## Reinforcement Learning Reinforcement Learning: Prediction and Planning in the Tabular Setting

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## RL: What Are We Going To See?





## Outline

- Operations Research and MDP.
- Reinforcement learning and interactions.
- More tabular reinforcement learning.
- Reinforcement and approximation of value functions.
- Actor/Critic: a Policy Point of View

## Operations Research and MDP





#### How to find the best policy knowing the MDP?

- Is there an optimal policy?
- How to estimate it numerically?
- Finite states/actions space assumption (tabular setting).
- Focus on interative methods using value functions (dynamic programming).
- Policy deduced by a statewise optimization of the value function over the actions.
- Focus on the discounted setting.

## Reinforcement Learning and Interactions





## How to find the best policy not knowing the MDP?

- How to interact with the environment to learn a good policy?
- Can we use a Monte Carlo strategy outside the episodic setting?
- How to update value functions after each interaction?
- Focus on stochastic methods using tabular value functions (*Q* learning, SARSA...)
- Policy deduced by a statewise optimization of the value function over the actions.



- Prediction with Monte Carlo
- 2 Planning with Monte Carlo
- 3 Prediction with Temporal Differencies
- 4 Link with Stochastic Approximation
- 6 Planning with Value Iteration
- 6 Planning with Policy Improvement
- Exploration vs Exploitation

## Reinforcement Learning





#### From Probability to Statistics?

- What to do if one has no knowledge of the underlying MDP?
- Only information through interactions!
- Prediction? Planning?
- Focus on the discounted setting



#### Prediction with Monte Carlo

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Monte Carlo, i.e. Just Play!



• Most simple way to evaluate a policy.

#### Just Play Following Policy $\Pi$

- Play *N* episodes following the policy.
- During each episode, compute the (discounted) gain.
- Compute the average gain.
- What is computed?

Average Gain or Value Function

Prediction with

$$\mathbb{E}[G_0]$$
 vs  $v_{t,\Pi}(s) = \mathbb{E}[G_t|S_t = s]$ 

#### Prediction as Value Function Evaluation

- Not the same goal.
- By construction,

$$\mathbb{E}[G_0] = \sum_{s} \mu_0(s) v_{t,\Pi}(s)$$

- Much easier to compute the average gain than the value function (even if we use a stationary policy)
- Average gain is nevertheless the most classical way to evaluate a policy (with a single number).
- Implicit episodic setting if we do not want to use approximated gain.

## Average Gain Estimation

Prediction with Monte Carlo

#### Episodic: Evaluation by MC

```
input: MDP environment, initial state distribution \mu_0, policy \Pi and discount factor \gamma
parameter: Number of episodes N
init: V = 0, n = 0
repeat
     n \leftarrow n+1
     t \leftarrow 0
     G \leftarrow 0
     Pick initial state S_0 following \mu_0
     repeat
          Pick action A_t according to \pi(\cdot|S_t)
          G \rightarrow G + \gamma^t R_{t+1}
          t \leftarrow t + 1
     until episod ends at time T
     V \leftarrow V + G
until n == N
V \leftarrow V/N
output: Average gain V
```

## Monte Carlo Prediction

Prediction with Monte Carlo

• How to estimate  $v_{t,\Pi}$ ?

#### Just Play Following Policy $\Pi$

- Play N episodes following the policy.
- During episode, record  $S_t$  and  $R_t$ .
- After each episode, compute recursively for each time t the gain  $G_t$ .
- Estimate  $v_{t,\Pi}(s)$  by the average  $G_t$  over all trajectories such that  $S_t = s$
- May require a lot of game to have a non empty set for each state *s* at each time *t*

## Monte Carlo Prediction



• How to estimate  $v_{\Pi}$  for a stationary policy?

#### Just Play Following Policy $\Pi$

- Play *N* episodes following the policy.
- During each episode, record  $S_t$  and  $R_t$ .
- After each episode, compute recursively for each time t the gain  $G_t$ .
- Estimate  $v_{\Pi}(s)$  by the average over all trajectories of all  $G_t$  such that  $S_t = s$ , whatever t.
- The same state may be reached several time during a single episode. . .
- First-visit variant: Use only the first visit of *s* for each episode.

## Monte Carlo Prediction

Prediction with Monte Carlo

## e Carlo

#### Episodic: Prediction by MC

```
input: MDP environment, initial state distribution \mu_0, policy \Pi and discount factor \gamma
parameter: Number of episodes N
init: \forall s, V(s), n = 0, N(s) = 0
repeat
     n \leftarrow n + 1
     t \leftarrow 0
     Pick initial state S_0 following \mu_0
     repeat
          (If First-visit) N(S_t) \leftarrow N(S_t) + 1
          Pick action A_t according to \pi(\cdot|S_t)
          Record R_{t+1}, S_{t+1}
          t \leftarrow t + 1
    until episod ends at time T
     G_{T+1} = 0
     t \rightarrow T + 1
     repeat
          t \leftarrow t - 1
          Compute G_t = R_{t+1} + \gamma G_{t+1}
          (If First-visit) V(S_t) = V(S_t) + G_t
    until t = 0
until n == N
for s \in S do
     V(s) \leftarrow V(s)/N(s)
end
output: Value function V
```



#### First-Visit Variant Analysis

- Straightforward analysis as all the used values for a given state s are independent.
- Variance of order 1/N(s) where N(s) is the number of episod where s is visited.
- $\bullet$  Convergence if the number of visit goes to  $\infty.$
- Strong assumption is practice as some states may not be visited by a given policy (if we cannot play on the initial state).
- Every-visit works. . . but not necessarily better!



### 1 Prediction with Monte Carlo

## Planning with Monte Carlo

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## Monte Carlo Planning



• Can we use a MC approach to find a good policy?

## A First Attempt

- Estimate  $v_{\pi}(s)$  by  $V_{\pi}(s)$  using MC.
- Compute  $Q_{\pi}(s, a) = r(s, a) + \gamma \sum_{s'} p(s'|s, a) V_{\pi}(s)$
- Enhance the current policy by setting  $\pi(s) = \operatorname{argmax}_a Q_{\pi}(s, a)$
- Inspired by the Operations Research results...
- But unusable as r and p are unknown!



## A Second Attempt

- Estimate  $q_{\pi}(s, a)$  by  $Q_{\pi}(s, a)$  using MC.
- Enhance the current policy by setting  $\pi(s) = \operatorname{argmax}_a Q_{\pi}(s, a)$
- Requires that N(s, a) the number of times that an episode contains the state s followed by action a goes to ∞.
- Impossible with a deterministic policy!

## Monte Carlo Planning

Planning with Monte Carlo



#### Classical Exploratory Policies...

- Stochastic policies ensuring that any action can occurs at any state.
- $\epsilon$ -exploratory policy: use a determistic policy and replace it with a random action with probability  $\epsilon$ .
- Gibbs policy: use a policy where  $\pi(a|s) \propto e^{G(a,s)} > 0$ .

## A Final Attempt

- Start from an exploratory policy.
- Estimate  $q_{\pi}(s, a)$  by  $Q_{\pi}(s, a)$  using MC.
- Enhance the current policy while remaining a exploratory policy.
- Last step is not straightforward...
- except for ε-deterministic policy for which the ε-exploratory policy with base policy π(s) = argmax<sub>a</sub> Q<sub>π</sub>(s, a) works.
- No convergence proof.

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Prediction with Temporal Differencies



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## Advanced Implementation of Monte Carlo Prediction

Prediction with Temporal Differencies



## $V_{\pi}(S_t) \leftarrow V_{\pi}(S_t) + \alpha(N(S_t))(G_t - V_{\pi}(S_t))$

#### **On-Line** Monte Carlo

- Average for a given state can be updated each time we have the gain  $G_t$  for a state  $S_t$ .
- Just use  $\alpha(N) = 1/N$  and increment  $N(S_t)$ .
- No need to record the values between episodes...
- We still need to wait until the end of each episode to compute  $G_t$ .
- Can we do better?

## Advanced MC Prediction

Prediction with Temporal Differencies



#### Episodic: Prediction by MC

```
input: MDP environment, initial state distribution \mu_0, policy \Pi and discount factor \gamma
parameter: Number of episodes N
init: \forall s, V(s), n = 0, N(s) = 0
repeat
     n \leftarrow n + 1
     t \leftarrow 0
     Pick initial state S_0 following \mu_0
     repeat
          (If First-visit) N(S_t) \leftarrow N(S_t) + 1
          Pick action A_t according to \pi(\cdot|S_t)
          Record R_{t+1}, S_{t+1}
          t \leftarrow t + 1
     until episod ends at time T
     G_{T+1} = 0
     t \rightarrow T + 1
     repeat
          t \leftarrow t - 1
          Compute G_t = R_{t+1} + \gamma G_{t+1}
          (If First-visit) V(S_t) = V(S_t) + \frac{1}{N(S_t)} (G_t - V(S_t))
     until t = 0
until n = -M
output: Value function V
```

- We still need to wait until the end of each episode to compute  $G_t$ .
- Can we do better?

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## Prediction with Temporal Differencies



From 
$$V_{\pi}(S_t) \leftarrow V_{\pi}(S_t) + \alpha(N(S_t))(G_t - V_{\pi}(S_t))$$
  
to  $V_{\pi}(S_t) \leftarrow V_{\pi}(S_t) + \alpha(N(S_t))\underbrace{(R_{t+1} + \gamma V_{\pi}(S_{t+1}) - V_{\pi}(S_t))}_{\delta_t}$ 

#### Bootstrap Strategy

- Replace  $G_t$  by an instantaneous estimate  $R_{t+1} + \gamma V_{\pi}(S_{t+1})$ .
- Amounts to replace  $\gamma R_{t+2} + \gamma^2 R_{t+1}$  by an approximation of its expectation given  $S_{t+1}$ :  $v_{\pi}(S_{t+1})$ .
- Bootstrap as we use the current estimate  $V_{\pi}(S_{t+1})$  instead of the true value.
- $\delta_t = R_{t+1} + \gamma V_{\pi}(S_{t+1}) V_{\pi}(S_t)$  is called a temporal difference.
- No need to wait until the end of the episodes!
- Can be used in the discounted setting.

## **TD** Prediction

Prediction with Temporal Differencies



#### Discounted: Prediction by TD

```
input: MDP environment, initial state distribution \mu_0, policy \Pi and discount factor \gamma
parameter: Number of step T
init: \forall s, V(s), n = 0, N(s) = 0, t' = 0
repeat
     t \leftarrow 0
     Pick initial state S_0 following \mu_0
    repeat
          N(S_t) \leftarrow N(S_t) + 1
          Pick action A_t according to \pi(\cdot|S_t)
          V(S_t) \leftarrow V(S_t) + \alpha(N(S_t)) \left( R_{t+1} + \gamma V(S_{t+1}) - V(S_t) \right)
          t \leftarrow t + 1
     until episod ends at time T' or t' == T
until t' == T
output: Value function V
```

#### • But does this work?

## Prediction with Temporal Differencies



$$\mathbb{E}[\delta_t|S_t] \mathbb{E}[R_{t+1} + \gamma V_{\pi}(S_{t+1}) - V_{\pi}(S_t)|S_t] = (\mathcal{T}^{\pi} - \mathrm{Id}) V_{\pi}(S_t)$$

#### TD and Bellman Operator

• TD as an approximate Policy Iteration:

 $\mathbb{E}[V_{\pi}](S_t) \leftarrow V_{\pi} + \alpha(N(S_t))(\mathcal{T}^{\pi} - \mathrm{Id}) V_{\pi}(S_t)$ 

- Proof of convergence of this algorithm to a zero of  $\mathcal{T}^{\pi}$  Id, i.e. the fixed point of  $\mathcal{T}^{\pi}$ !
- Proof requires a mild assumption of  $\alpha$  (satisfied by  $\alpha(N) = 1/N$ ) and the strong assumption that N(s) goes to  $\infty$ .
- MC could be interpreted in a similar way (stochastic approximation) by noticing that  $\mathbb{E}[G_t V_{\pi}(S_t)|S_t] = v_{\pi}(S_t) V_{\pi}(S_t)$ .
- $\bullet$  Often use with a constant  $\alpha$

## MC vs TD

Prediction with Temporal Differencies



$$V_{\pi}(S_t) \leftarrow V_{\pi}(S_t) + \alpha(N(S_t))(G_t - V_{\pi}(S_t))$$
  
or 
$$V_{\pi}(S_t) \leftarrow V_{\pi}(S_t) + \alpha(N(S_t))\underbrace{(R_{t+1} + \gamma V_{\pi}(S_{t+1}) - V_{\pi}(S_t))}_{\delta_t}$$

## MC vs TD

- Both are based on stochastic approximation.
- Both converges (under similar assumptions) to the correct value function.
- TD does not require to wait until the end of the episode.
- $\bullet$  No theorical difference in the speed of convergence but often TD is better. . .
- Solve different approximate problems when used with a finite set of episodes:
  - MC compute the empirical gain from any state.
  - TD compute the value function of the empirical Bellman operator (the one obtained by using the empirical transition probabilities)
- If  $V_{\pi}$  is kept constant during an episode

$$G_t - V_{\pi}(S_t) = \sum \gamma^{t'-t} \delta_t$$

Link with Stochastic Approximation



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## Stochastic Approximation

Link with Stochastic Approximation



# $\theta_{k+1} = \theta_k + \alpha_k h_k(\theta_k) \quad \text{with} \quad h_k(\theta) = H(\theta) + \epsilon_k + \eta_k$ $\implies \theta_k \to \{\theta, H(\theta) = 0\}$

#### Stochastic Approximation

- Family of sequential stochastic algorithm converging to a zero of a function.
- Classical assumptions:
  - $\mathbb{E}[\epsilon_k] = 0$ ,  $\mathbb{V}$ ar  $[\epsilon_k] < \sigma^2$ , and  $\mathbb{E}[\|\eta_k\|] \to 0$ ,
  - $\sum_k \alpha_k \to \infty$  and  $\sum_k \alpha_k^2 < \infty$ ,
  - the algorithm converges if we replace  $h_k$  by H.
- Convergence toward a neighborhood if  $\alpha$  is kept constant (as often in practice).
- Most famous example are probably Robbins-Monro and SGD.
- Proof quite technical in general.
- The convergence with H is easy to obtain for a contraction.

## Stochastic Approximation and ODE





From 
$$\theta_{k+1} = \theta_k + \alpha_k h_k(\theta_k)$$
 with  $h_k(\theta) = H(\theta) + \epsilon_k + \eta_k$   
to  $\frac{d\tilde{\theta}}{dt} = H(\tilde{\theta})$ 

#### ODE Approach

- General proof showing that the algorithm converges provided the ODE converges.
- Rely on the rewriting the equation

$$\frac{\partial_{k+1} - \theta_k}{\alpha_k} = h_k(\theta_k) = H(\theta_k) + \epsilon_k + \eta_k$$

- $\alpha_k$  can be interpreted as a time difference allowing to define a time  $t_k = \sum_{t' \le t} \alpha_k$ .
- $\theta(t)$  is piecewise affine and defined through its derivative at time  $t \in (t_k, t_{k+1})$ .
- This piecewise function remains close to any solution of the ODE starting from  $\theta_k$  for an arbitrary amount of time provided k is large enough.
- More general proofs based on martingale.

## Asynchronous Update

Link with Stochastic Approximation



## From $\theta_{k+1} = \theta_k + \alpha_k h_k(\theta_k)$ with $h_k(\theta) = H(\theta) + \epsilon_k + \eta_k$ to $\forall i, \theta_{k+1}(i) = \theta_k(i) + \alpha_k(i)h_k(\theta_k)(i)$

## Asynchronous Update

- Componentwise action on  $\theta$ .
- Not necessarily the same stepsize  $\alpha_k(i)$  for all components.
- $\alpha_k(i) = 0$  is permitted!
- Previous results hold provided for every component i,  $\sum_k \alpha_k(i) \to \infty$  and  $\sum_k \alpha_k^2(i) < \infty$ ,
- Exact setting of TD approximation!



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## Planning with Temporal Differencies

#### A State Value Function Attempt

- $V_{\star}$  is the fixed point of  $\mathcal{T}^{\star}$ .
- Approximate it as the zero of  $\mathcal{T}^{\star} \mathrm{Id}$ .
- By construction

$$\mathcal{T}^{\star} v(S_t) = \max_{a} \mathbb{E}[R_{T+1} + \gamma v(S_{t+1})|S_t, a]$$

• Not an expectation!

## A State-Action Value Function Attempt

- $q_{\star}$  is the fixed point of  $\mathcal{T}^{\star}$ .
- Approximate it as the zero of  $\mathcal{T}^{\star} \mathrm{Id}$ .
- By construction

$$\mathcal{T}^{\star}q(S_t, A_t) = \mathbb{E}\left[R_{t+1} + \gamma \max_{a} q(S_{t+1}, a) \middle| S_t, A_t\right]$$

• An expectation!





## Q Learning

Planning with Value Iteration

## Discounted: Planning by Q-Learning

```
input: MDP environment, initial state distribution \mu_0, policy \Pi and discount factor \gamma
parameter: Number of step T
init: \forall s, a, Q(s, a), N(s, a) = 0, n=0, t' = 0
repeat
     t \leftarrow 0
     Pick initial state S_0 following \mu_0
     repeat
          N(S_t) \leftarrow N(S_t) + 1
          Pick action A_t according to \pi(\cdot|S_t)
          Q(S_t, A_t) \leftarrow Q(S_t, A_t) + \alpha(N(S_t, A_t)) \left(R_{t+1} + \gamma \max Q(S_{t+1}, a) - Q(S_t, A_t)\right)
          t \leftarrow t + 1
          t' \leftarrow t' + 1
     until episod ends at time T' or t' == T
until t' == T
output: Deterministic policy \tilde{\pi}(s) = \operatorname{argmax}_{s} Q(s, a)
```

## Planning with Q Learning



$$Q(S_t, A_t) = Q(S_t, A_t) + \alpha(N(S_t, A_t)) \left(\underbrace{R_{t+1} + \gamma \max_a Q(S_{t+1}, a) - Q(S_t, A_t)}_{\delta_t}\right)$$

,

## Q-Learning

- Update is independent of the policy  $\Pi.$
- Convergence of the Q-value function provided the policy is such that N(s, a) tends to  $\infty$  for any state and any action.
- Implies a convergence of the policy.
- Relies on temporal difference.
- Most classical (tabular) planning algorithm!

Planning with Policy Improvement



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## Planning with Policy Improvement

Planning with Policy Improvement



from 
$$Q(S_t, A_t) = Q(S_t, A_t) + \alpha(N(S_t, A_t)) \left(\underbrace{\frac{R_{t+1} + \gamma \max_a Q(S_{t+1}, a) - Q(S_t, A_t)}{\delta_t}}_{\delta_t}\right)$$
  
to  $Q(S_t, A_t) = Q(S_t, A_t) + \alpha(N(S_t, A_t)) \left(\underbrace{\frac{R_{t+1} + \gamma Q(S_{t+1}, A_{t+1}) - Q(S_t, A_t)}{\delta_t}}_{\delta_t}\right)$ 

 $\Pi(S_t) = \operatorname*{argmax}_{a} Q(S_t, a) (\text{plus exploration})$ 

## Policy Improvement

- More emphasis on the policy with a link between the policy used to play and the optimized policy.
- Almost equivalent to use the current policy in the Q-Learning algorithm.

SARSA

Planning with Policy Improvement



#### Discounted: Planning by SARSA

```
input: MDP environment, initial state distribution \mu_0, policy \Pi and discount factor \gamma
parameter: Number of step T
init: \forall s, a, Q(s, a), N(s, a) = 0, n=0, t' = 0
repeat
     t \leftarrow 0 Pick initial state S_0 following \mu_0
     repeat
           N(S_t) \leftarrow N(S_t) + 1
           Pick action A_t according to \pi(\cdot|S_t)
           Q_t(S_{t-1}, A_{t-1}) \leftarrow Q(S_{t-1}, A_{t-1}) + \alpha(N(S_{t-1}, A_{t-1}))(R_t + \gamma Q(S_t, A_t) - Q(S_{t-1}, A_{t-1}))
           \Pi(S_{t-1}) = \operatorname{argmax}_{a} Q(S_{t-1}, a) (plus exploration)
           t \leftarrow t + 1
          t' \leftarrow t' + 1
     until episod ends at time T' or t' == T
until t' == T
output: Deterministic policy \tilde{\pi}(s) = \operatorname{argmax}_{s} Q(s, a)
```

• Does this work?

## SARSA and exploration

Planning with Policy Improvement



$$\Pi(S_t) = \operatorname*{argmax}_a Q(S_t, a) (\mathsf{plus} \; \mathsf{exploration})$$

#### SARSA and Exploration

- No hope of convergence if we do not explore all possible actions (and states).
- Impossible if the policy used is deterministic.
- Exploration is required!
- Most classical choice:  $\epsilon$ -greedy policy with a decaying  $\epsilon$ .
- Convergence proof is harder than for *Q*-Learning.
- Relies on the similarity in the limit (when  $\epsilon$  goes to 0) with the *Q*-Learning algorithm.

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## Q-Learning vs SARSA









#### How different are they?

- $\bullet\,$  In Q-learning, the exploratory policy used is decoupled from the optimized policy.
- This exploratory policy may yield low rewards on average.
- In SARSA, the two policies are linked with the hope on having higher rewards during the learning step.
- Subtle different behavior even if we modify the exploratory policy in *Q*-Learning.



## Exploration vs Exploitation

- Exploration: explore new policies to be able to discover the best ones.
- Exploitation: use good policies to obtain a good return.
- Exploration is a requirement.
- No tradeoff if we optimize only the final result!
- Tradeoff between the two if we consider that the returns during training matters!
- $\bullet~Q$ -learning use the first approach and SARSA try to tackle the second.
- Tradeoff if we study a regret:

$$\sum_{\star} \mathbb{E}_{\Pi_{\star}}[R_t] - \mathbb{E}_{\Pi_t}[R_t]$$

which forces us to be good as fast as possible.

• No natural definition in the discounted setting.

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