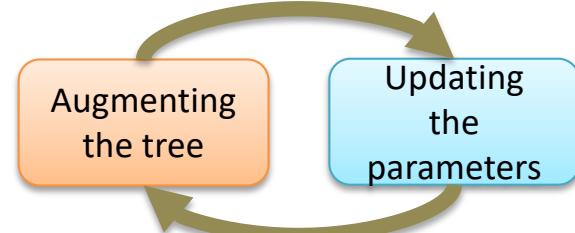
# Intégrer données moléculaires et fossiles dans les inférences de la diversification

Jérémie Andréoletti

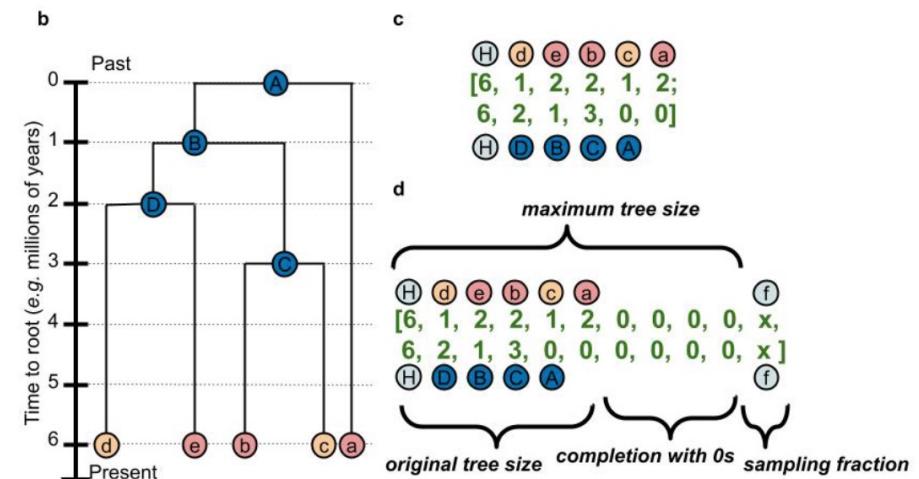


# Les limites de l'inférence statistique « classique » et les approches alternatives

## Inférence par augmentation de données



## Apprentissage profond



Lambert et al.  
*Syst Bio* 2023

These tools are implemented in well-documented, user-friendly packages

## Methods in Ecology and Evolution

*Methods in Ecology and Evolution* 2016, 7, 589–597



doi: 10.1111/2041-210X.12526



APPLICATION

### RPANDA: an R package for macroevolutionary analyses on phylogenetic trees

Hélène Morlon<sup>1\*</sup>, Eric Lewitus<sup>1</sup>, Fabien L. Condamine<sup>2</sup>, Marc Manceau<sup>1</sup>, Julien Clavel<sup>1</sup> and Jonathan Drury<sup>1</sup>



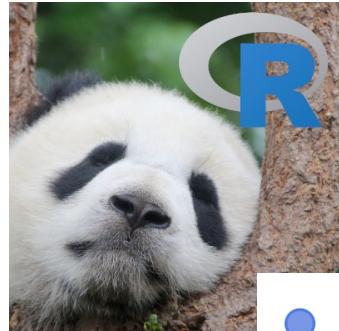
## Beast2

Bayesian evolutionary analysis by sampling trees

## julia



<https://www.transmittingscience.com/>



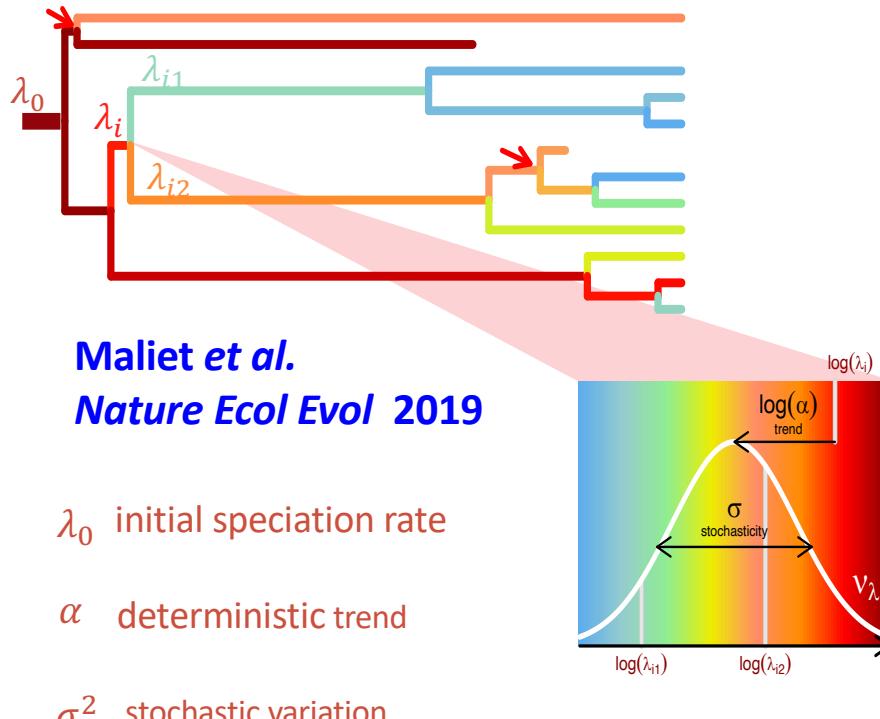
## UNDERSTANDING MACROEVOLUTIONARY DYNAMICS USING RPANDA AND JPANDA



Bayesian evolutionary analysis by sampling trees

## BAYESIAN PHYLOGENETIC INFERENCE WITH BEAST2

# Towards macroevolutionary models accounting for the interplay between speciation and demography / intraspecific genetic differentiation



## + Demographic process



Overcast et al. in prep.

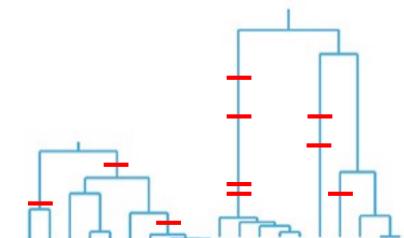
each species follows density-dependent population dynamics  
growth rate evolves as a Brownian

random split of individuals at speciation

extinction naturally proceeds from the death of all individuals in a given species

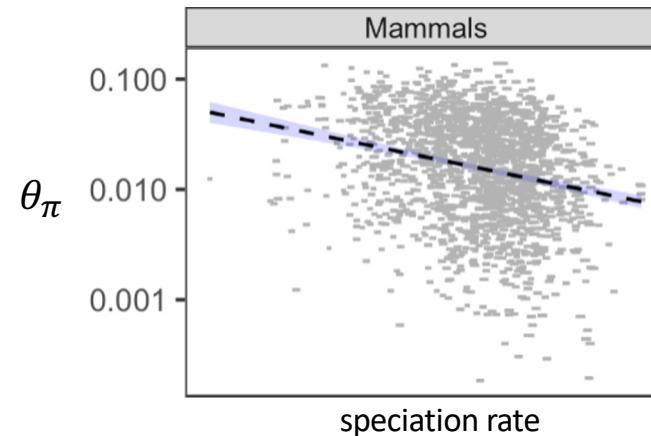
## + Population genetics

demography controls  $N_e$



# The model predicts either a positive or negative association between speciation rate and genetic diversity depending of the relative pace of speciation and accumulation of genetic diversity

Rapid speciation can limit the accumulation of genetic diversity



The model can be fitted to data using machine learning techniques