# Introduction to Optimization 

September 18, 2017<br>TC2 - Optimisation<br>Université Paris-Saclay, Orsay, France

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## What is Optimization?



## What is Optimization?

Typically, we aim at

- finding solutions $x$ which minimize $f(x)$ in the shortest time possible (maximization is reformulated as minimization)
- or finding solutions $x$ with as small $f(x)$ in the shortest time possible (if finding the exact optimum is not possible)


## Course Overview

| Date | Topic |
| :--- | :--- |
| Mon, 18.9.2017 | Introduction and Group Project |
| Wed, 20.9.2017 | Benchmarking with the COCO Platform (Group Project) |
| Fri, 22.9.2017 | Introduction to Continuous Optimization |
| Fri, 29.9.2017 | Gradient-Based Algorithms |
| Fri, 6.10.2017 | Stochastic Algorithms and Derivative-free Optimization |
| Fri, 13.10.2017 | Graph Theory, Greedy Algorithms and Dynamic <br> programming |
| Fri, 20.10.2017 | Dynamic Programming, Branch and Bound and Heuristics |
| vacation | Exam |
| Fri, 10.11.2017 | Exal |

## all classes + exam are from 14h till 17h15 (incl. a 15min break) here in D101 (except for E210 this Wednesday)

- possibly not clear yet what the lecture is about in detail
- but there will be always examples and small exercises to learn "on-the-fly" the concepts and fundamentals


## Overall goals:

(1) give a broad overview of where and how optimization is used
(2) understand the fundamental concepts of optimization algorithms
(3) be able to apply common optimization algorithms on real-life (engineering) problems

## The Exam

- open book: take as much material as you want
- (most likely) multiple-choice
- Friday, $10^{\text {th }}$ of November 2017
- counts $2 / 3$ of overall grade


## Group Project (aka "contrôle continu")

- we will have one group project with 4-5 students per group
- counts as $1 / 3$ of overall grade
- the basic ideas: each group...
- reads a scientific paper about an optimization algorithm
- implements this algorithm
- connects it to the benchmarking platform COCO
- runs the algorithm with COCO to produce benchmarking data
- compares their algorithm with others


## Group Project: Grading

- counts as $1 / 3$ of overall grade
- grading mainly based on
- a technical report (10 pages) to be handed in by October 21
- an oral (group) presentation in the week November 7-11
- grading partly based on
- each student's contribution to the group (via a written document to be signed by each student)
- the online documentation (in a provided wiki)
- the submitted source code
- the timely submission of all required documents


## looks a lot ;-)

but: important to go out of your comfort zone to learn!

## Course Overview

| 1 | Mon, 18.9.2017 | today's lecture: more infos in the end <br> Tue, 19.9.2017 |
| :--- | :--- | :--- |
| groups defined via wiki |  |  |
| everybody went (actively!) through the Getting Started part of |  |  |
| github.com/numbbo/coco |  |  |
| lecture "Benchmarking", final adjustments of groups |  |  |
| everybody can run and postprocess the example experiment (~1h for |  |  |
| final questions/help during the lecture) |  |  |
| lecture "Introduction to Continuous Optimization" |  |  |$|$

## Group Project (aka "contrôle continu")

- more detailed information in the end of today's lecture

All information also available at
http://www.cmap.polytechnique.fr/
~dimo.brockhoff/optimizationSaclay/2017/
(group project info + link to wiki, lecture slides, ...)

## Advertisement: Master's Thesis Topics

## RandOpt team

Cinría Inria and Ecole Polytechnique

Permanent members:
Anne Auger, Dimo Brockhoff, Nikolaus Hansen https://team.inria.fr/randopt/team-members/

Master's theses available (PhD theses possible):

- start anytime
- 6 months
- paid via Inria
- many topics around blackbox optimization
- theory $\leftrightarrow$ algorithm design

| constrained |  |
| :---: | :---: |
| large-scale multiobjective |  |
| CMA-ES |  |
| theory |  |
| blackbox |  |
| optimization |  | expensive algorithm design benchmarking http://randopt.gforge.inria.fr/thesisprojects/

## Overview of Today's Lecture

- More examples of optimization problems
- introduce some basic concepts of optimization problems such as domain, constraint, ...
- Beginning of continuous optimization part
- typical difficulties in continuous optimization
- basics of benchmarking blackbox optimization algorithms with the COCO platform
- basics needed for group project (more on Wednesday)


## General Context Optimization

Given:
set of possible solutions

## Search space

quality criterion
Objective function
Objective:
Find the best possible solution for the given criterion

## Formally:

Maximize or minimize

$$
\begin{aligned}
\mathcal{F}: \Omega & \mapsto \mathbb{R} \\
x & \mapsto \mathcal{F}(x)
\end{aligned}
$$



## Constraints

Maximize or minimize

$$
\begin{aligned}
\mathcal{F}: \Omega & \mapsto \mathbb{R}, \\
x & \mapsto \mathcal{F}(x)
\end{aligned}
$$

unconstrained
$\Omega$

Maximize or minimize

$$
\mathcal{F}: \Omega \mapsto \mathbb{R}
$$

$$
x \mapsto \mathcal{F}(x)
$$

$$
\text { where } \quad g_{i}(x) \leq 0
$$

$$
h_{j}(x)=0
$$

example of a constrained $\Omega$

Constraints explicitely or implicitely define the feasible solution set [e.g. $\|x\|-7 \leq 0$ vs. every solution should have at least 5 zero entries]

Hard constraints must be satisfied while soft constraints are preferred to hold but are not required to be satisfied
[e.g. constraints related to manufactoring precisions vs. cost constraints]

## Example 1: Combinatorial Optimization

## Knapsack Problem

- Given a set of objects with a given weight and value (profit)
- Find a subset of objects whose overall mass is below a certain limit and maximizing the total value of the objects
[Problem of ressource allocation with financial constraints]


$$
\begin{array}{ll}
\max . & \sum_{j=1}^{n} p_{j} x_{j} \text { with } x_{j} \in\{0,1\} \\
& \text { s.t. } \sum_{j=1}^{n} w_{j} x_{j} \leq W
\end{array}
$$

$\Omega=\{0,1\}^{n}$

## Example 2: Combinatorial Optimization

## Traveling Salesperson Problem (TSP)

- Given a set of cities and their distances
- Find the shortest path going through all cities


$$
\Omega=S_{n}(\text { set of all permutations })
$$

## Example 3: Continuous Optimization

A farmer has 500 m of fence to fence off a rectangular field that is adjacent to a river. What is the maximal area he can fence off?


## Exercise:

a) what is the search space?
b) what is the objective function?

## Example 3: Continuous Optimization

A farmer has 500 m of fence to fence off a rectangular field that is adjacent to a river. What is the maximal area he can fence off?

solution can be found analytically:
exercise for the weekend ;-)

$$
\begin{gathered}
\Omega=\mathbb{R}_{+}^{2}: \\
\max x y \\
\text { where } x+2 y \leq 500
\end{gathered}
$$

## Example 4: A "Manual" Engineering Problem

Optimizing a Two-Phase Nozzle [Schwefel 1968+]

- maximize thrust under constant starting conditions
- one of the first examples of Evolution Strategies
initial design:

final design:

$\Omega=$ all possible nozzles of given number of slices

> copyright Hans-Paul Schwefel [http://ls11-www.cs.uni-dortmund.de/people/schwefel/EADemos/]

## Example 5: Continuous Optimization Problem

Computer simulation teaches itself to walk upright (virtual robots (of different shapes) learning to walk, through stochastic optimization (CMA-ES)), by Utrecht University:

We present a control system based on 3D muscle actuation

https://www.youtube.com/watch?v=yci5Ful1ovk
T. Geitjtenbeek, M. Van de Panne, F. Van der Stappen: "Flexible Muscle-Based Locomotion for Bipedal Creatures", SIGGRAPH Asia, 2013.

## Example 6: Constrained Continuous Optimization

## Design of a Launcher


$\Omega=\mathbb{R}^{23}$


- Scenario: multi-stage launcher brings a satellite into orbit
- Minimize the overall cost of a launch
- Parameters: propellant mass of each stage / diameter of each stage / flux of each engine / parameters of the command law

23 continuous parameters to optimize

+ constraints


## Example 7: An Expensive Real-World Problem

Well Placement Problem


for a given structure, per well:

- angle \& distance to previous well
- well depth
structure $+\mathbb{R}_{+}^{3} \cdot \#$ wells
$\sigma \in \Omega$ : variable length!


## Example 8: Data Fitting - Data Calibration

## Objective

- Given a sequence of data points $\left(\boldsymbol{x}_{i}, y_{i}\right) \in \mathbb{R}^{p} \times \mathbb{R}, i=1, \ldots, N$, find a model " $y=f(\boldsymbol{x})$ " that "explains" the data experimental measurements in biology, chemistry, ...
- In general, choice of a parametric model or family of functions $\left(f_{\theta}\right)_{\theta \in \mathbb{R}^{n}}$
use of expertise for choosing model or only a simple model is affordable (e.g. linear, quadratic)
- Try to find the parameter $\theta \in \mathbb{R}^{n}$ fitting best to the data

Fitting best to the data
Minimize the quadratic error:

$$
\min _{\theta \in \mathbb{R}^{n}} \sum_{i=1}^{N}\left|f_{\theta}\left(\boldsymbol{x}_{i}\right)-y_{i}\right|^{2}
$$

## Example 9: Lin. Regression in Machine Learning

## Supervised Learning:

Predict $y \in \mathcal{Y}$ from $\boldsymbol{x} \in \mathcal{X}$, given a set of observations (examples) $\left\{y_{i}, \boldsymbol{x}_{i}\right\}_{i=1, \ldots, N}$
(Simple) Linear regression where all the $y_{i}$ and $x_{i}$ are from $\mathbb{R}$ Given a set of data: $\{y_{i}, \underbrace{x_{i}^{1}, \ldots, x_{i}^{p}}_{\boldsymbol{x}_{i}^{T}}\}_{i=1 \ldots N}$

$$
\min _{\boldsymbol{w} \in \mathbb{R}^{p}, \beta \in \mathbb{R}} \underbrace{\sum_{i \widetilde{\boldsymbol{w}}-\boldsymbol{y} \|^{2}}^{N}\left|\boldsymbol{w}^{T} \boldsymbol{x}_{i}+\beta-y_{i}\right|^{2}}_{\| \widetilde{i=1}}
$$

same as data fitting with linear model, i.e. $f_{(w, \beta)}(\boldsymbol{x})=\boldsymbol{w}^{T} \boldsymbol{x}+\beta$, $\theta \in \mathbb{R}^{p+1}$

## Example 10: Deep Learning

## Actually the same idea:

 match model best to given dataModel here:
artificial neural nets with many hidden layers (aka deep neural networks)

## Parameters to tune:



- weights of the connections (continuous parameter)
- topology of the network (discrete)
- firing function (less common)


## Example 11: Interactive Optimization

## Coffee Tasting Problem

- Find a mixture of coffee in order to keep the coffee taste from one year to another
- Objective function = opinion of one expert

M. Herdy: "Evolution Strategies with subjective selection", 1996


## Many Problems, Many Algorithms?

## Observation:

- Many problems with different properties
- For each, it seems a different algorithm?


## In Practice:

- often most important to categorize your problem first in order to find / develop the right method
- $\rightarrow$ problem types

Algorithm design is an art, what is needed is skill, intuition, luck, experience, special knowledge and craft
freely translated and adapted from Ingo Wegener (1950-2008)

## Problem Types

- discrete vs. continuous
- discrete: integer (linear) programming vs. combinatorial problems
- continuous: linear, quadratic, smooth/nonsmooth, blackbox/DFO, ...
- both discrete\&continuous variables: mixed integer problem
- unconstrained vs. constrained (and then which type of constraint)
- one or multiple objective functions

Not covered in this introductory lecture:

- deterministic vs. stochastic outcome of objective function(s)


## Example: Numerical Blackbox Optimization

Typical scenario in the continuous, unconstrained case:

Optimize $f: \Omega \subset \mathbb{R}^{n} \mapsto \mathbb{R}^{k}$

derivatives not available or not useful

## General Concepts in Optimization

- search domain
- discrete vs. continuous variables vs. mixed integer
- finite vs. infinite dimension
- constraints
- bound constraints (on the variables only)
- linear/quadratic/non-linear constraints
- blackbox constraints
- many more
(see e.g. Le Digabel and Wild (2015), https://arxiv.org/abs/1505.07881)

Further important aspects (in practice):

- deterministic vs. stochastic algorithms
- exact vs. approximation algorithms vs. heuristics
- anytime algorithms
- simulation-based optimization problem / expensive problem


## continuous optimization

## Continuous Optimization

- Optimize $f:\left\{\begin{array}{c}\Omega \subset \mathbb{R}^{n} \rightarrow \mathbb{R} \\ x=\left(x_{1}, \ldots, x_{n}\right) \rightarrow f\left(x_{1}, \ldots, x_{n}\right)\end{array}\right.$
unconstrained optimization
- Search space is continuous, i.e. composed of real vectors $x \in \mathbb{R}^{n}$
- $n=\left\{\begin{array}{l}\text { dimension of the problem } \\ \text { dimension of the search space } \mathbb{R}^{n} \text { (as vector space) }\end{array}\right.$


2-D level sets


## Unconstrained vs. Constrained Optimization

## Unconstrained optimization

$$
\inf \left\{f(x) \mid x \in \mathbb{R}^{n}\right\}
$$

## Constrained optimization

- Equality constraints: $\inf \left\{f(x) \mid x \in \mathbb{R}^{n}, g_{k}(x)=0,1 \leq k \leq p\right\}$
- Inequality constraints: $\inf \left\{f(x) \mid x \in \mathbb{R}^{n}, g_{k}(x) \leq 0,1 \leq k \leq p\right\}$
where always $g_{k}: \mathbb{R}^{n} \rightarrow \mathbb{R}$


## Example of a Constraint

$\min _{x \in \mathbb{R}} f(x)=x^{2}$ such that $x \leq-1$


## Analytical Functions

## Example: 1-D

$$
\begin{gathered}
f_{1}(x)=a\left(x-x_{0}\right)^{2}+b \\
\text { where } x, x_{0}, b \in \mathbb{R}, a \in \mathbb{R}
\end{gathered}
$$

## Generalization:

 convex quadratic function$$
\begin{aligned}
& \qquad f_{2}(x)=\left(x-x_{0}\right)^{T} A\left(x-x_{0}\right)+b \\
& \text { where } x, x_{0}, b \in \mathbb{R}^{n}, A \in \mathbb{R}^{\{n \times n\}} \\
& \text { and } A \text { symmetric positive definite (SPD) }
\end{aligned}
$$

## Exercise:

What is the minimum of $f_{2}(x)$ ?

## Levels Sets of Convex Quadratic Functions

## Continuation of exercise: What are the level sets of $f_{2}$ ?

Reminder: level sets of a function

$$
L_{c}=\left\{x \in \mathbb{R}^{n} \mid f(x)=c\right\}
$$

(similar to topography lines / level sets on a map)


## Levels Sets of Convex Quadratic Functions

## Continuation of exercise:

What are the level sets of $f_{2}$ ?

- Probably too complicated in general, thus an example here
- Consider $A=\left(\begin{array}{ll}9 & 0 \\ 0 & 1\end{array}\right), b=0, n=2$
a) Compute $f_{2}(x)$.
b) Plot the level sets of $f_{2}(x)$.
c) More generally, for $n=2$, if $A$ is SPD with eigenvalues $\lambda_{1}=$ 9 and $\lambda_{2}=1$, what are the level sets of $f_{2}(x)$ ?


## What Makes a Function Difficult to Solve?

- dimensionality
(considerably) larger than three
- non-separability dependencies between the objective variables
- ill-conditioning
- ruggedness

cut from 3D example, solvable with an evolution strategy


## Curse of Dimensionality

- The term Curse of dimensionality (Richard Bellman) refers to problems caused by the rapid increase in volume associated with adding extra dimensions to a (mathematical) space.
- Example: Consider placing 100 points onto a real interval, say $[0,1]$. To get similar coverage, in terms of distance between adjacent points, of the 10 -dimensional space $[0,1]^{10}$ would require $100^{10}=10^{20}$ points. The original 100 points appear now as isolated points in a vast empty space.
- Consequently, a search policy (e.g. exhaustive search) that is valuable in small dimensions might be useless in moderate or large dimensional search spaces.


## Separable Problems

## Definition (Separable Problem)

A function $f$ is separable if

$$
\underset{\left(x_{1}, \ldots, x_{n}\right)}{\operatorname{argmin}} f\left(x_{1}, \ldots, x_{n}\right)=\left(\underset{x_{1}}{\operatorname{argmin}} f\left(x_{1}, \ldots\right), \ldots, \underset{x_{n}}{\operatorname{argmin}} f\left(\ldots, x_{n}\right)\right)
$$

$\Rightarrow$ it follows that $f$ can be optimized in a sequence of $n$ independent 1-D optimization processes

## Example:

Additively decomposable functions

$$
f\left(x_{1}, \ldots, x_{n}\right)=\sum_{\substack{i=1 \\ \text { Rastrigin function }}}^{n} f_{i}\left(x_{i}\right)
$$



## Non-Separable Problems

## Building a non-separable problem from a separable one [1,2]

## Rotating the coordinate system

- $f: x \mapsto f(x)$ separable
- $f: \boldsymbol{x} \mapsto f(R \boldsymbol{x})$ non-separable


## $R$ rotation matrix


[1] N. Hansen, A. Ostermeier, A. Gawelczyk (1995). "On the adaptation of arbitrary normal mutation distributions in evolution strategies: The generating set adaptation". Sixth ICGA, pp. 57-64, Morgan Kaufmann
[2] R. Salomon (1996). "Reevaluating Genetic Algorithm Performance under Coordinate Rotation of Benchmark Functions; A survey of some theoretical and practical aspects of genetic algorithms." BioSystems, 39(3):263-278

## III-Conditioned Problems: Curvature of Level Sets

Consider the convex-quadratic function

$$
f(\boldsymbol{x})=\frac{1}{2}\left(\boldsymbol{x}-\boldsymbol{x}^{*}\right)^{T} H\left(\boldsymbol{x}-\boldsymbol{x}^{*}\right)=\frac{1}{2} \sum_{i} h_{i, i} x_{i}^{2}+\frac{1}{2} \sum_{i, j} h_{i, j} x_{i} x_{j}
$$

H is Hessian matrix of $f$ and symmetric positive definite


> gradient direction $-f^{\prime}(x)^{T}$
> Newton direction $-H^{-1} f^{\prime}(x)^{T}$

III-conditioning means squeezed level sets (high curvature). Condition number equals nine here. Condition numbers up to $10^{10}$ are not unusual in real-world problems.

If $H \approx I$ (small condition number of $H$ ) first order information (e.g. the gradient) is sufficient. Otherwise second order information (estimation of $H^{-1}$ ) information necessary.

## Different Notions of Optimum

## Unconstrained case

- local vs. global
- local minimum $x^{*}$ : $\exists$ a neighborhood $V$ of $x^{*}$ such that $\forall x \in \mathrm{~V}: f(\boldsymbol{x}) \geq f\left(\boldsymbol{x}^{*}\right)$
- global minimum: $\forall x \in \Omega: f(x) \geq f\left(x^{*}\right)$
- strict local minimum if the inequality is strict


## Constrained case

- a bit more involved
- hence, later in the lecture :


## Blackbox optimization benchmarking

...and some more details on the group project

## Numerical Blackbox Optimization

Optimize $f: \Omega \subset \mathbb{R}^{n} \mapsto \mathbb{R}^{k}$


## derivatives not available or not useful

## Not clear:

which of the many algorithms should I use on my problem?

## Numerical Blackbox Optimizers

Deterministic algorithms
Quasi-Newton with estimation of gradient (BFGS) [Broyden et al. 1970]
Simplex downhill [Nelder \& Mead 1965]
Pattern search [Hooke and Jeeves 1961]
Trust-region methods (NEWUOA, BOBYQA) [Powell 2006, 2009]
Stochastic (randomized) search methods
Evolutionary Algorithms (continuous domain)

- Differential Evolution [Storn \& Price 1997]
- Particle Swarm Optimization [Kennedy \& Eberhart 1995]
- Evolution Strategies, CMA-ES
[Rechenberg 1965, Hansen \& Ostermeier 2001]
- Estimation of Distribution Algorithms (EDAs)
[Larrañaga, Lozano, 2002]
- Cross Entropy Method (same as EDA) [Rubinstein, Kroese, 2004]
- Genetic Algorithms [Holland 1975, Goldberg 1989]

Simulated annealing [Kirkpatrick et al. 1983]
Simultaneous perturbation stochastic approx. (SPSA) [Spall 2000]

## Numerical Blackbox Optimizers

## Deterministic algorithms

Quasi-Newton with estimation of gradient (BFGS) [Broyden et al. 1970]
Simplex downhill [Nelder \& Mead 1965]
Pattern search [Hooke and Jeeves 1961]
Trust-reaion methods (NEWUOA. BOBYQA) IPowell 2006. 20091
choice typically not immediately clear although practitioners have knowledge about which difficulties their problem has (e.g. multi-modality, non-separability, ...)

- ᄃVUIULIUI DIIategies, LiviA-CD
[Rechenberg 1965, Hansen \& Ostermeier 2001]
- Estimation of Distribution Algorithms (EDAs)
[Larrañaga, Lozano, 2002]
- Cross Entropy Method (same as EDA) [Rubinstein, Kroese, 2004]
- Genetic Algorithms [Holland 1975, Goldberg 1989]

Simulated annealing [Kirkpatrick et al. 1983]
Simultaneous perturbation stochastic approx. (SPSA) [Spall 2000]

## Need: Benchmarking

- understanding of algorithms
- algorithm selection
- putting algorithms to a standardized test
- simplify judgement
- simplify comparison
- regression test under algorithm changes

Kind of everybody has to do it (and it is tedious):

- choosing (and implementing) problems, performance measures, visualization, stat. tests, ...
- running a set of algorithms


## that's where COCO comes into play

Comparing Continuous Optimizers Platform
https://github. com/numbbo/coco

## automatized benchmarking

## How to benchmark algorithms with COCO?

## https://github.com/numbbo/coco



## https：／／github．com／numbbo／coco

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Numerical Black－Box Optimization Benchmarking Framework http：／／coco．gforge．inria．fr／
Add topics
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\(\bigcirc 31\) releases
215 contributors


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raising an error in bbob2009＿logger．c when best＿value is NULL．Plus s．．．
small correction in AUTHORS
Update LICENSE
Added link to \＃1335 before closing．
refactoring here and there in do．py to get closer to PEP8 specifications
moved all files into code－experiments／folder besides the do．py scrip．．．
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https：／／github．com／numbbo／coco．git 睺
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F．code－preprocessing
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目 LICENSE
目 README．md
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Fixed preprocessing to work correctly with the extended biobjectiv Update create－a－suite－howto．md

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## 国 README．md

## numbbo／coco：Comparing Continuous Optimizers

This code reimplements the original Comparing Continous Optimizer platform，now rewritten fully in ANSI C with other languages calling the C code．As the name suggests，the code provides a platform to benchmark and compare continuous optimizers，AKA non－linear solvers for numerical optimization．Languages currently available are
－C／C＋＋
－Java
－matlab／Octave

## https：／／github．com／numbbo／coco

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－C／C＋＋
－Java
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－Python
Contributions to link further languages（including a better example in $\mathrm{C}_{++}$）are more than welcome．

For more information，
－read our benchmarking guidelines introduction
－read the COCO experimental setup description

## https://github.com/numbbo/coco

## numbbo/coco: Comparing Continuous Optimizers

This code reimplements the original Comparing Continous Optimizer platform, now rewritten fully in ANSI C with other languages calling the c code. As the name suggests, the code provides a platform to benchmark and compare continuous optimizers, AKA non-linear solvers for numerical optimization. Languages currently available are

- C/C++
- Java
- MATLAB/Octave
- Python

Contributions to IInk further languages (including a better example in $\mathrm{C}_{++}$) are more than welcome.
For more information,

- read our benchmarking guidelines introduction
- read the COCO experimental setup description
- see the bbob-biobj and bbob-biobj-ext COCO multi-objective functions testbed documentation and the specificities of the performance assessment for the bi-objective testbeds.
- consult the BBOB workshops series,
- consider to register here for news,
- see the previous COCO home page here and
- see the links below to learn more about the ideas behind CoCO.


## https：／／github．com／numbbo／coco

## Gettina Started

0 ．Check out the Requirements above．

## requirements \＆download

－either by clicking the Download ZIP button and unzip the zip file，
－or by typing git clone https：／／github．com／numbbo／coco．git．This way allows to remain up－to－date easily（but needs git to be installed）．After cloning，git pull keeps the code up－to－date with the latest release．

The record of official releases can be found here．The latest release corresponds to the master branch as linked above．
2．In a system shell，cd into the coco or coco－＜version＞folder（framework root），where the file do．py can be found． Type，i．e．execute，one of the following commands once
python do．py run－c
python do．py run－java
python do．py run－matlab
python do．py run－octave
python do．py run－python
depending on which language shall be used to run the experiments．run－＊will build the respective code and run the example experiment once．The build result and the example experiment code can be found under code－experiments／build ／＜language＞（＜language＞＝matlab for Octave）．python do．py lists all available commands．

3．On the computer where experiment data shall be post－processed，run

## https://github.com/numbbo/coco

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## Getting Started

0 . Check out the Requirements above.

1. Download the COCO framework code from github,

- either by clicking the Download ZIP button and unzip the zip file,
- or by typing git clone https://github.com/numbbo/coco.git. This way allows to remain up-to-date easily (but needs git to be installed). After cloning, git pull keeps the code up-to-date with the latest release.

The record of official releases can be found here. The latest release corresponds to the master branch as linked above.
2. In a system shell, cd into the coco or coco-<version> folder (framework root), where the file do.py can be found. Type, i.e. execute, one of the following com
python do.py run-c
python do.py run-java
installation l: experiments
python do.py run-matlab
python do.py run-python
depending on which language shall be used to run the experiments. run-* will build the respective code and run the example experiment once. The build result and the example experiment code can be found under code-experiments/build /<language> (<language>=matlab for Octave). python do.py lists all available commands.
3. On the computer where experiment data shall be post-processed, run

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3．On the computer where experiment data shall b
python do．py install－postprocessing

## installation II：postprocessing

to（user－locally）install the post－processing．From here on，do．py nas donentsjow and is oniy needearagantor upaating the builds to a new release．

4．Copy the folder code－experiments／build／YOUR－FAVORITE－LANGUAGE and its content to another location．In Python it is sufficient to copy the file example＿experiment．py．Run the example experiment（it already is compiled）．As the details vary，see the respective read－me＇s and／or example experiment files：
－c read me and example experiment
－Java read me and example experiment
－Matlab／Octave read me and example experiment
－Python read me and example experiment
If the example experiment runs，connect your favorite algorithm to Coco：replace the call to the random search optimizer in the example experiment file by a call to your algorithm（see above）．Update the output result＿folder，the algorithm＿name and algorithm＿info of the observer options in the example experiment file．

Another entry point for your own experiments can be the code－experiments／examples folder．
5．Now you can run your favorite algorithm on the bbob suite（for single－objective algorithms）or on the bbob－biobj and bbob－biobj－ext suites（for multi－objective algorithms）．Output is automatically generated in the specified data result＿folder．By now，more suites might be available，see below．

## https：／／github．com／numbbo／coco

2）Most Visited Getting Started coco－Algorithms numbbo／numbbo．Gi．．．GandOpt CMAP Inria GitLab RER B from lab example experıment once．The buld result and the example experıment code can be tound under code－experiments／build ／＜language＞（＜language＞＝matlab for Octave）．python do．py lists all available commands．

3．On the computer where experiment data shall be post－processed，run

```
python do.py install-postprocessing
```

to（user－locally）install the post－processing．From here on，do．py has done its job and is only needed again for updating the builds to a new release．

4．Copy the folder code－experiments／build／YOUR－FAVORITE－LANGUAGE and its content to another location．In Python it is sufficient to copy the file example＿experiment．py ．Run the example experiment（it already is compiled）．As the details vary，see the respective read－me＇s and／or example experiment files：
－c read me and example experiment
－Java read me and example experiment
－Matlab／Octave read me and example experiment

## coupling algo＋COCO

－Python read me and example experiment
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## Simplified Example Experiment in Python

```
import cocoex
import scipy.optimize
### input
suite_name = "bbob"
output_folder = "scipy-optimize-fmin"
fmin = scipy.optimize.fmin
### prepare
suite = cocoex.Suite(suite_name, "", "")
observer = cocoex.Observer(suite_name,
"result_folder: " + output_folder)
```

\#\#\# go
for problem in suite: \# this loop will take several minutes
problem.observe_with(observer) \# generates the data for
\# cocopp post-processing
fmin (problem, problem.initial_solution)

Note: the actual example_experiment.py contains more advanced things like restarts, batch experiments, other algorithms (e.g. CMA-ES), etc.

## https：／／github．com／numbbo／coco

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6．Postprocess the data from the results folder by typing
python－m cocopp［－o OUTPUT＿FOLDERNAME］YOURDA

## running the experiment

Any subfolder in the folder arguments will be searched fo different folders collected under a single＂root＂YOURDATAFOLDER folder．We can also compare more than one algorithm by specifying several data result folders generated by different algorithms．

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# tip： <br> start with small \＃funevals（until bugs fixed ©） then increase budget to get a feeling how long a＂long run＂will take 

8．The experiments can be parallelized with any re－distribution of single problem instances to batches（see example＿experiment．py for an example）．Each batch must write in a different target folder（this should happen automatically）．Results of each batch must be kept under their separate folder as is．These folders then must be

## https：／／github．com／numbbo／coco

numbbo／coco at develop．．．$\times$
（i）GitHub，Inc．（US）https：／／github．com／numbbo／coco／tree／development
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6．Postprocess the data from the results folder by typing
python－m cocopp［－o OUTPUT＿FOLDERNAME］YOURDATAFOLDER［MORE＿DATAFOLDERS］

Any subfolder in the folder arguments will be searched for logged data．That is，experiments from different batches can be in different folders collected under a single＂root＂Yourdatafolder specifying several data result folders generated by different algc

A folder，ppdata by default，will be generated，which contains

## postprocessing

file，useful as main entry point to explore the result with a brows
the output folder name with the－o OUTPUT＿FOLDERNAME option．
A summary pdf can be produced via LaTeX．The corresponding templates can be found in the code－postprocessing／latex－
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exalmpre exper миеті automatically）．Results of each batch must be kept under their separate folder as is．These folders then must be

## Result Folder



## Automatically Generated Results



Single algorithm data
BIPOP-CMA-ES hansen noiseless

## Automatically Generated Results

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## BIPOP-CMA-ES

## Home

Runtime distributions (ECDFs) per function
Runtime distributions (ECDFs) summary and function groups
Scaling with dimension for selected targets
Tables for selected targets
Runtime distribution for selected targets and f-distributions
Runtime loss ratios
Runtime distributions (ECDFs) over all targets


## Automatically Generated Results

- (i) file:///C:/Users/dimo/Desktop/coco/BBOB/data-archive/data/gecco-bbob-1-24/2009.

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## Overview page

Runtime distributions (ECDFs) per function


## Automatically Generated Results



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## Overview page

Average number of $f$-evaluations to reach target


# doesn't look too complicated, does it? 

[the devil is in the details $\odot$ ]

## Course Overview

| 1 | Mon, 18.9.2017 <br> Tue, 19.9.2017 | today's lecture: more infos in the end <br> groups defined via wiki <br> everybody went (actively!) through the Getting Started part of github.com/numbbo/coco |
| :---: | :---: | :---: |
| 2 | Wed, 20.9.2017 | lecture "Benchmarking", final adjustments of groups everybody can run and postprocess the example experiment ( $\sim 1 \mathrm{~h}$ for final questions/help during the lecture) |
| 3 | Fri, 22.9.2017 | lecture "Introduction to Continuous Optimization" |
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| 6 | Fri, 13.10.2017 | lecture "Discrete Optimization I: graphs, greedy algos, dyn. progr." deadline for submitting data sets |
| 7 | Wed, 18.10.2017 <br> Fri, 20.10.2017 | deadline for paper submission <br> final lecture "Discrete Optimization II: dyn. progr., B\&B, heuristics" |
|  | Thu, 26.10.2017/ Fri, 27.10.2017 | oral presentations (individual time slots) |
|  | after 30.10.2017 | vacation aka learning for the exams |
|  | Fri, 10.11.2017 | written exam All deadlines: |
|  |  | 23:59pm Paris time |

## Group Project: Remark

## both report and talk should be in English [at the time being, THE scientific language]

## Group Project Wiki

## http://randopt.gforge.inria.fr/teaching/optimization-Saclay/groupproject2017/



Trace: $\cdot$ rules $\cdot$ papers $\cdot$ groups $\cdot$ presentations $\cdot$ faq $\cdot$ start

## Welcome to the web page of the Optimization Group Project

This is the web page of the group project of the Introduction to Optimization lecture, given in September-November 2017 by Dimo Brockhoff at the Univesity Paris-Saclay.

It will be the main source for any information on the group project, be it the rules, the produced data, the submitted papers, or the documentation of each group.

Enjoy your work with this DokuWiki,

- Dimo Brockhoff
start.txt • Last modified: 2017/08/30 18:18 by admin


## Group Project Wiki

- to be found at
- http://randopt.gforge.inria.fr/teaching/optimizationSaclay/groupproject2017/
- also via a link on the home page
- please use this to interact within the groups
- document what you do
- document who is doing what
- document what still needs to be done
- and coordinate the assignments of all of you to groups with paper/algorithm and programming language (by tomorrow!)
- 6 algorithms available
- 0,1 , or 2 groups per algorithm
- if 2 groups: choose different programming language! easiest: choose among python, C/C++, Java, Matlab/Octave


## Group Project: Recommendations

- Do not start working last minute.

Understanding an algorithm, implementing and testing it always takes time.

- Get an overview of what COCO is and does by reading the General Introduction to COCO and the documents on performance assessment with COCO to get an idea of how to read the main plots.
- Consider using a version control system for your code (and potentially for your final report and slides as well).

Github/Gitlab might come in handy

- Test your software extensively. Optimally, write (unit) tests before the actual code.
- Again: run (very) short experiments first, then increase budget.


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## Conclusions

I hope it became clear...
...what kind of optimization problems we are interested in
...what are the requirements for the group project and the exam
...and what are the next important steps to do:
by tomorrow: build the groups and decide on an algorithm by Wednesday:

- go through the "Getting Started" of COCO
- collect the things that don't work (concrete questions)

