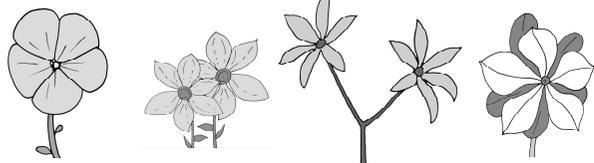




# Ecological networks and interaction types : which modelling approaches?

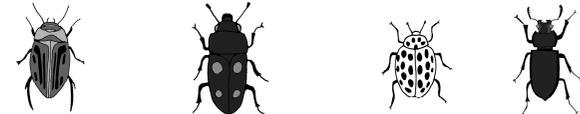


Mutualistic interactions



**Elisa Thébault**

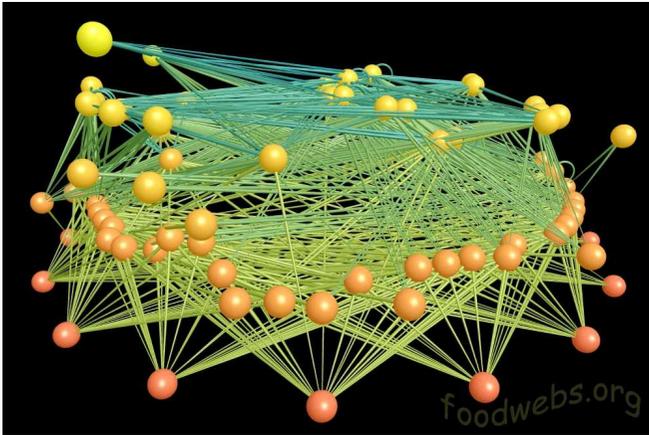
*Wageningen University,  
The Netherlands*



Trophic interactions



# interaction networks



# Modelling the dynamics of interaction networks

*From May's work ...*

Dynamic of a  $n$  species community near equilibrium:

$$\frac{dx_i}{dt} = \sum_{j=1}^n a_{ij} x_j$$

with  $a_{ij}$  the effect of species  $j$  upon species  $i$  near equilibrium



Stable if  $s(nC)^{0.5} < 1$

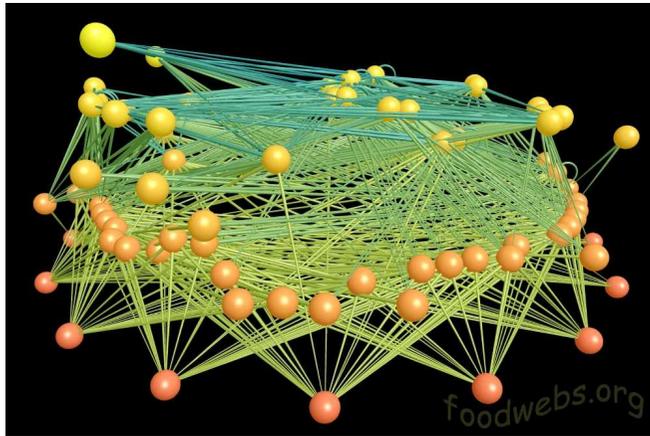
		Effect of species $j$ on $i$ (i.e., sign of $a_{ij}$ )		
		+	0	-
Effect of species $i$ on $j$ (i.e., sign of $a_{ji}$ )	+	++	+0	+-
	0	0+	00	0-
	-	-+	-0	--

Apart from complete independence, there are five distinguishably different categories of interaction between any given pair of species, namely commensalism (+0), amensalism (-0) mutualism or symbiosis (++) , competition (--), and general predator-prey (+-) including plant-herbivore, parasite-host, and so on.

$s$  interaction strength  
 $C$  network connectance

May 1973

# Modelling the dynamics of interaction networks

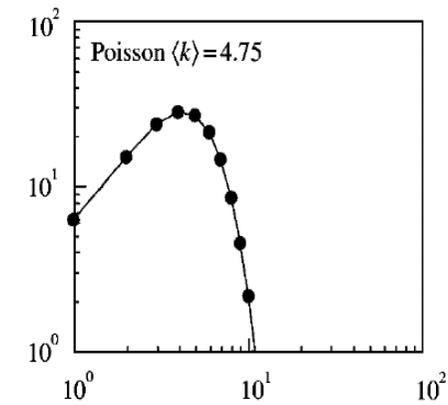
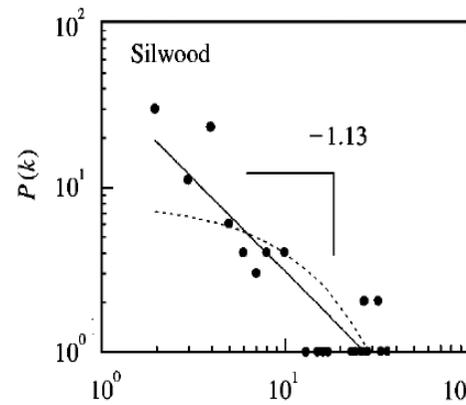
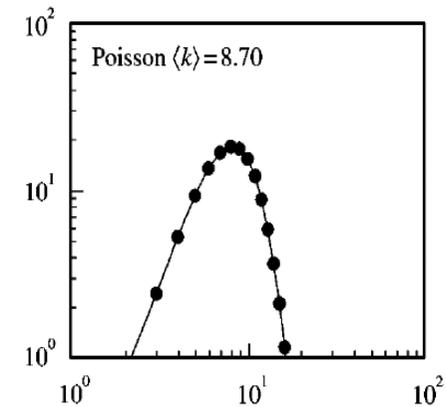
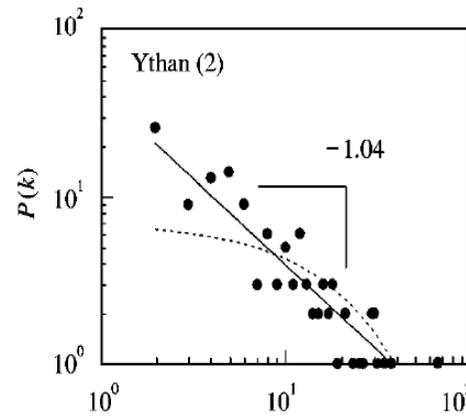


non random  
structural patterns

... to now

empirical data

random expectation

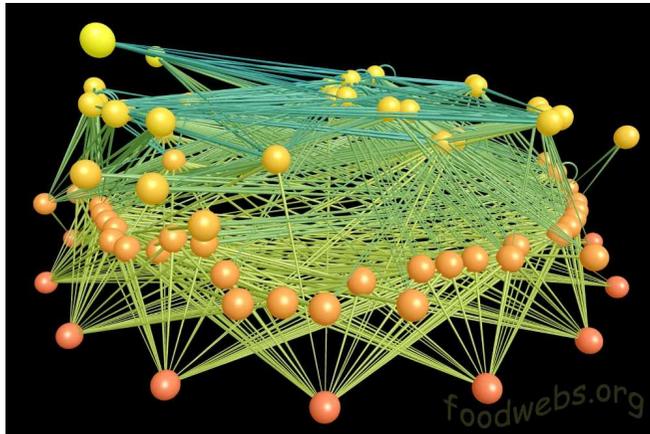


Number of links  $k$

Number of links  $k$

Montoya & Solé (2002)

# Modelling the dynamics of interaction networks

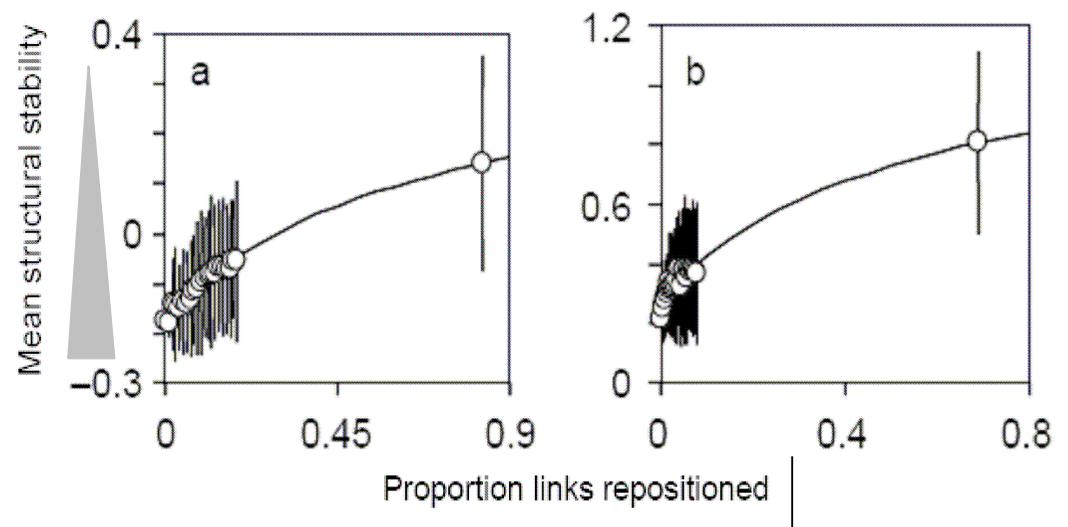


non random  
structural patterns



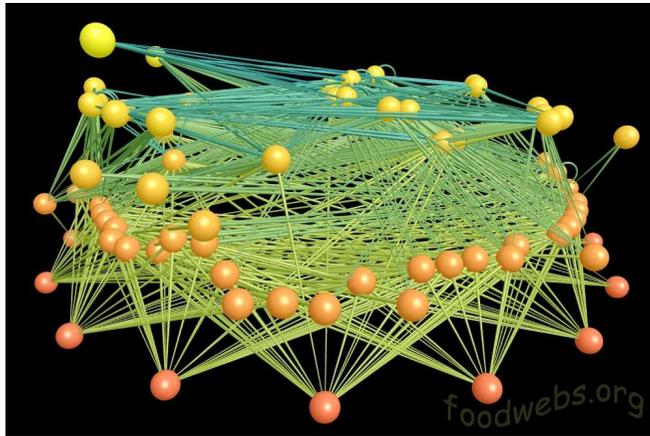
community stability

*... to now*



Non random structural patterns enhance  
community stability

# Modelling the dynamics of interaction networks

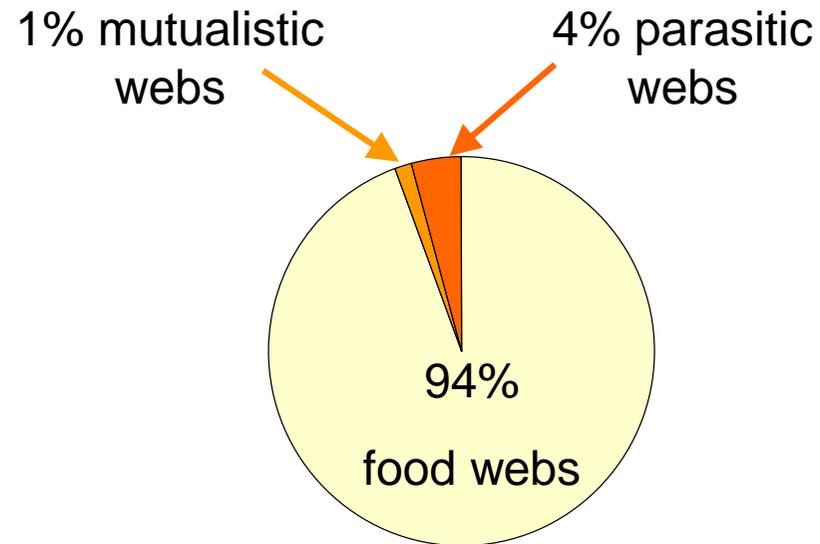


non random  
structural patterns



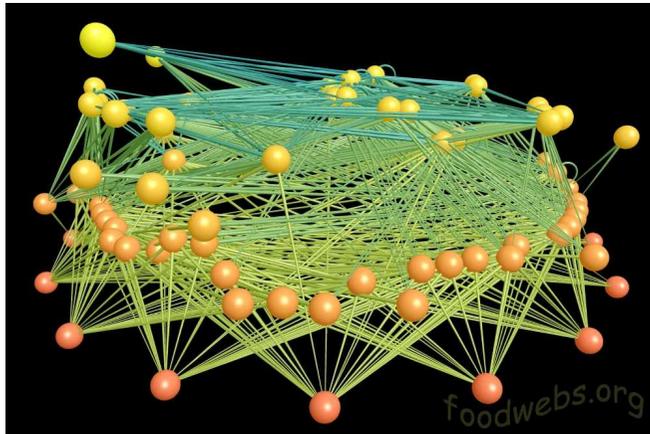
community stability

*... to now*



Proportions of papers on ecological networks published in the last 50 years that were related to food webs, mutualistic webs and parasitic webs

# Modelling the dynamics of interaction networks



non random  
structural patterns



community stability

*... to now*

Food webs →

Large number of  
analyses of food  
web models

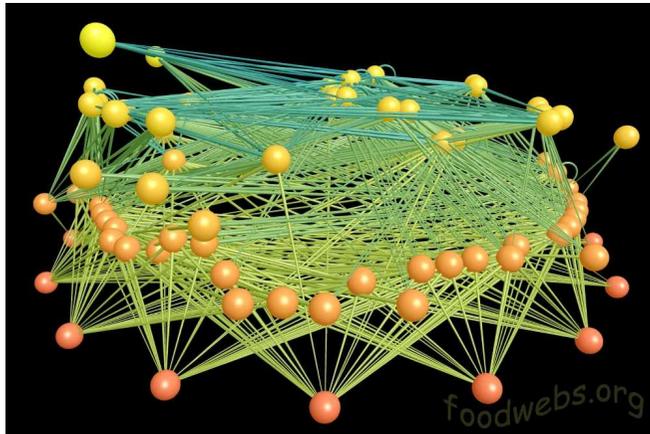
Mutualistic webs →

Only a few recent  
works

Host-parasite & host-  
parasitoid webs →

No models  
at network  
level?

# Modelling the dynamics of interaction networks

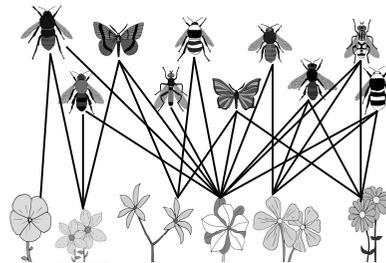


non random  
structural patterns

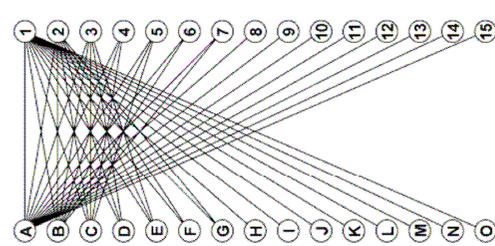
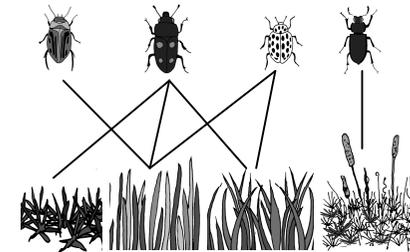


community stability

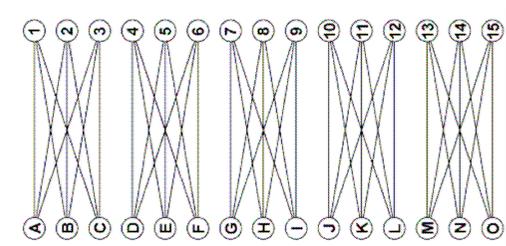
Mutualistic



Trophic

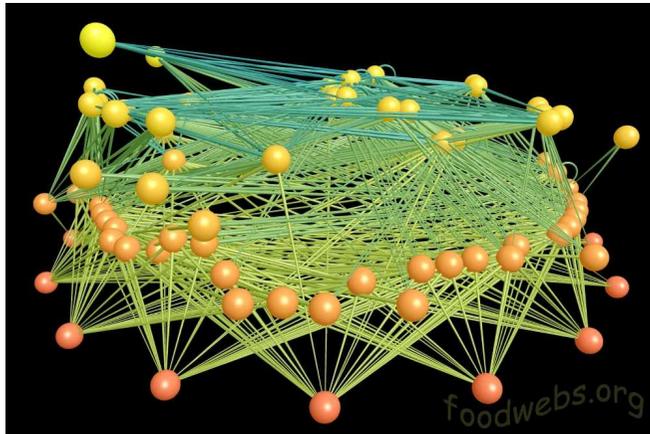


nested



compartmented

# Modelling the dynamics of interaction networks

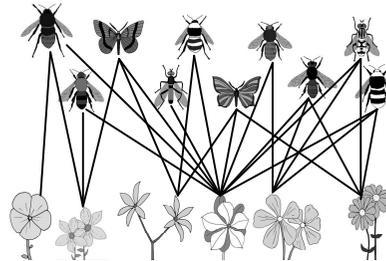


non random  
structural patterns

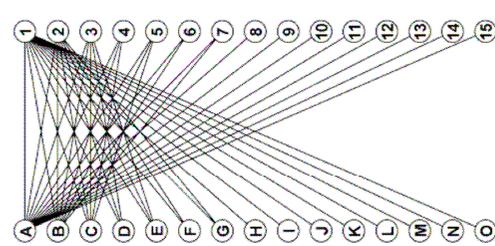
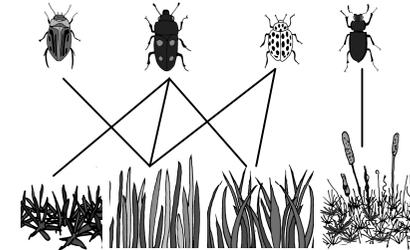


community stability

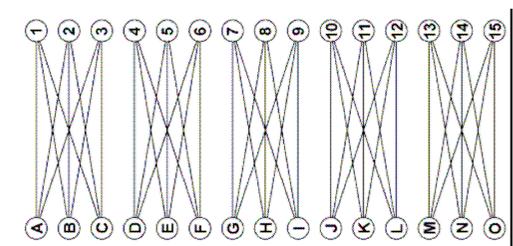
Mutualistic



Trophic



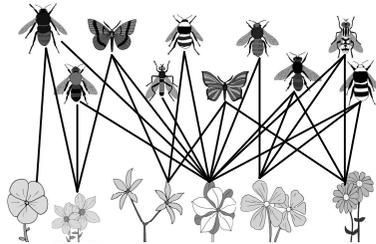
nested



compartmented

How these different structures affect species coexistence and stability in both networks?

# The model: dynamics of mutualistic and trophic webs

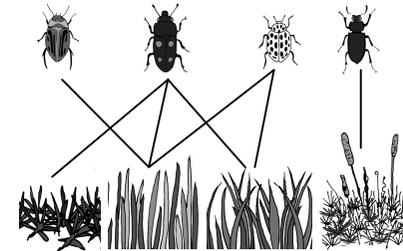


Mutualistic

$$\frac{dA_i}{dt} = r_{A_i} A_i - I_{A_i} A_i^2 + \sum_{j=1}^{N_p} \frac{c_{ji} A_i P_j}{\alpha_{ji}^{-1} + \sum_{P_k \in \text{mut}(A_i)} P_k}$$

$$\frac{dP_i}{dt} = r_{P_i} P_i - I_{P_i} P_i^2 + \sum_{j=1}^{N_a} \frac{c_{ij} A_j P_i}{\alpha_{ij}^{-1} + \sum_{A_k \in \text{mut}(P_i)} A_k}$$

-intrinsic growth rates  
 $r_P$  and  $r_A < 0 \rightarrow$  obligate mutualism



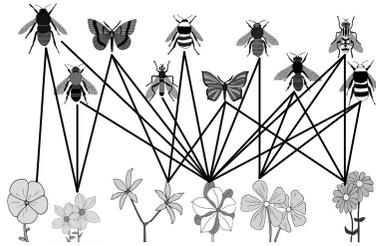
Trophic

$$\frac{dA_i}{dt} = r_{A_i} A_i - I_{A_i} A_i^2 + \sum_{j=1}^{N_p} \frac{c_{ji} A_i P_j}{\alpha_{ji}^{-1} + \sum_{P_k \in \text{prey}(A_i)} P_k}$$

$$\frac{dP_i}{dt} = r_{P_i} P_i - I_{P_i} P_i^2 - \sum_{j=1}^{N_a} \frac{c_{ij} A_j P_i}{\alpha_{ij}^{-1} + \sum_{P_k \in \text{prey}(A_j)} P_k}$$

-intrinsic growth rates  
 $r_P > 0$  and  $r_A < 0$

# The model: dynamics of mutualistic and trophic webs

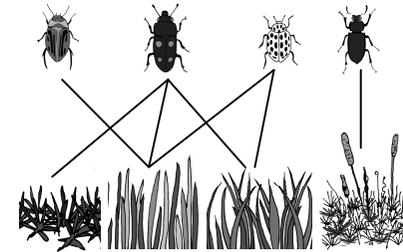


Mutualistic

$$\frac{dA_i}{dt} = \underbrace{r_{A_i} A_i}_{\text{blue}} - \underbrace{A_i^2}_{\text{green}} + \sum_{j=1}^{N_p} \frac{c_{ji} A_i P_j}{\alpha_{ji}^{-1} + \sum_{P_k \in \text{mut}(A_i)} P_k}$$

$$\frac{dP_i}{dt} = \underbrace{r_{P_i} P_i}_{\text{blue}} - \underbrace{P_i^2}_{\text{green}} + \sum_{j=1}^{N_a} \frac{c_{ij} A_j P_i}{\alpha_{ij}^{-1} + \sum_{A_k \in \text{mut}(P_i)} A_k}$$

- intrinsic growth rates  
 $r_P$  and  $r_A < 0 \rightarrow$  obligate mutualism
- density dependence term



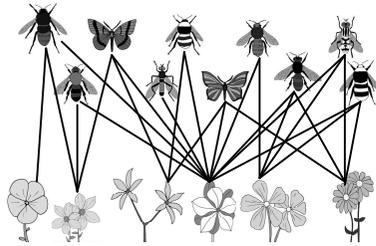
Trophic

$$\frac{dA_i}{dt} = \underbrace{r_{A_i} A_i}_{\text{blue}} - \underbrace{A_i^2}_{\text{green}} + \sum_{j=1}^{N_p} \frac{c_{ji} A_i P_j}{\alpha_{ji}^{-1} + \sum_{P_k \in \text{prey}(A_i)} P_k}$$

$$\frac{dP_i}{dt} = \underbrace{r_{P_i} P_i}_{\text{blue}} - \underbrace{P_i^2}_{\text{green}} - \sum_{j=1}^{N_a} \frac{c_{ij} A_j P_i}{\alpha_{ij}^{-1} + \sum_{P_k \in \text{prey}(A_j)} P_k}$$

- intrinsic growth rates  
 $r_P > 0$  and  $r_A < 0$
- density dependence term

# The model: dynamics of mutualistic and trophic webs

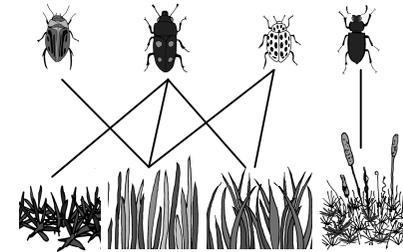


Mutualistic

$$\frac{dA_i}{dt} = r_A A_i - I_{AA} A_i^2 + \frac{\sum_{j=1}^{M_A} c_{ij} A_j P_j}{1 + \alpha_{ij} + \sum_{k=1}^{M_A} P_k} \quad \text{Plus mut}(A_i)$$

$$\frac{dP_i}{dt} = r_P P_i - I_{PP} P_i^2 + \frac{\sum_{j=1}^{M_A} c_{ji} A_j P_j}{1 + \alpha_{ji} + \sum_{k=1}^{M_A} A_k} \quad \text{Plus mut}(P_i)$$

- intrinsic growth rates  
 $r_P$  and  $r_A < 0 \rightarrow$  obligate mutualism
- density dependence term
- interaction term  
saturates with mutualistic partner densities



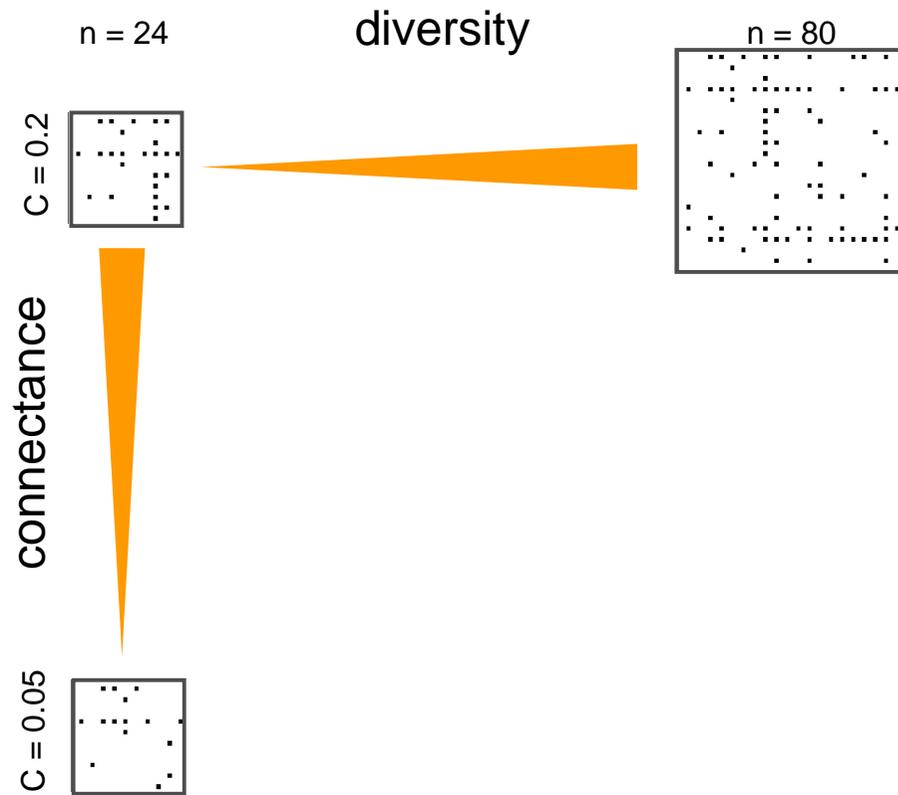
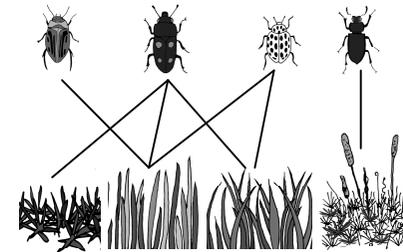
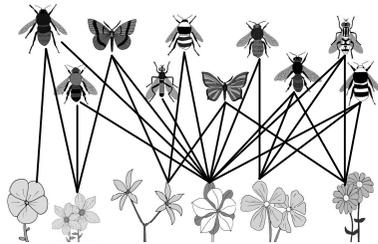
Trophic

$$\frac{dA_i}{dt} = r_A A_i - I_{AA} A_i^2 + \frac{\sum_{j=1}^{M_A} c_{ij} A_j P_j}{1 + \alpha_{ij} + \sum_{k=1}^{M_A} P_k} \quad \text{Plus prey}(A_i)$$

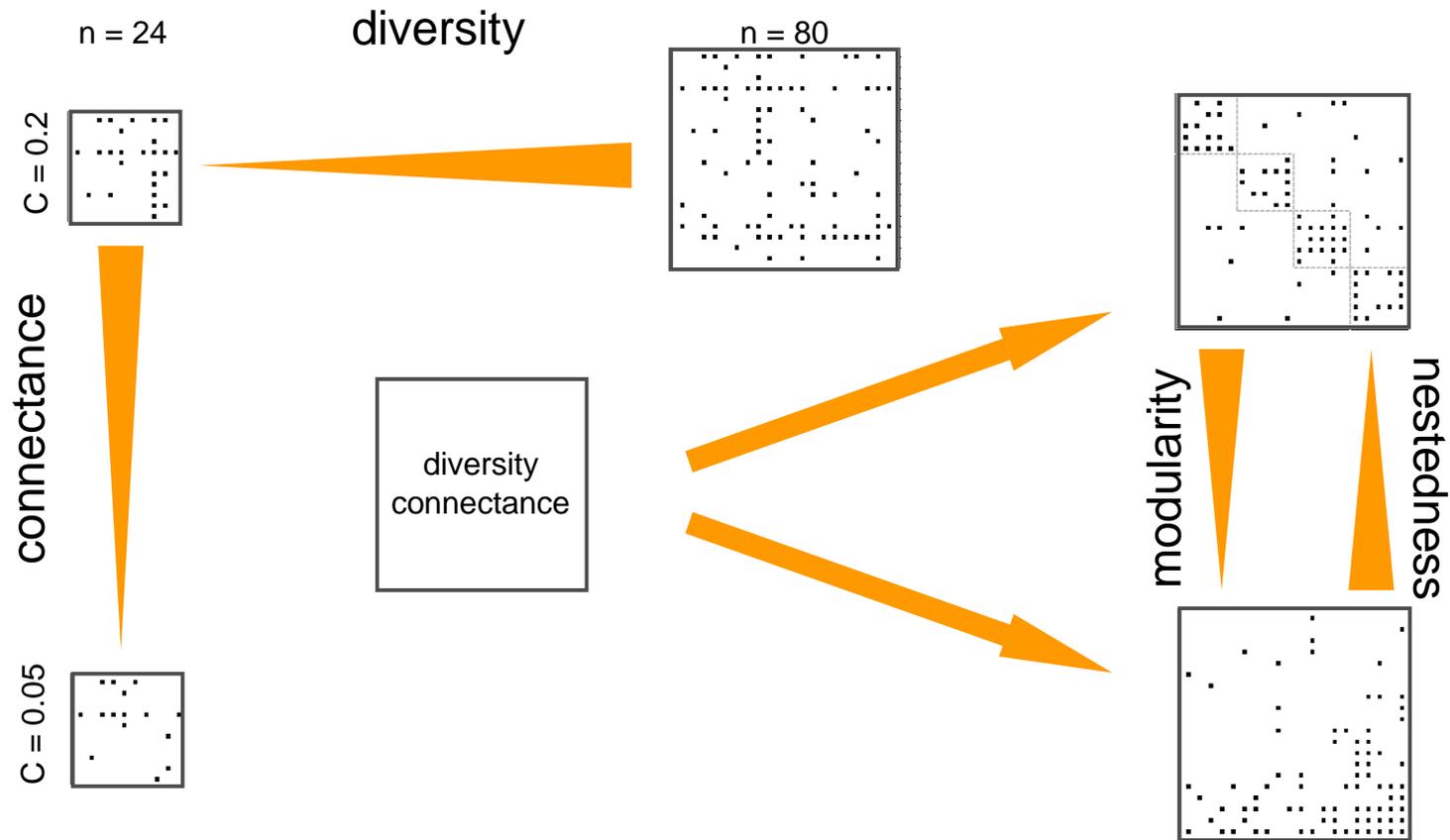
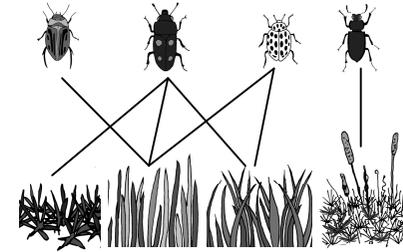
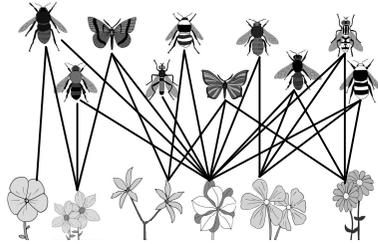
$$\frac{dP_i}{dt} = r_P P_i - I_{PP} P_i^2 - \frac{\sum_{j=1}^{M_A} c_{ji} A_j P_j}{1 + \alpha_{ji} + \sum_{k=1}^{M_A} A_k} \quad \text{Plus prey}(P_i)$$

- intrinsic growth rates  
 $r_P > 0$  and  $r_A < 0$
- density dependence term
- interaction term  
saturates with prey densities

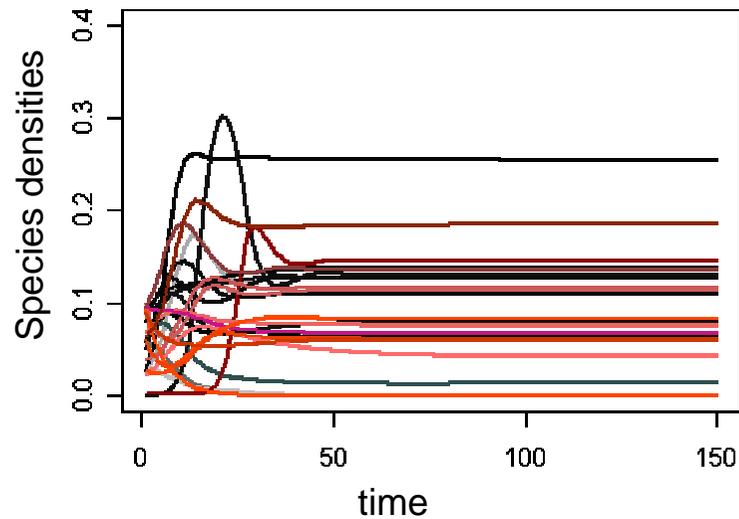
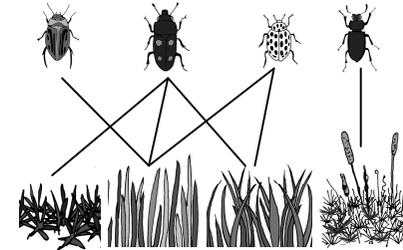
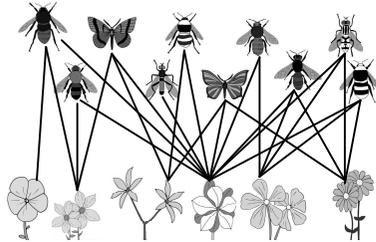
# The model: network structure



# The model: network structure



# The model: stability measurements



➤ Persistence:

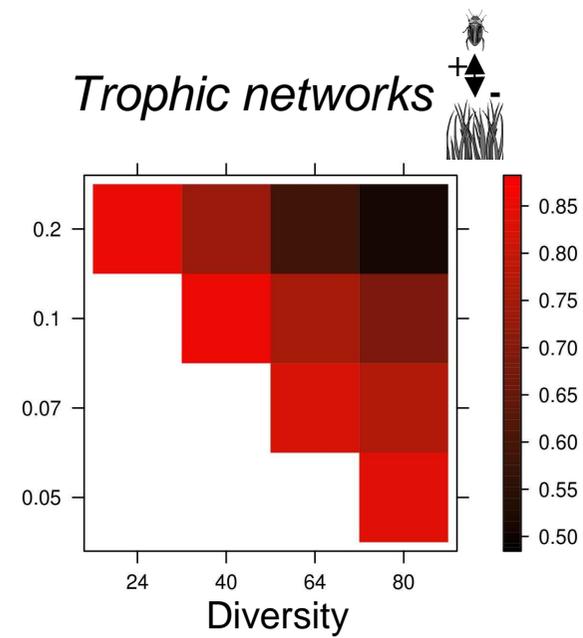
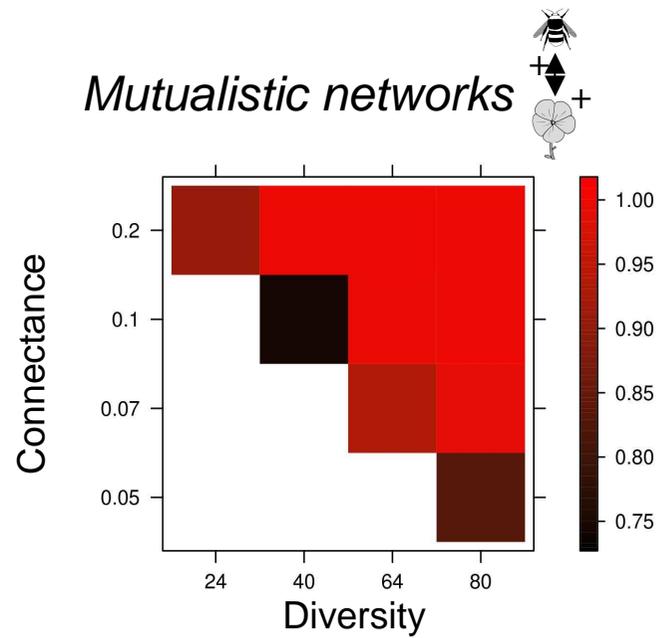
*proportion of species persisting at equilibrium*

➤ Resilience:

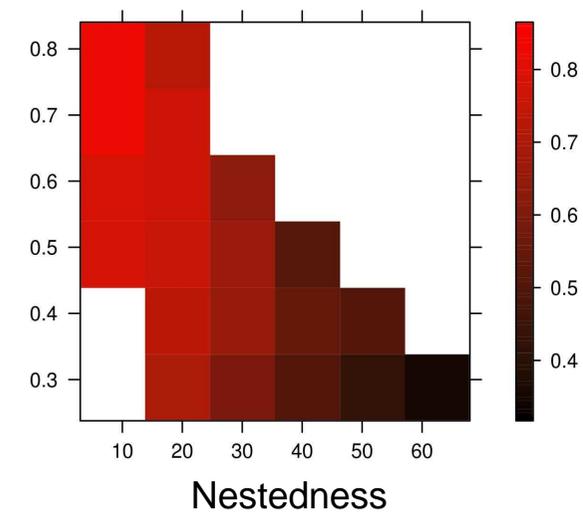
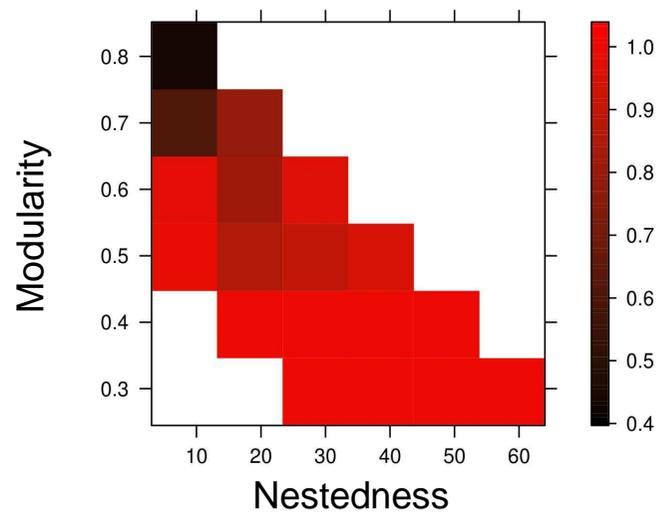
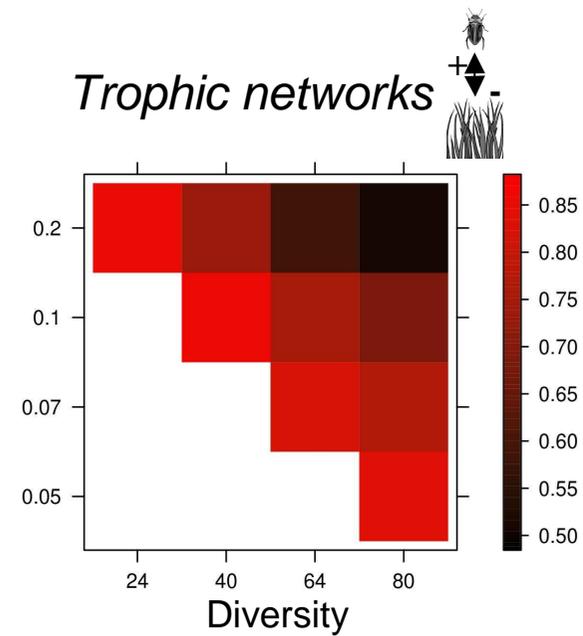
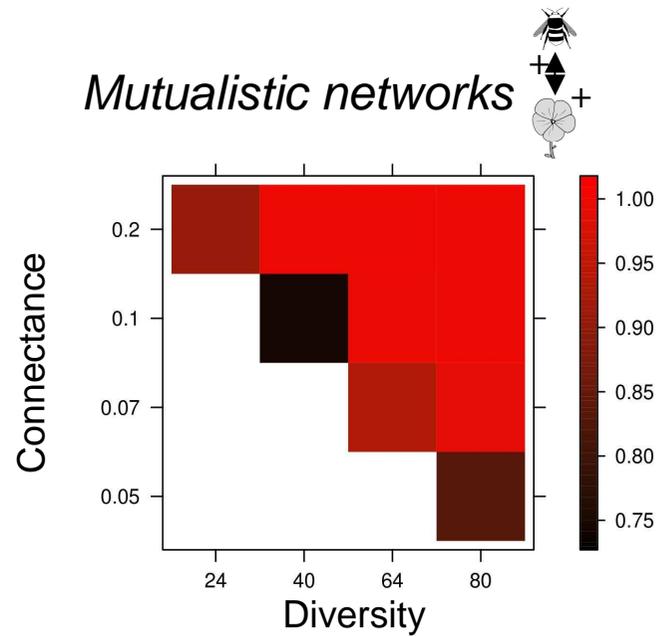
*measure of the speed at which a system returns to its original state after a perturbation*

Evaluated by the absolute value of the dominant eigenvalue of the Jacobian matrix of the system at equilibrium

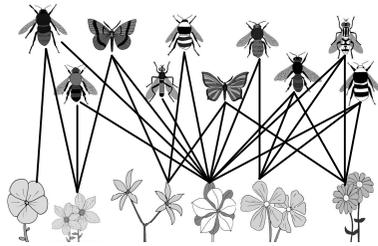
# Results: impact of network structure on persistence



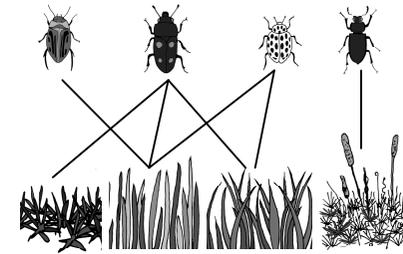
# Results: impact of network structure on persistence



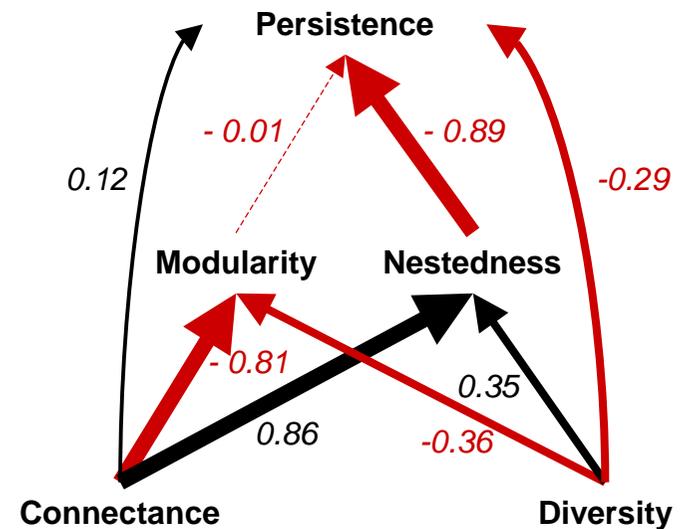
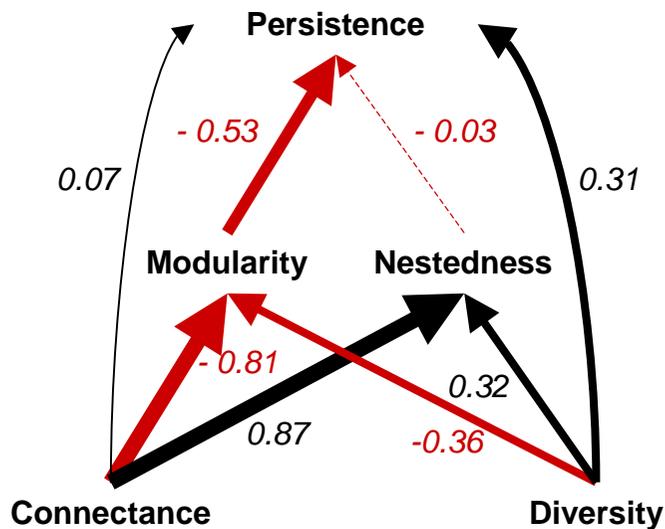
# Results: impact of network structure on persistence



Mutualistic

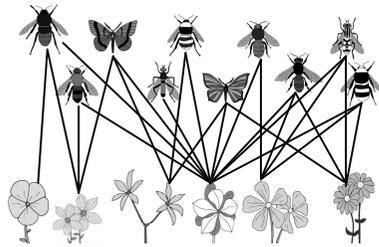


Trophic

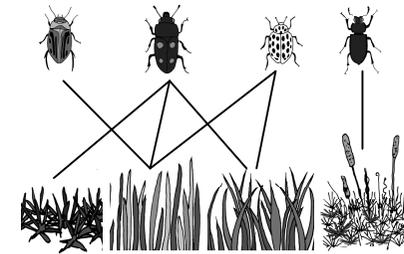


- opposite effect of network structure on the persistence of mutualistic and trophic networks

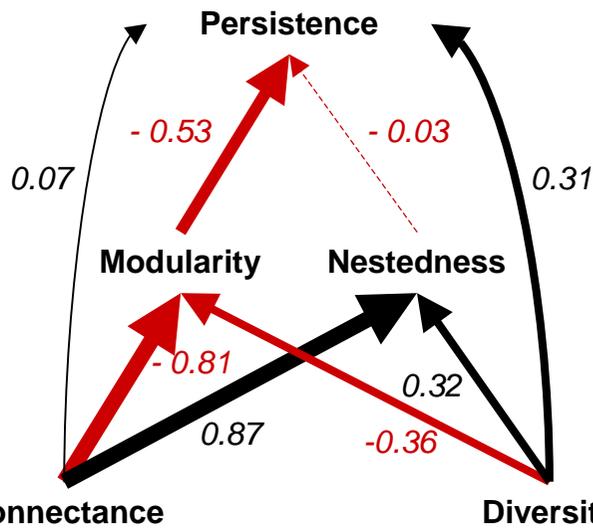
# Results: impact of network structure on persistence



Mutualistic

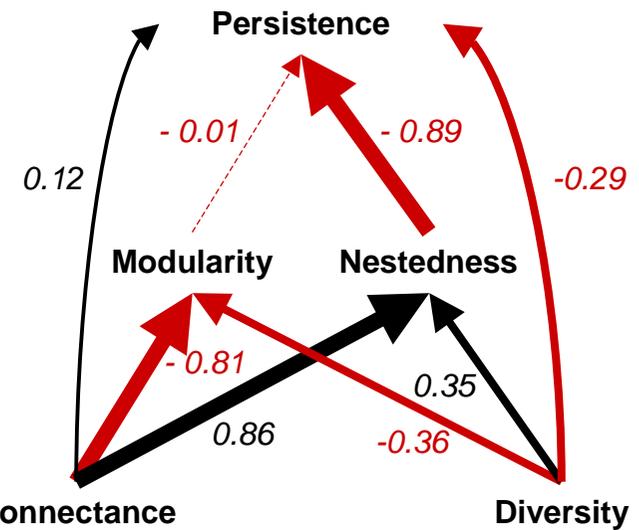


Trophic



indirect effect: 0.40

indirect effect: 0.18

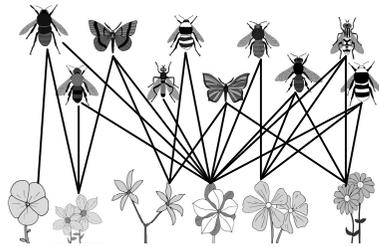


indirect effect: -0.76

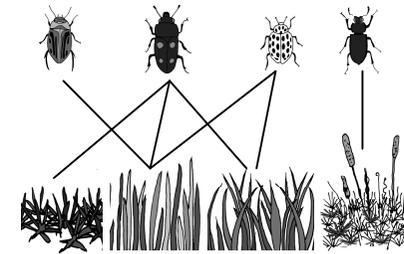
indirect effect: -0.31

➤ Importance of nestedness and modularity for network stability

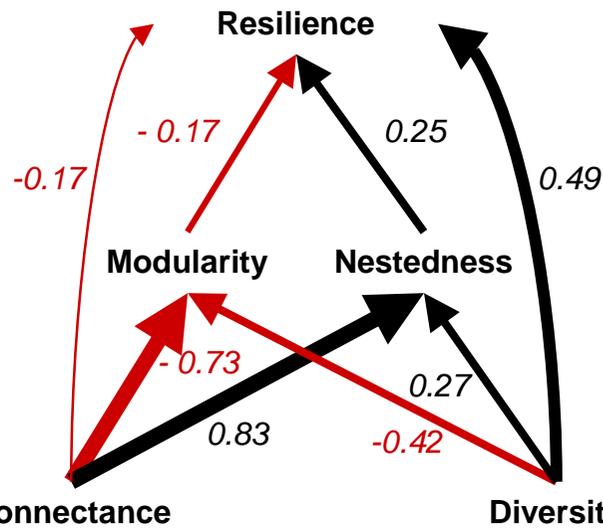
# Results: impact of network structure on resilience



Mutualistic



Trophic

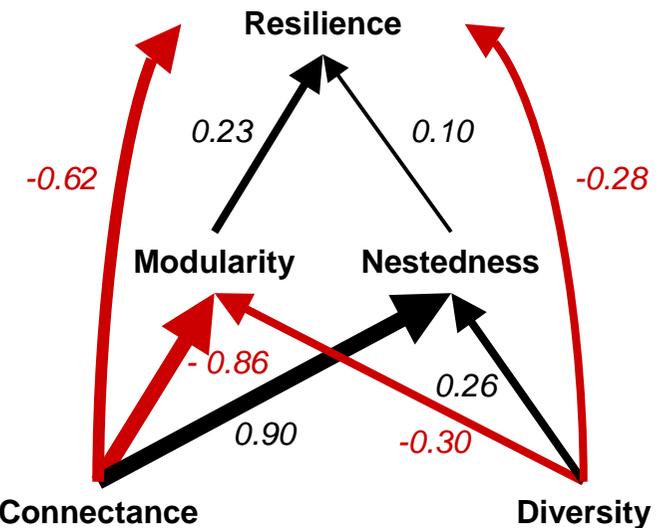


Connectance

Diversity

indirect effect: 0.32

indirect effect: 0.13



Connectance

Diversity

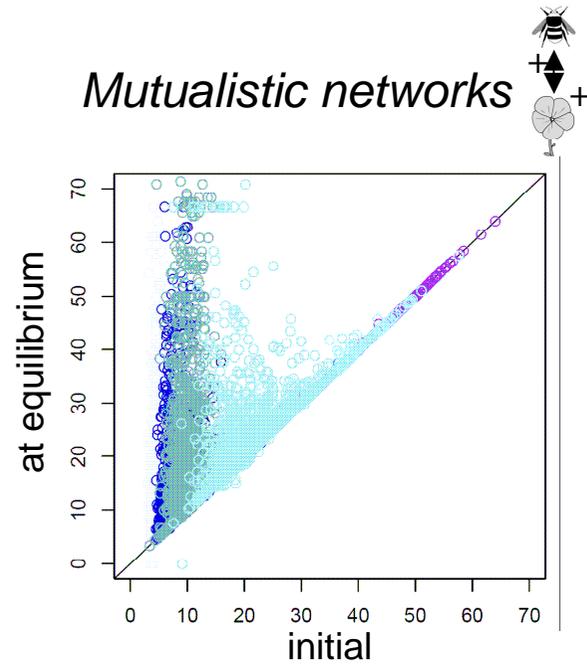
indirect effect: -0.10

indirect effect: -0.04

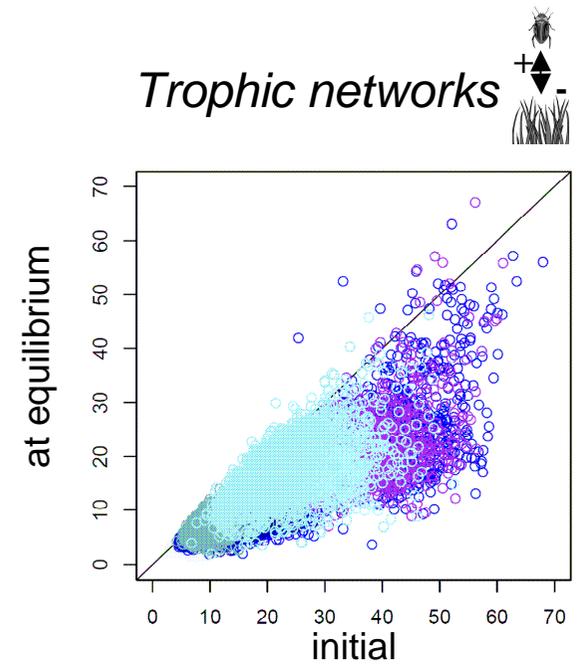
➤ opposite effect of network structure on the resilience of mutualistic and trophic networks

# Results: network structure at equilibrium

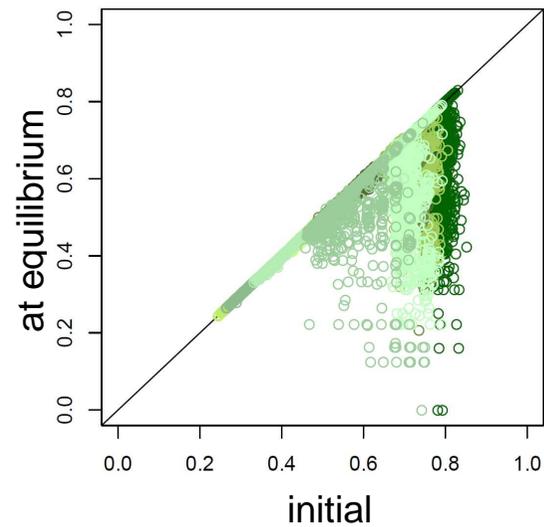
**Nestedness**



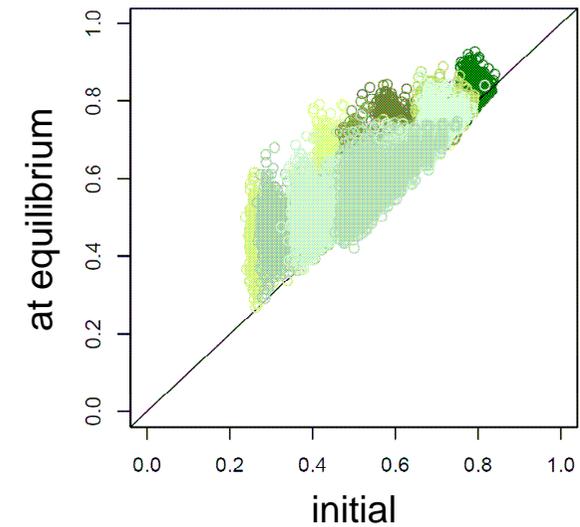
**Nestedness**



**Modularity**

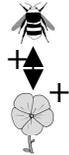


**Modularity**



# Conclusions and Perspectives

*Mutualistic networks*



*Trophic networks*



Strong effects of network structure on community stability  
that differ between interaction types

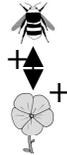
- Connectance and diversity promote stability
- Modularity has a destabilizing effect

- Connectance and diversity have destabilizing effects
- Nestedness has a destabilizing effect

Importance of the fine architecture of interaction networks in  
determining their stability

# Conclusions and Perspectives

*Mutualistic networks*



*Trophic networks*



Strong effects of network structure on community stability  
that differ between interaction types

- Connectance and diversity promote stability
- Modularity has a destabilizing effect
- Connectance and diversity have destabilizing effects
- Nestedness has a destabilizing effect

Importance of the fine architecture of interaction networks in  
determining their stability

Although different, the architectures of mutualistic and trophic  
networks both promote stability

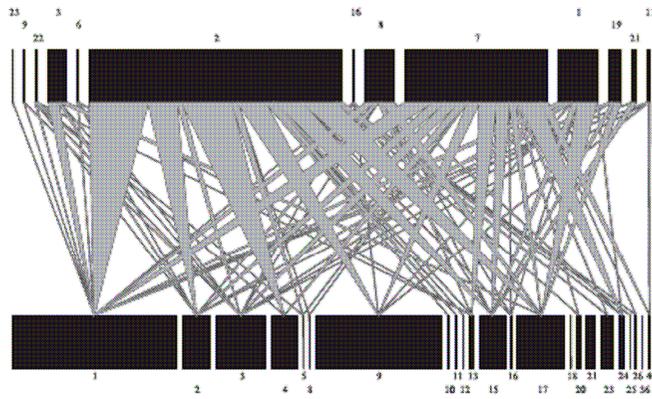
# Conclusions and Perspectives

- Comparison between networks of different interaction types offers promising approaches to understand the response of communities to disturbances

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- Comparison between networks of different interaction types offers promising approaches to understand the response of communities to disturbances

*Impact of interaction intimacy?*

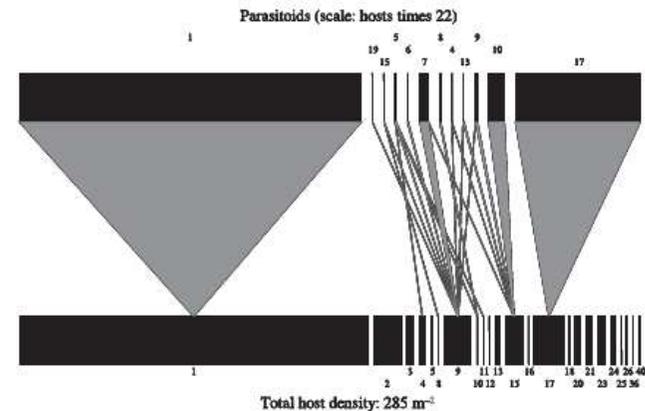


Van Veen et al. 2008

interactions during a short time scale

predator-prey  
pollination

interaction intimacy



interaction during all or part of the life with the same individual

host-parasite  
mycorrhizae

# Conclusions and Perspectives

- Comparison between networks of different interaction types offers promising approaches to understand the response of communities to disturbances

*Impact of interaction intimacy?*

effects of network  
structure on community  
stability that depend on  
interaction intimacy?

# Conclusions and Perspectives

- Comparison between networks of different interaction types offers promising approaches to understand the response of communities to disturbances

*Impact of interaction intimacy?*

effects of network structure on community stability that depend on interaction intimacy?

		Effect of species $j$ on $i$ (i.e., sign of $a_{ij}$ )		
		+	0	-
Effect of species $i$ on $j$ (i.e., sign of $a_{ji}$ )	+	++	+0	+-
	0	0+	00	0-
	-	-+	-0	--

Apart from complete independence, there are five distinguishably different categories of interaction between any given pair of species, namely commensalism (+0), amensalism (-0) mutualism or symbiosis (++) , competition (--) , and general predator-prey (+-) including plant-herbivore, parasite-host, and so on. .

May 1973

# Conclusions and Perspectives

- Comparison between networks of different interaction types offers promising approaches to understand the response of communities to disturbances

*Impact of interaction intimacy?*

effects of network structure on community stability that depend on interaction intimacy?

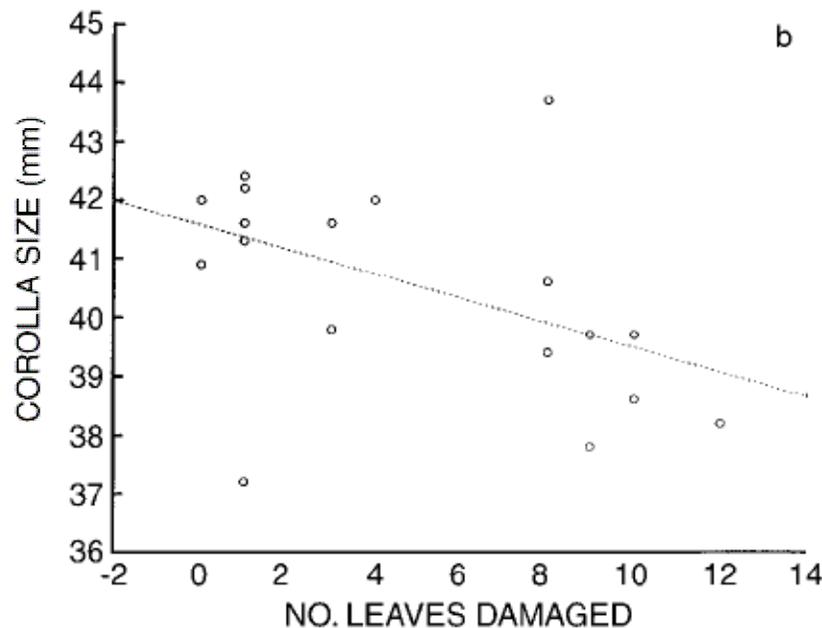
Model different life stages:

- free-living stage
- parasite within hosts

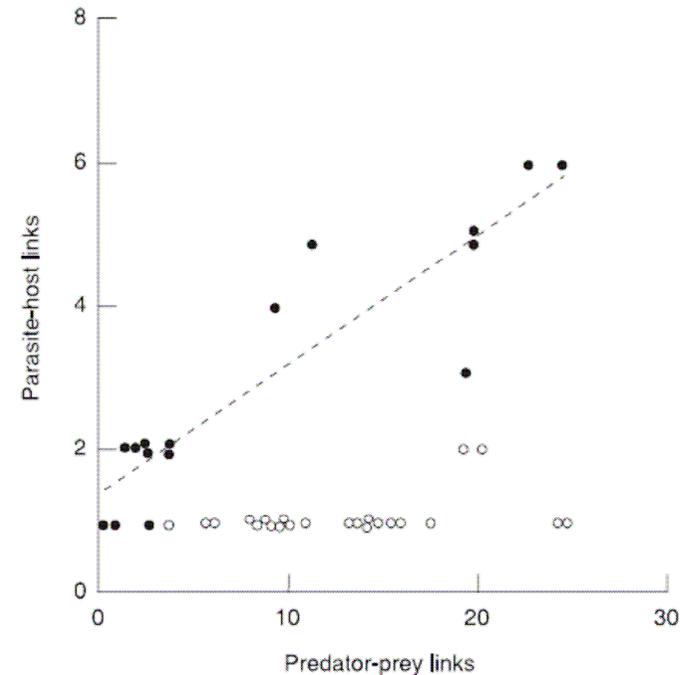
Anderson and May 1978

# Conclusions and Perspectives

- Comparison between networks of different interaction types offers promising approaches to understand the response of communities to disturbances
- Consequences of combining different types of interactions in ecological networks



Strauss 1997



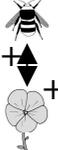
Amundsen et al. 2009

# Conclusions and Perspectives

- Comparison between networks of different interaction types offers promising approaches to understand the response of communities to disturbances
- Consequences of combining different types of interactions in ecological networks
- Importance of evolutionary processes

*Different coevolutionary mechanisms?*

(Thompson 2005, Bascompte et al. 2006)

*Mutualistic networks* 

- complementarity and convergence of traits in interacting species.
- importance of flower morphology on the structure of plant-pollinator networks

*Trophic networks* 

- coevolution of defences and counter defences between interacting species.
- importance of chemical compounds on plant – insect herbivores interaction

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Mutualistic interactions

Trophic interactions

**Thank you for your attention**

