



## The Genetic and Evolutionary Computation Conference

### Algorithm and Experiment Design with HeuristicLab

An Open Source Optimization Environment for Research and Education

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## Instructor Biographies

### Stefan Wagner

- ❖ MSc in computer science (2004)  
Johannes Kepler University Linz, Austria
- ❖ PhD in technical sciences (2009)  
Johannes Kepler University Linz, Austria
- ❖ Associate professor (2005 – 2009)  
Upper Austria University of Applied Sciences
- ❖ Full professor for complex software systems (since 2009)  
Upper Austria University of Applied Sciences
- ❖ Co-founder of the HEAL research group
- ❖ Project manager and chief architect of HeuristicLab
- ❖ <http://heal.heuristiclab.com/team/wagner>



### Gabriel Kronberger

- ❖ MSc in computer science (2005)  
Johannes Kepler University Linz, Austria
- ❖ PhD in technical sciences (2010)  
Johannes Kepler University Linz, Austria
- ❖ Research assistant (since 2005)  
Upper Austria University of Applied Sciences
- ❖ Member of the HEAL research group
- ❖ Architect of HeuristicLab
- ❖ <http://heal.heuristiclab.com/team/kronberger>



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## Agenda

- ❖ Objectives of the Tutorial
- ❖ Introduction
- ❖ Where to get HeuristicLab?
- ❖ Plugin Infrastructure
- ❖ Graphical User Interface
- ❖ Available Algorithms & Problems
- ❖ Demonstration
- ❖ Some Additional Features
- ❖ Planned Features
- ❖ Team
- ❖ Suggested Readings
- ❖ Bibliography
- ❖ Questions & Answers



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## Objectives of the Tutorial

- ❖ Introduce general motivation and design principles of HeuristicLab
- ❖ Show where to get HeuristicLab
- ❖ Explain basic GUI usability concepts
- ❖ Demonstrate basic features
- ❖ Demonstrate editing and analysis of optimization experiments
- ❖ Demonstrate custom algorithms and graphical algorithm designer
- ❖ Demonstrate data-based modeling features
- ❖ Outline some additional features

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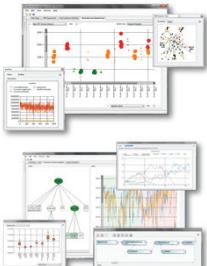


## Introduction



### HeuristicLab

A Paradigm-Independent and Extensible Environment for Heuristic Optimization



- ❖ Motivation and Goals
  - graphical user interface
  - paradigm independence
  - multiple algorithms and problems
  - large scale experiments and analyses
  - parallelization
  - extensibility, flexibility and reusability
  - visual and interactive algorithm development
  - multiple layers of abstraction
  
- ❖ Facts
  - development of HeuristicLab started in 2002
  - based on Microsoft .NET and C#
  - used in research and education
  - second place at the Microsoft Innovation Award 2009
  - open source (GNU General Public License)
  - version 3.3.0 released on May 18th, 2010
  - latest version 3.3.5 released in June 2011

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## Where to get HeuristicLab?

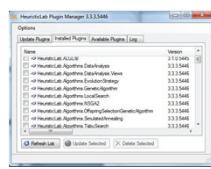


- ❖ Download binaries
  - deployed as ZIP archives
  - latest stable version 3.3.5
    - released in June 2011
  - daily trunk build
  - <http://dev.heuristiclab.com/download>
  
- ❖ Check out sources
  - SVN repository
  - HeuristicLab 3.3.5 tag
    - <http://dev.heuristiclab.com/svn/hl/core/tags/3.3.5>
  - current development trunk
    - <http://dev.heuristiclab.com/svn/hl/core/trunk>
  
- ❖ License
  - GNU General Public License (Version 3)
  
- ❖ System requirements
  - Microsoft .NET Framework 4.0 Full Version
  - enough RAM and CPU power :-)

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## Plugin Infrastructure



- ❖ HeuristicLab consists of many assemblies
  - for example 74 plugins in HeuristicLab 3.3.3
  - plugins can be loaded or unloaded at runtime
  - plugins can be updated via internet
  - application plugins provide GUI frontends
  
- ❖ Extensibility
  - developing and deploying new plugins is easy
  - dependencies are explicitly defined, automatically checked and resolved
  - automatic discovery of interface implementations (service locator pattern)
  
- ❖ Plugin Manager
  - GUI to check, install, update or delete plugins

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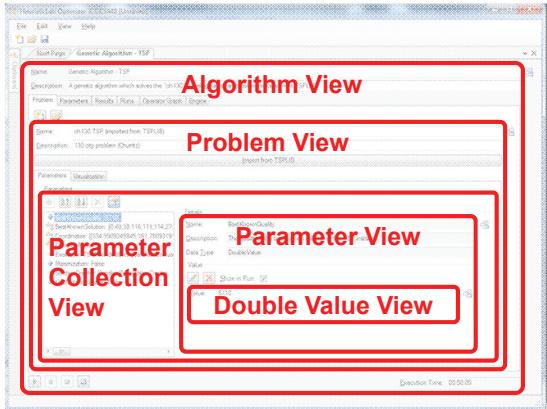
## Graphical User Interface

- ❖ HeuristicLab GUI is made up of views
  - views are visual representations of content objects
  - views are composed in the same way as their content
  - views and content objects are loosely coupled
  - multiple different views may exist for the same content
  
- ❖ Drag & Drop
  - views support drag & drop operations
  - content objects can be copied (default) or moved (shift key)
  - enabled for collection items and content objects

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## Graphical User Interface



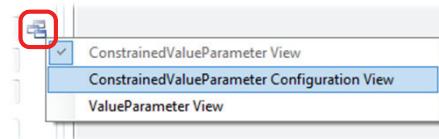
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## Graphical User Interface

### ❖ ViewHost

- control which hosts views
- right-click on windows icon to switch views
- double-click on windows icon to open another view
- drag & drop windows icon to copy contents



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## Available Algorithms & Problems

### ❖ Algorithms

- Genetic Algorithm
- Island Genetic Algorithm
- Offspring Selection Genetic Algorithm
- Island Offspring Selection Genetic Algorithm
- SASEGASA
- Evolution Strategy
- NSGA-II
- Particle Swarm Optimization
- Local Search
- Simulated Annealing
- Tabu Search
- Variable Neighborhood Search
- Linear Regression
- Linear Discriminant Analysis
- Support Vector Machine
- K-Means
- User-defined Algorithm

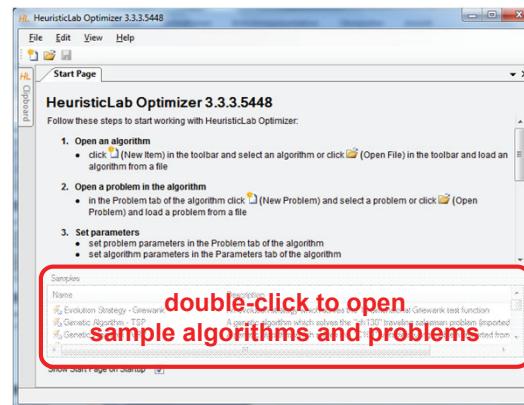
### ❖ Problems

- Single-Objective Test Function
- Traveling Salesman Problem
- Quadratic Assignment Problem
- Vehicle Routing Problem
- Scheduling
- Knapsack
- OneMax
- Data Analysis
- Regression
- Symbolic Regression
- Classification
- Symbolic Classification
- Clustering
- Artificial Ant
- External Evaluation Problem
- User-defined Problem

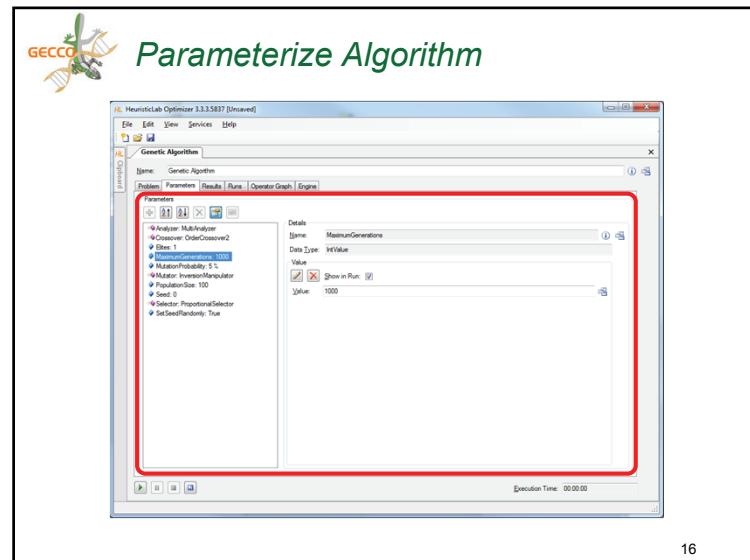
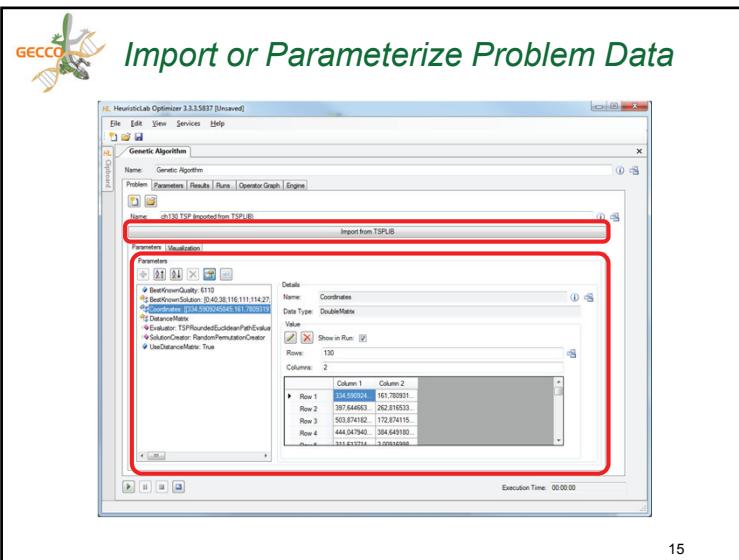
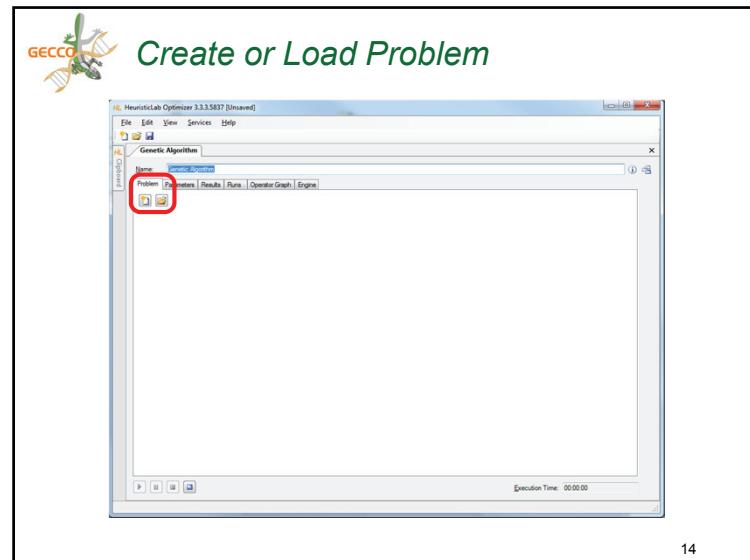
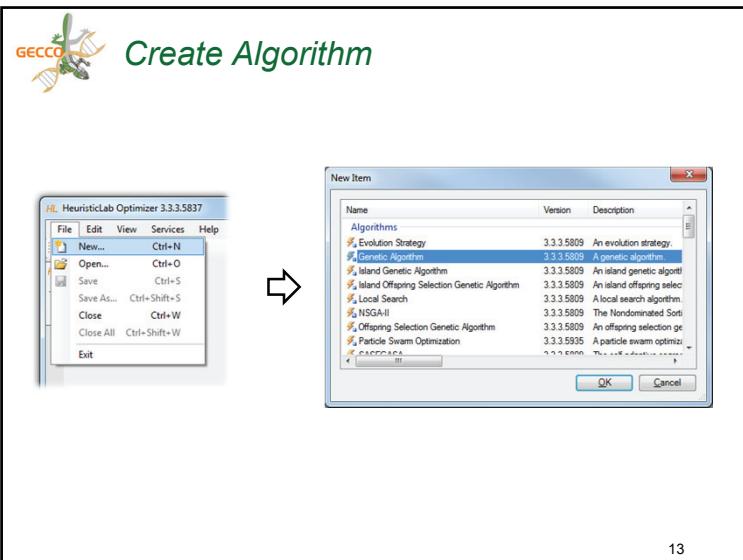
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## HeuristicLab Optimizer

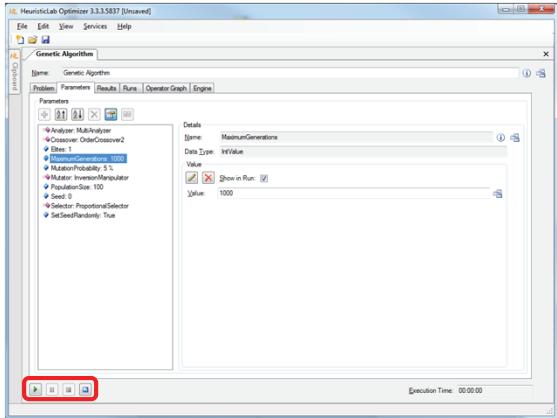


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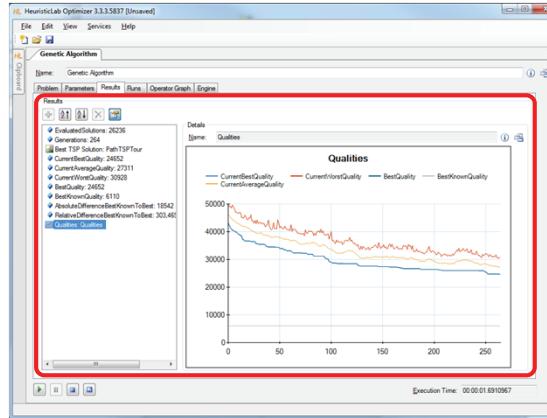
## Start, Pause, Resume, Stop and Reset



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## Inspect Results



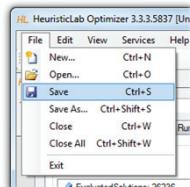
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## Save and Load

### ❖ Save to and load from disk

- HeuristicLab items (i.e., algorithms, problems, experiments, ...) can be saved to and loaded from a file
- algorithms can be paused, saved, loaded and resumed
- data format is custom compressed XML
- saving and loading files might take several minutes
- saving and loading large experiments requires some memory

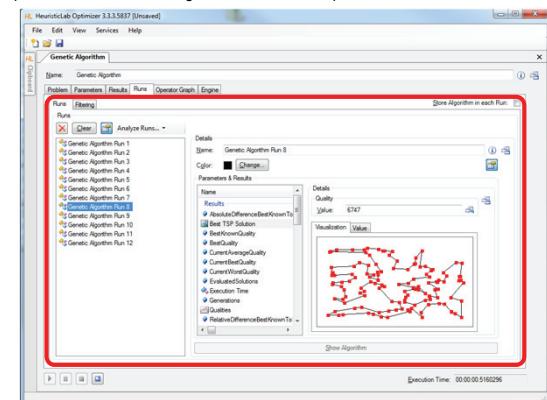


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## Compare Runs

- ❖ A run is created each time when the algorithm is stopped
  - runs contain all results and parameter settings
  - previous results are not forgotten and can be compared



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## Create Batch Runs and Experiments

### ❖ Batch runs

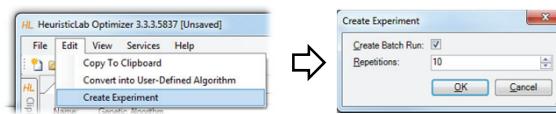
- execute the same optimizer (e.g. algorithm, batch run, experiment) several times

### ❖ Experiments

- execute different optimizers
- suitable for large scale algorithm comparison and analysis

### ❖ Experiments and batch runs can be nested

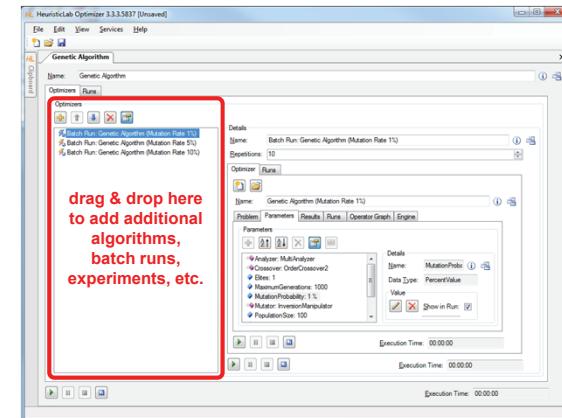
### ❖ Generated runs can be compared afterwards



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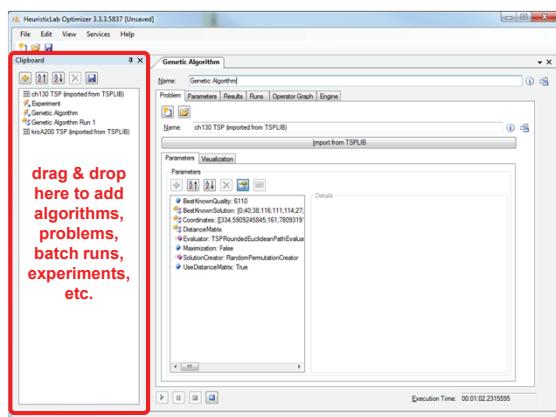
## Create Batch Runs and Experiments



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## Clipboard



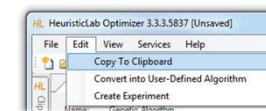
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## Clipboard

### ❖ Store items

- click on the buttons to add or remove items
- drag & drop items on the clipboard
- use the menu to add a copy of a shown item to the clipboard



### ❖ Show items

- double-click on an item in the clipboard to show its view

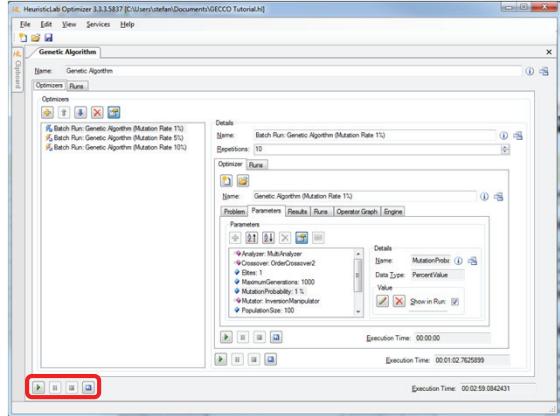
### ❖ Save and restore clipboard content

- click on the save button to write the clipboard content to disk
- clipboard is automatically restored when HeuristicLab is started the next time

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## Start, Pause, Resume, Stop, Reset



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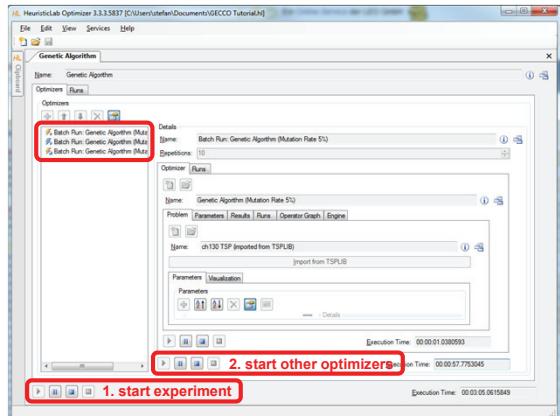
## Multi-core CPUs and Parallelization

- ❖ Parallel execution of optimizers in experiments
  - optimizers in an experiment are executed sequentially from top to bottom per default
  - experiments support parallel execution of their optimizers
  - select a not yet executed optimizer and start it manually to utilize another core
  - execution of one of the next optimizers is started automatically after an optimizer is finished
- ❖ Parallel execution of algorithms
  - HeuristicLab provides special operators for parallelization
  - engines decide how to execute parallel operations
  - sequential engine executes everything sequentially
  - parallel engine executes parallel operations on multiple cores
  - Hive engine (under development) executes parallel operations on multiple computers
  - all implemented algorithms support parallel solution evaluation

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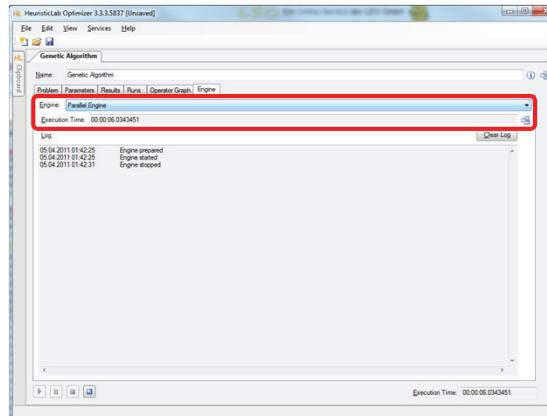
## Parallel Execution of Experiments



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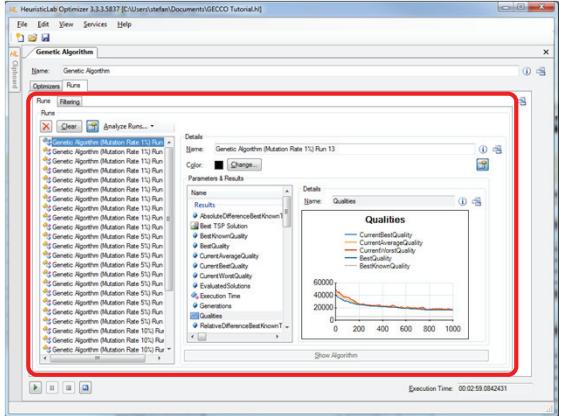
## Parallel Execution of Algorithms



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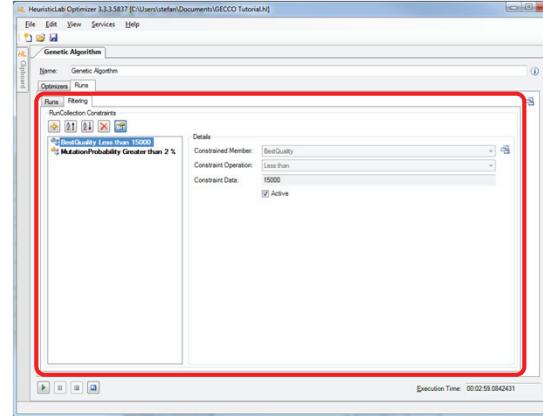
## Compare Runs



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## Filter Runs

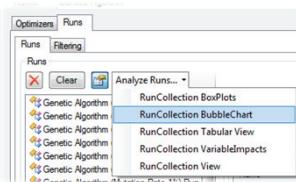


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## Analyze Runs

- ❖ HeuristicLab provides interactive views to analyze and compare all runs of a run collection
  - textual analysis
    - RunCollection Tabular View
  - graphical analysis
    - RunCollection BubbleChart
    - RunCollection BoxPlots
- ❖ Filtering is automatically applied to all open run collection views



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## RunCollection Tabular View

	BestKnownQuality	BestKnownSolution	BestQuality	Coordinates	Crossover	CurrentAverageQuality
Genetic Algorithm (Mutation Rate 1%) Run 13	3110	[04:30:116.111.114...]	16405	[334.590245...	OrderCrossover	16543.13
Genetic Algorithm (Mutation Rate 1%) Run 14	3110	[04:30:116.111.114...]	14793	[334.590245...	OrderCrossover	15029.02
Genetic Algorithm (Mutation Rate 1%) Run 15	3110	[04:30:116.111.114...]	14522	[334.590245...	OrderCrossover	15045.42
Genetic Algorithm (Mutation Rate 1%) Run 16	3110	[04:30:116.111.114...]	13243	[334.590245...	OrderCrossover	12405.95
Genetic Algorithm (Mutation Rate 1%) Run 17	3110	[04:30:116.111.114...]	13703	[334.590245...	OrderCrossover	17103.58
Genetic Algorithm (Mutation Rate 1%) Run 18	3110	[04:30:116.111.114...]	13964	[334.590245...	OrderCrossover	13951.09
Genetic Algorithm (Mutation Rate 1%) Run 19	3110	[04:30:116.111.114...]	15431	[334.590245...	OrderCrossover	15431.74
Genetic Algorithm (Mutation Rate 1%) Run 20	3110	[04:30:116.111.114...]	14484	[334.590245...	OrderCrossover	15147
Genetic Algorithm (Mutation Rate 1%) Run 21	3110	[04:30:116.111.114...]	13771	[334.590245...	OrderCrossover	13954.56
Genetic Algorithm (Mutation Rate 1%) Run 22	3110	[04:30:116.111.114...]	14529	[334.590245...	OrderCrossover	14532.3
Genetic Algorithm (Mutation Rate 1%) Run 23	3110	[04:30:116.111.114...]	14599	[334.590245...	OrderCrossover	14527
Genetic Algorithm (Mutation Rate 1%) Run 24	3110	[04:30:116.111.114...]	12403	[334.590245...	OrderCrossover	12810.09
Genetic Algorithm (Mutation Rate 1%) Run 25	3110	[04:30:116.111.114...]	14091	[334.590245...	OrderCrossover	14953.98
Genetic Algorithm (Mutation Rate 1%) Run 26	3110	[04:30:116.111.114...]	12595	[334.590245...	OrderCrossover	13297.39
Genetic Algorithm (Mutation Rate 1%) Run 27	3110	[04:30:116.111.114...]	12792	[334.590245...	OrderCrossover	13254.38
Genetic Algorithm (Mutation Rate 1%) Run 28	3110	[04:30:116.111.114...]	12711	[334.590245...	OrderCrossover	13151.19
Genetic Algorithm (Mutation Rate 1%) Run 29	3110	[04:30:116.111.114...]	13345	[334.590245...	OrderCrossover	12625.78
Genetic Algorithm (Mutation Rate 1%) Run 30	3110	[04:30:116.111.114...]	13007	[334.590245...	OrderCrossover	12544.73
Genetic Algorithm (Mutation Rate 1%) Run 31	3110	[04:30:116.111.114...]	12403	[334.590245...	OrderCrossover	12544.51
Genetic Algorithm (Mutation Rate 1%) Run 32	3110	[04:30:116.111.114...]	12741	[334.590245...	OrderCrossover	117113.18
Genetic Algorithm (Mutation Rate 1%) Run 33	3110	[04:30:116.111.114...]	15921	[334.590245...	OrderCrossover	18204.04
Genetic Algorithm (Mutation Rate 1%) Run 34	3110	[04:30:116.111.114...]	16384	[334.590245...	OrderCrossover	19609.36

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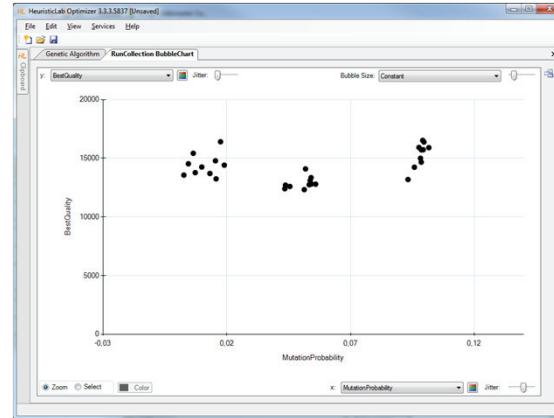
## RunCollection Tabular View

- ❖ Sort columns
  - click on column header to sort column
  - Ctrl-click on column header to sort multiple columns
- ❖ Show or hide columns
  - right-click on table to open dialog to show or hide columns
- ❖ Compute statistical values
  - select multiple numerical values to see count, sum, minimum, maximum, average and standard deviation
- ❖ Select, copy and paste into other applications

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## RunCollection BubbleChart



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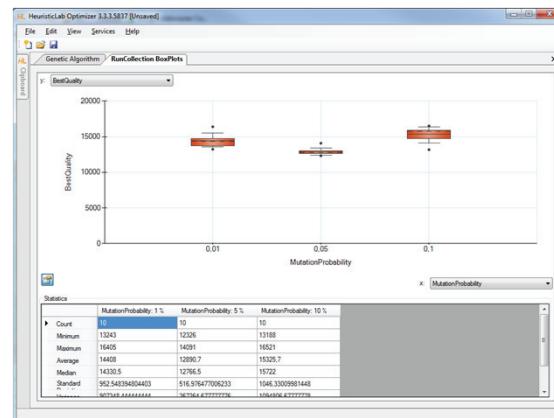
## RunCollection BubbleChart

- ❖ Choose values to plot
  - choose which values to show on the x-axis, the y-axis and as bubble size
  - possible values are all parameter settings and results
- ❖ Add jitter
  - add jitter to separate overlapping bubbles
- ❖ Zoom in and out
  - click on Zoom and click and drag in the chart area to zoom in
  - double click on the chart area background or on the circle buttons beside the scroll bars to zoom out
- ❖ Color bubbles
  - click on Select, choose a color and click and drag in the chart area to select and color bubbles
  - apply coloring automatically by clicking on the axis coloring buttons
- ❖ Show runs
  - double click on a bubble to open its run
- ❖ Export image
  - right-click to open context menu to copy or save image
  - save image as pixel (BMP, JPG, PNG, GIF, TIF) or vector graphics (EMF)
- ❖ Show box plots
  - right-click to open context menu to show box plots view

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## RunCollection BoxPlots



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## RunCollection BoxPlots

- ❖ Choose values to plot
  - choose which values to show on the x-axis and y-axis
  - possible values are all parameter settings and results
- ❖ Zoom in and out
  - click on Zoom and click and drag in the chart area to zoom in
  - double click on the chart area background or on the circle buttons beside the scroll bars to zoom out
- ❖ Show or hide statistical values
  - click on the lower left button to show or hide statistical values
- ❖ Export image
  - right-click to open context menu to copy or save image
  - save image as pixel (BMP, JPG, PNG, GIF, TIF) or vector graphics (EMF)

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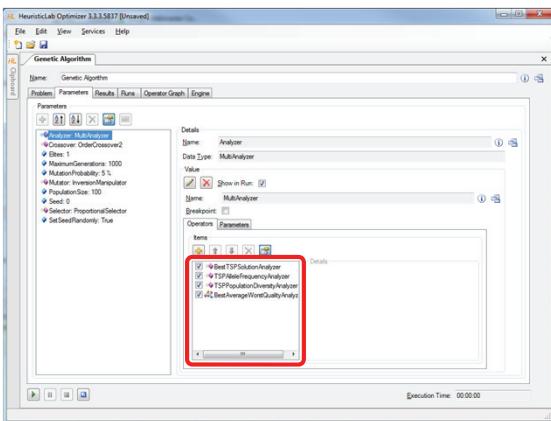
## Analyzers

- ❖ Special operators for analysis purposes
  - are executed after each iteration
  - serve as general purpose extension points of algorithms
  - can be selected and parameterized in the algorithm
  - perform algorithm-specific and/or problem-specific tasks
  - some analyzers are quite costly regarding runtime and memory
  - implementing and adding custom analyzers is easy
- ❖ Examples
  - TSPAlleleFrequencyAnalyzer
  - TSPPopulationDiversityAnalyzer
  - SuccessfulOffspringAnalyzer
  - SymbolicDataAnalysisVariableFrequencyAnalyzer
  - SymbolicRegressionSingleObjectiveTrainingBestSolutionAnalyzer
  - ...

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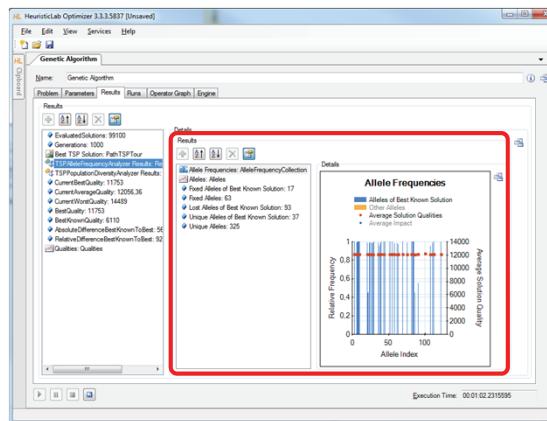
## Analyzers



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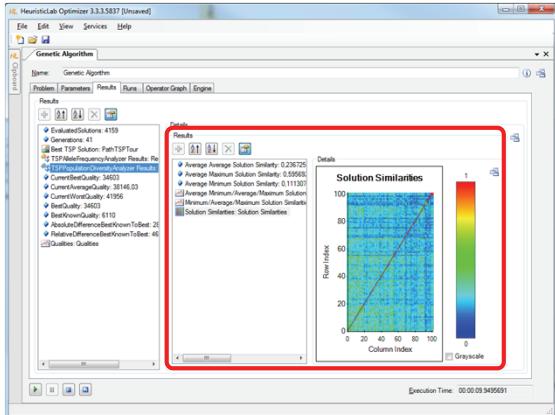
## TSPAlleleFrequencyAnalyzer



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## TSPPopulationDiversityAnalyzer



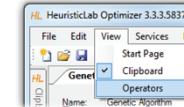
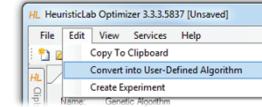
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## Building User-Defined Algorithms

### Operator graphs

- algorithms are represented as operator graphs
- operator graphs of user-defined algorithms can be changed
- algorithms can be defined in the graphical algorithm designer
- use the menu to convert a standard algorithm into a user-defined algorithm



### Operators sidebar

- drag & drop operators into an operator graph

### Programmable operators

- add programmable operators in order to implement custom logic in an algorithm
- no additional development environment needed

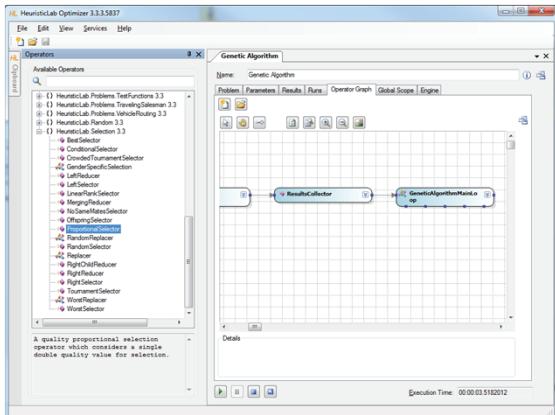
### Debug algorithms

- use the debug engine to obtain detailed information during algorithm execution

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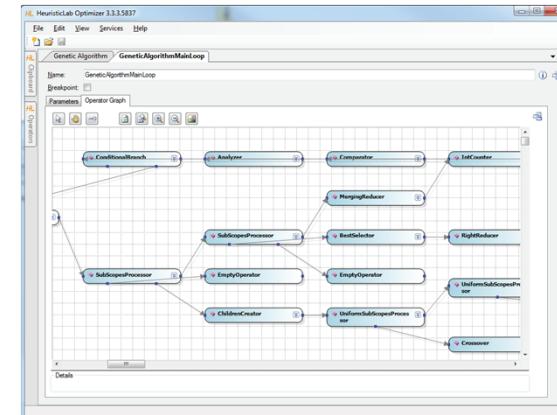
## Building User-Defined Algorithms



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## Building User-Defined Algorithms



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## Programmable Operators

The screenshot shows the HeuristicLab Optimizer interface. A code editor window displays the following Java code:

```

public class ProgrammableSingleSuccessorOperator : IOperation
{
    public static IOperation Execute(ProgrammableSingleSuccessorOperator op,
        IExecutionContext context)
    {
        // Implement custom operator logic here
        return op.Successor == null ? null : context.CreateOperation(op.Successor);
    }
}

```

The code editor has a toolbar at the top with icons for File, Edit, View, Services, Help, and various tool buttons. On the left, there's a navigation pane with sections like Assemblies, Namespaces, and Parameters. The main code area has scroll bars.

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## Debugging Algorithms

The screenshot shows the HeuristicLab Optimizer interface with the 'Debug Engine' tab selected. The main window displays a tree view of algorithm components and their execution context. A status bar at the bottom right shows 'Execution Time: 00:00:03.5160212'.

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## Introduction to Data-based Modeling

- ❖ Dataset: Matrix  $(x_{i,j})_{i=1..N, j=1..K}$ 
  - N observations of K input variables
  - $x_{i,j}$  = i-th observation of j-th variable
  - Additionally: Vector of labels  $(y_1 \dots y_N)^T$
- ❖ Goal: learn association of input variable values to labels
- ❖ Common tasks
  - Regression (real-valued labels)
  - Classification (discrete labels)
  - Clustering (no labels, group similar observations)

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## Data-based Modeling Algorithms in HeuristicLab

- ❖ Symbolic regression and classification based on genetic programming
- ❖ External Libraries:
  - Support Vector Machines for Regression and Classification
  - Linear Regression
  - Linear Discriminate Analysis
  - K-Means clustering

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## In the next 60 minutes: case studies

### ❖ Regression

- Artificial benchmark problem dataset *Poly-10*
- Algorithms:
  - Linear regression
  - Symbolic regression using Genetic Programming

### ❖ Classification

- Real world medical *Mammographic Mass* dataset from the UCI Machine Learning Repository
- Algorithms:
  - Symbolic classification

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## Case study: Regression

### ❖ Poly-10 benchmark problem dataset

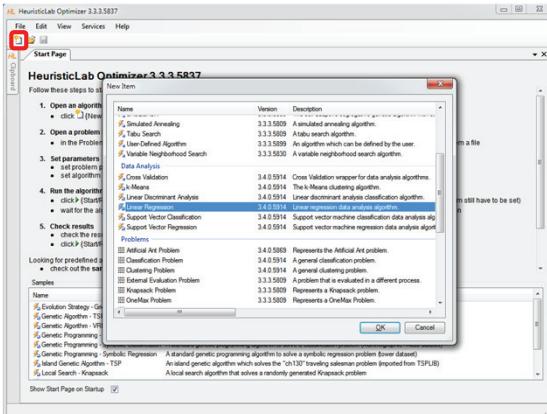
- 10 input variables  $x_1 \dots x_{10}$
- $y = x_1 x_2 + x_3 x_4 + x_5 x_6 + x_1 x_7 x_9 + x_3 x_6 x_{10}$
- Non-linear modeling approach necessary
- Frequently used in GP literature
- Download:  
<http://dev.heuristiclab.com/AdditionalMaterial#GECCO2011>

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## Linear Regression

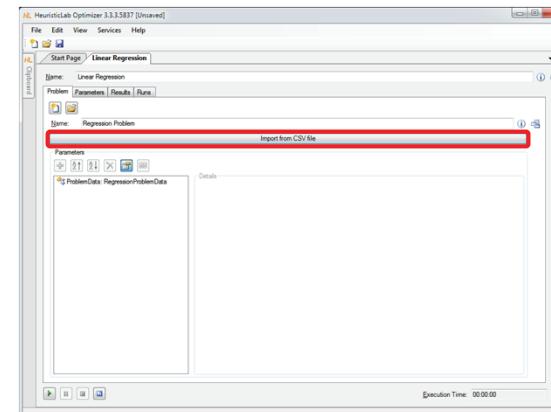
### ❖ Create new algorithm



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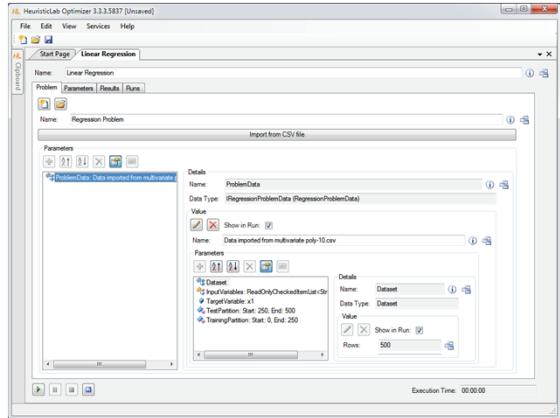
## Import Data from CSV-File



52



## Inspect And Configure Dataset



53



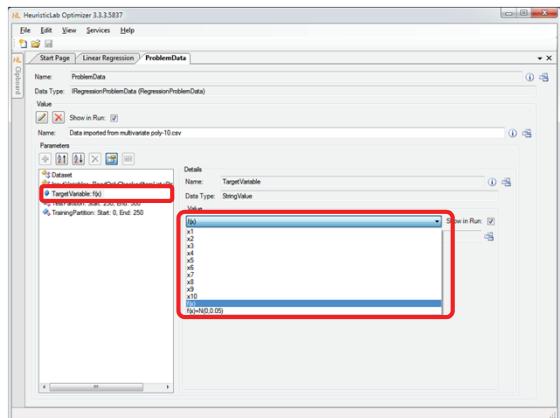
## Inspect Imported Data

Data imported from multivariate poly-10.csv											
x1	x2	x3	x4	x5	x6	x7	x8	x9	x10	x11	x12
0.37	0.26	0.97	0.35	0.24	-0.92	0.99	0.63	0.47	0.07	0.25	0.89
0.74	-0.11	0.72	0.36	-0.72	0.03	0.05	0.80	0.25	0.89	0.25	0.23
0.64	0.74	0.51	0.79	0.00	0.41	0.03	0.01	0.02	0.95	0.01	0.23
0.51	0.89	0.89	0.39	0.56	0.01	0.56	0.01	0.94	0.99	0.01	0.23
0.89	0.34	0.66	0.85	0.01	0.20	0.32	0.55	-0.07	0.75	0.01	0.23
0.00	0.50	-0.87	0.48	0.62	0.86	-0.09	0.59	-0.71	0.32	0.01	0.23
0.47	0.15	0.14	0.04	0.28	-0.76	0.48	0.01	0.01	0.75	0.01	0.23

54



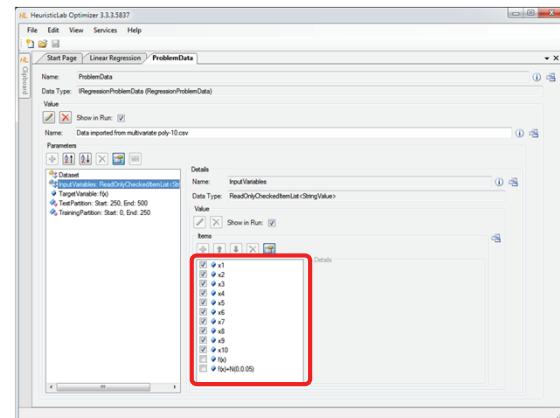
## Set Target Variable



55



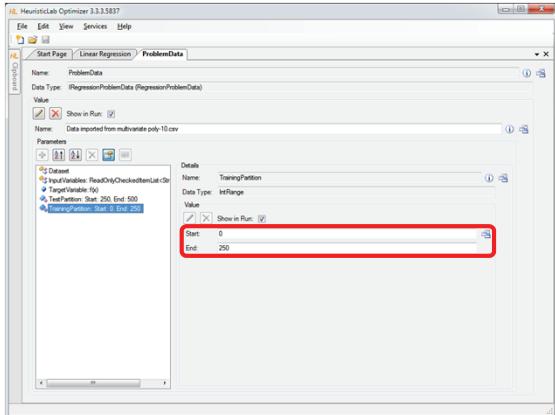
## Select Input Variables



56



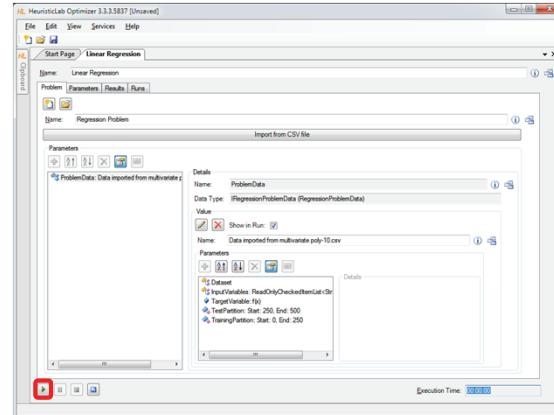
## Configure Training and Test Partitions



57



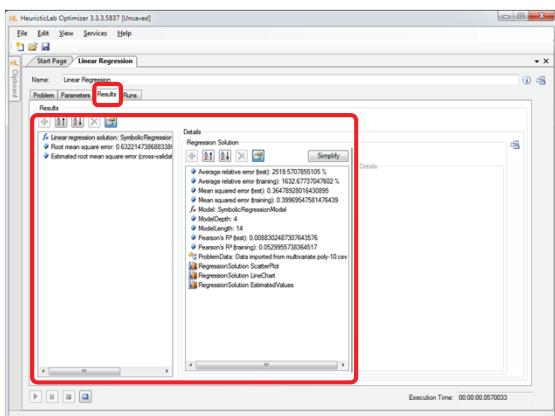
## Run Linear Regression



58



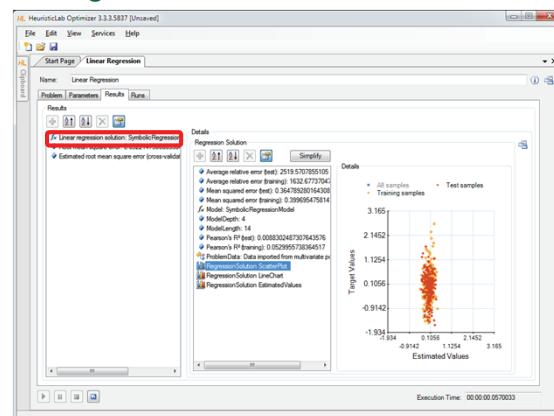
## Inspect Results



59



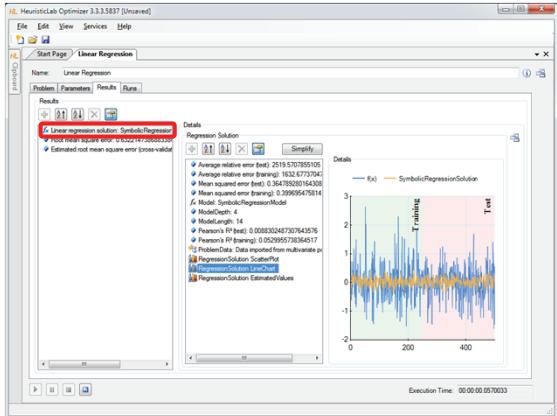
## Inspect Scatterplot of Predicted and Target Values



60



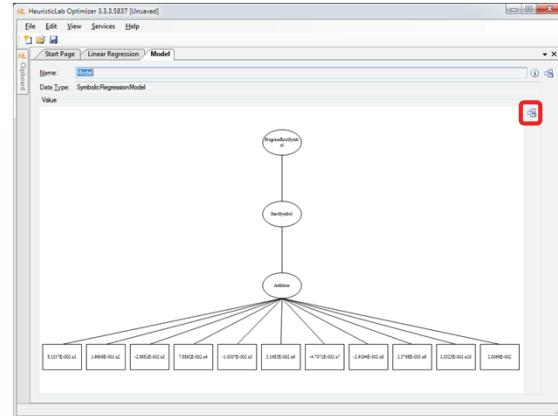
## Inspect Linechart



61



## Inspect Graphical Representation of Model

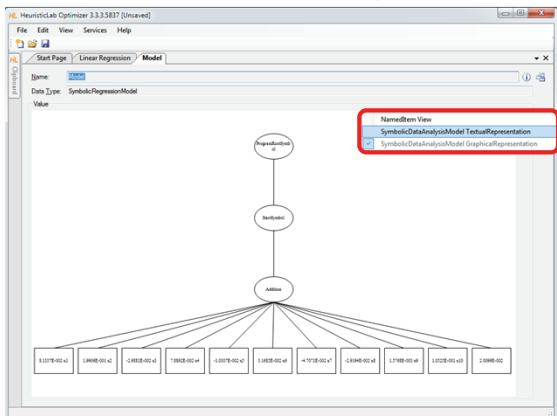


62



## Textual Representations Are Also Available

- ❖ Use ViewHost to switch to textual representation view.



63



## Default Textual Representation for Model Export

```
HeuristicLab Optimizer 3.3.3.5837 [Unsaved]
File Edit View Services Help
Start Page | Linear Regression | Model |
Name: linear
Data Type: SymbolicRegressionModel
Value
Formatter: Default String Formatter
ProgramRootSymbol
SymbolicRegressionModel
Addition
(1.13178e-002)x
(1.13178e-002)
(1.13178e-002)
(7.89302e-002)x
(1.13178e-002)
(3.10516e-002)x
(4.20731e-002)
(-2.91942e-002)x
(1.13178e-002)
(1.05258e-001)x
(2.05998e-002)
```

64



## Textual Representation for Export to LaTeX

```

% need LaTeXpackage{amsmath}
\begin{aligned}
\text{Regr.} &= c_{10} \cdot x_{10}^{10} + c_9 \cdot x_9^{10} + c_8 \cdot x_8^{10} + c_7 \cdot x_7^{10} + c_6 \cdot x_6^{10} + c_5 \cdot x_5^{10} + c_4 \cdot x_4^{10} + c_3 \cdot x_3^{10} + c_2 \cdot x_2^{10} + c_1 \cdot x_1^{10} + c_0 \\
&\quad + c_{10} \cdot x_{10}^9 + c_9 \cdot x_9^9 + c_8 \cdot x_8^9 + c_7 \cdot x_7^9 + c_6 \cdot x_6^9 + c_5 \cdot x_5^9 + c_4 \cdot x_4^9 + c_3 \cdot x_3^9 + c_2 \cdot x_2^9 + c_1 \cdot x_1^9 + c_0 \\
&\quad + c_{10} \cdot x_{10}^8 + c_9 \cdot x_9^8 + c_8 \cdot x_8^8 + c_7 \cdot x_7^8 + c_6 \cdot x_6^8 + c_5 \cdot x_5^8 + c_4 \cdot x_4^8 + c_3 \cdot x_3^8 + c_2 \cdot x_2^8 + c_1 \cdot x_1^8 + c_0 \\
&\quad + c_{10} \cdot x_{10}^7 + c_9 \cdot x_9^7 + c_8 \cdot x_8^7 + c_7 \cdot x_7^7 + c_6 \cdot x_6^7 + c_5 \cdot x_5^7 + c_4 \cdot x_4^7 + c_3 \cdot x_3^7 + c_2 \cdot x_2^7 + c_1 \cdot x_1^7 + c_0 \\
&\quad + c_{10} \cdot x_{10}^6 + c_9 \cdot x_9^6 + c_8 \cdot x_8^6 + c_7 \cdot x_7^6 + c_6 \cdot x_6^6 + c_5 \cdot x_5^6 + c_4 \cdot x_4^6 + c_3 \cdot x_3^6 + c_2 \cdot x_2^6 + c_1 \cdot x_1^6 + c_0 \\
&\quad + c_{10} \cdot x_{10}^5 + c_9 \cdot x_9^5 + c_8 \cdot x_8^5 + c_7 \cdot x_7^5 + c_6 \cdot x_6^5 + c_5 \cdot x_5^5 + c_4 \cdot x_4^5 + c_3 \cdot x_3^5 + c_2 \cdot x_2^5 + c_1 \cdot x_1^5 + c_0 \\
&\quad + c_{10} \cdot x_{10}^4 + c_9 \cdot x_9^4 + c_8 \cdot x_8^4 + c_7 \cdot x_7^4 + c_6 \cdot x_6^4 + c_5 \cdot x_5^4 + c_4 \cdot x_4^4 + c_3 \cdot x_3^4 + c_2 \cdot x_2^4 + c_1 \cdot x_1^4 + c_0 \\
&\quad + c_{10} \cdot x_{10}^3 + c_9 \cdot x_9^3 + c_8 \cdot x_8^3 + c_7 \cdot x_7^3 + c_6 \cdot x_6^3 + c_5 \cdot x_5^3 + c_4 \cdot x_4^3 + c_3 \cdot x_3^3 + c_2 \cdot x_2^3 + c_1 \cdot x_1^3 + c_0 \\
&\quad + c_{10} \cdot x_{10}^2 + c_9 \cdot x_9^2 + c_8 \cdot x_8^2 + c_7 \cdot x_7^2 + c_6 \cdot x_6^2 + c_5 \cdot x_5^2 + c_4 \cdot x_4^2 + c_3 \cdot x_3^2 + c_2 \cdot x_2^2 + c_1 \cdot x_1^2 + c_0 \\
&\quad + c_{10} \cdot x_{10}^1 + c_9 \cdot x_9^1 + c_8 \cdot x_8^1 + c_7 \cdot x_7^1 + c_6 \cdot x_6^1 + c_5 \cdot x_5^1 + c_4 \cdot x_4^1 + c_3 \cdot x_3^1 + c_2 \cdot x_2^1 + c_1 \cdot x_1^1 + c_0 \\
&\quad + c_{10} \cdot x_{10}^0 + c_9 \cdot x_9^0 + c_8 \cdot x_8^0 + c_7 \cdot x_7^0 + c_6 \cdot x_6^0 + c_5 \cdot x_5^0 + c_4 \cdot x_4^0 + c_3 \cdot x_3^0 + c_2 \cdot x_2^0 + c_1 \cdot x_1^0 + c_0
\end{aligned}

```

65

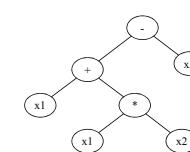


## Nonlinear Modeling: Symbolic Regression

- ❖ Linear regression produced an inaccurate model.
- ❖ Next: produce a nonlinear symbolic regression model using genetic programming

### Genetic programming

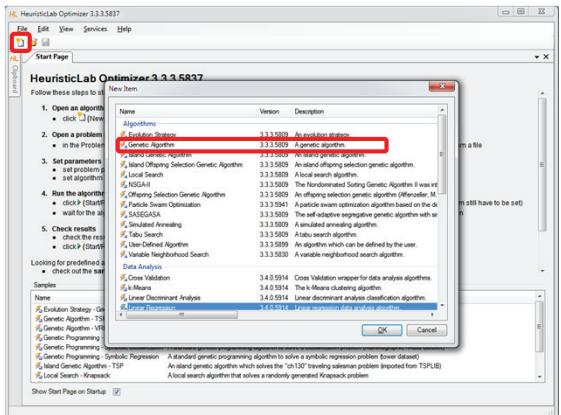
- Evolve variable-length models
- Model representation: symbolic expression tree
- Structure and model parameters are evolved side-by-side
- White-box models



66



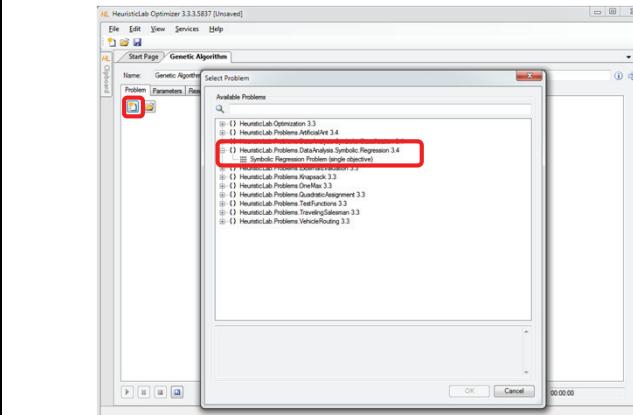
## Create New Genetic Algorithm



67



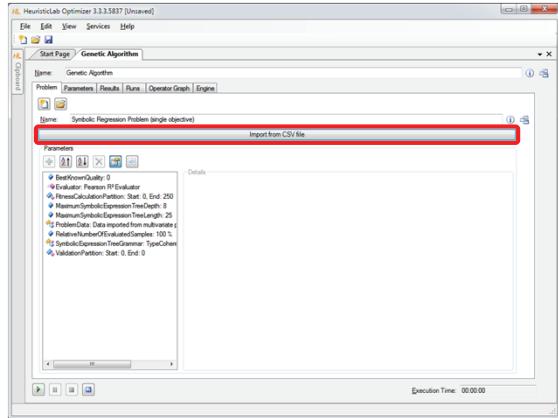
## Create New Symbolic Regression Problem



68



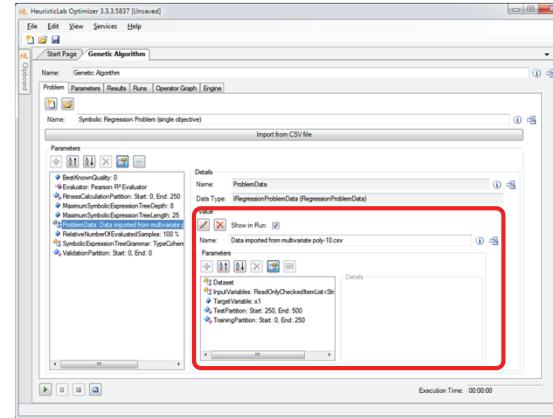
## Import Data



69



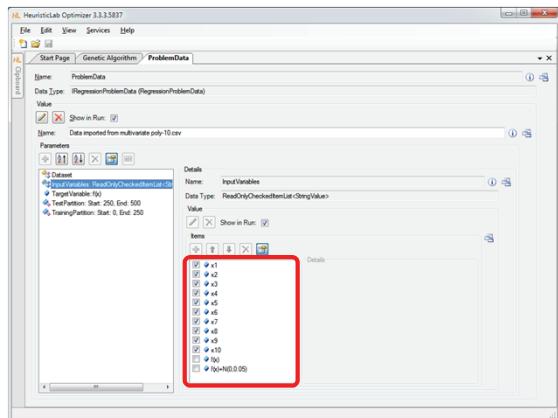
## Inspect Data and Configure Dataset



70



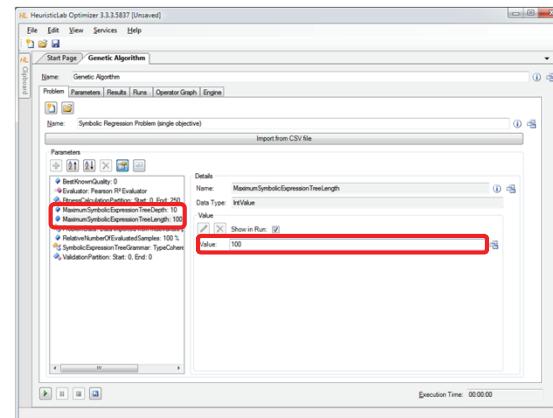
## Set Target and Input Variables



71



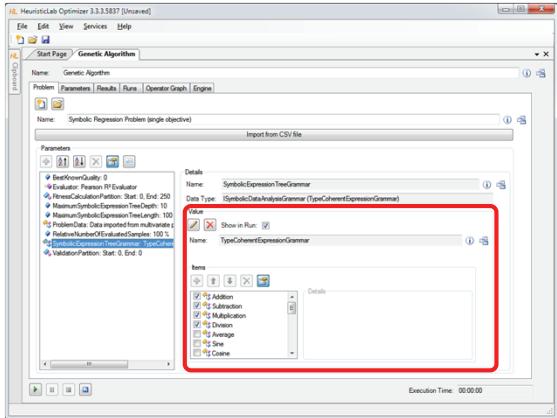
## Configure Maximal Model Depth and Length



72



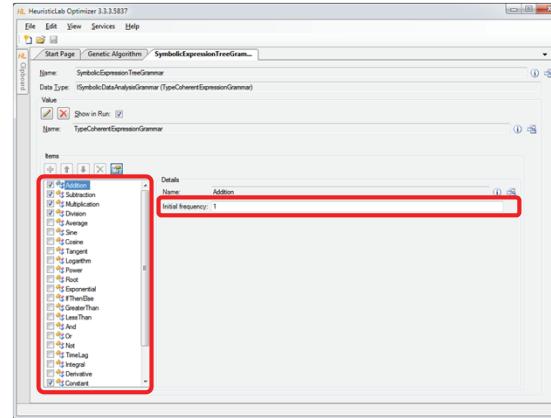
## Configure Function Set (Grammar)



73



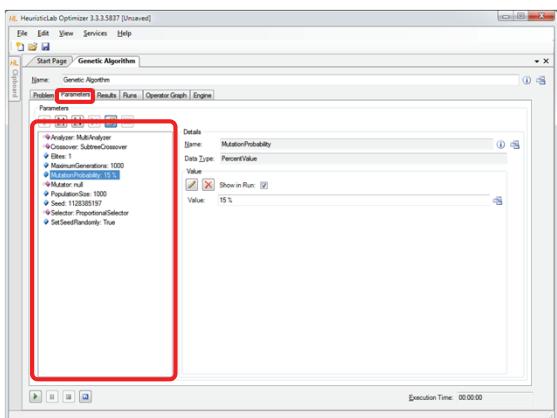
## Configure Function Set (Grammar)



74



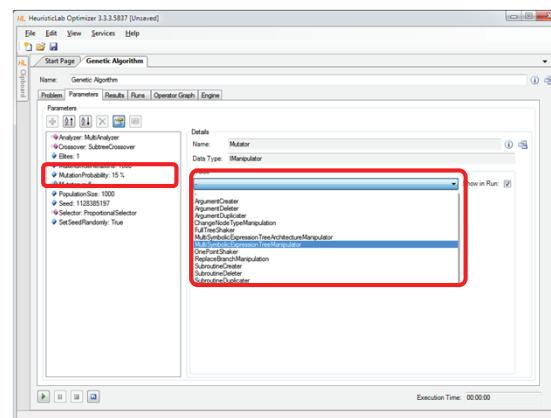
## Configure Algorithm Parameters



75



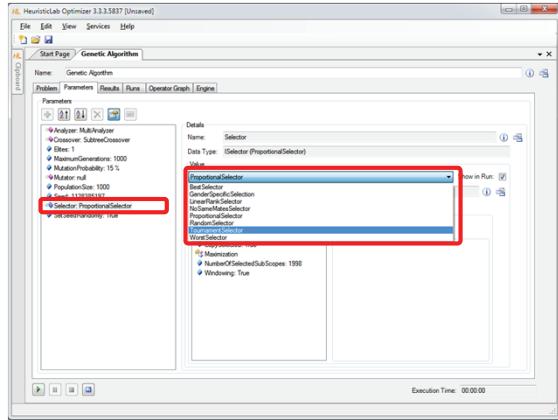
## Configure Mutation Operator



76



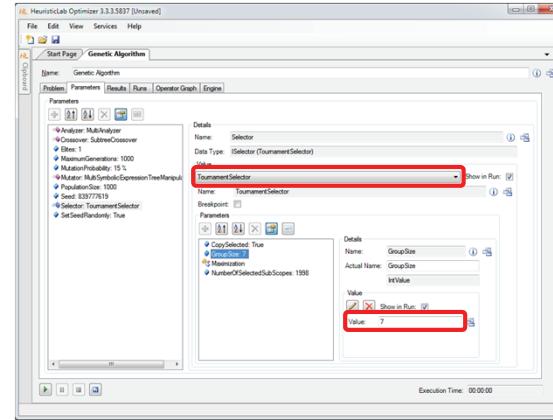
## Configure Selection Operator



77



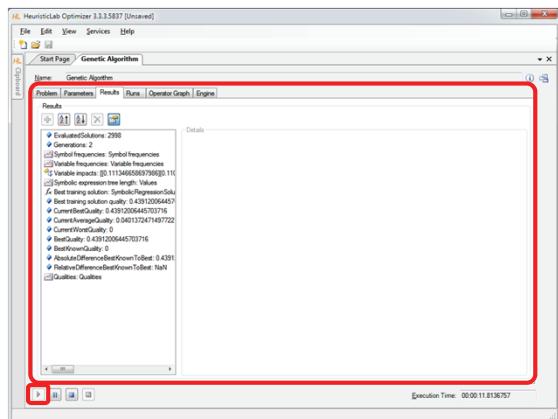
## Configure Tournament Group Size



78



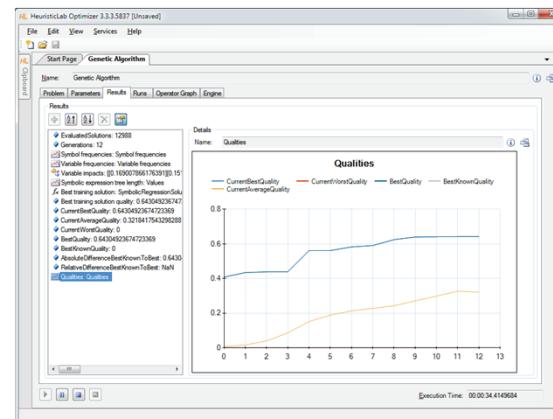
## Start Algorithm and Inspect Results



79



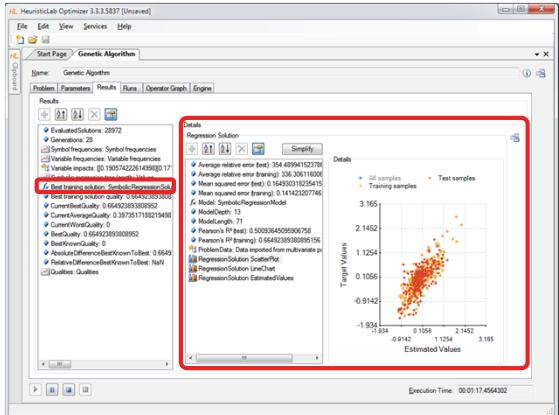
## Inspect Quality Chart



80



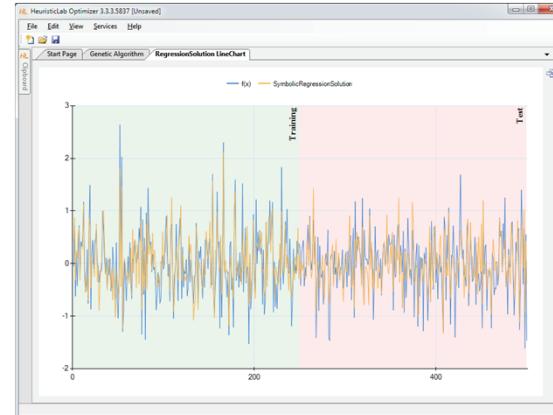
### Inspect Best Model on Training Partition



81



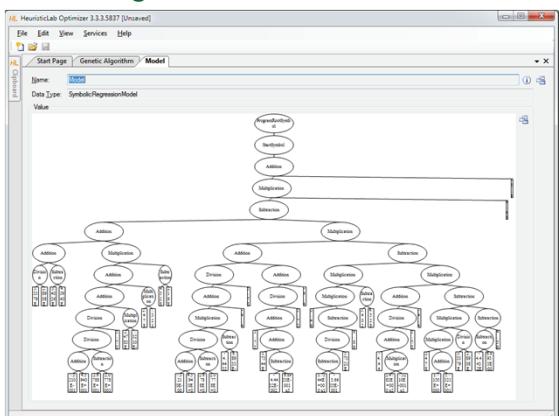
### Inspect Linechart of Best Model on Trainingset



82



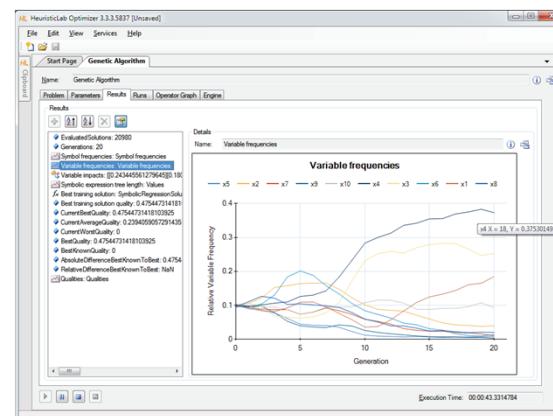
### Inspect Structure of Best Model on Trainingset



83



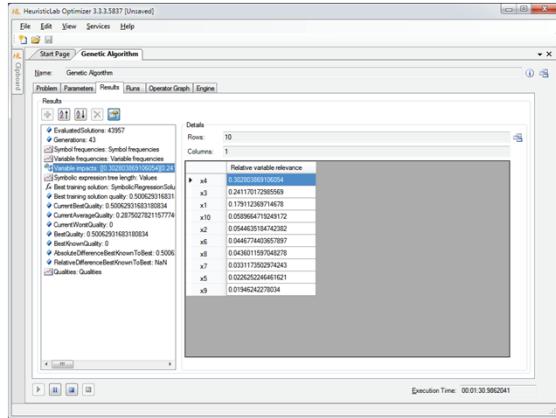
### Inspect Variable Frequency Chart



84



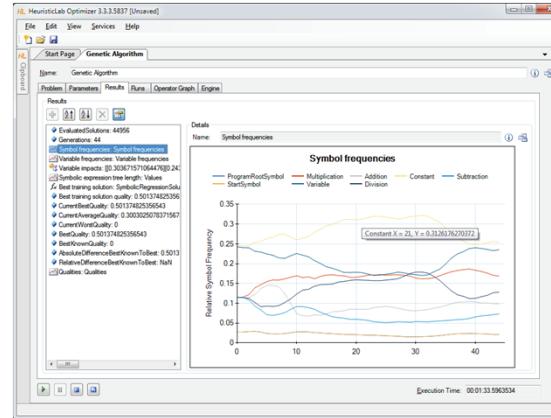
## Inspect Variable Impacts



85



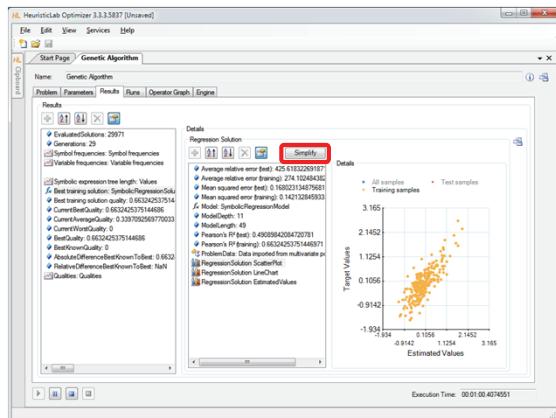
## Inspect Symbol Frequencies



86



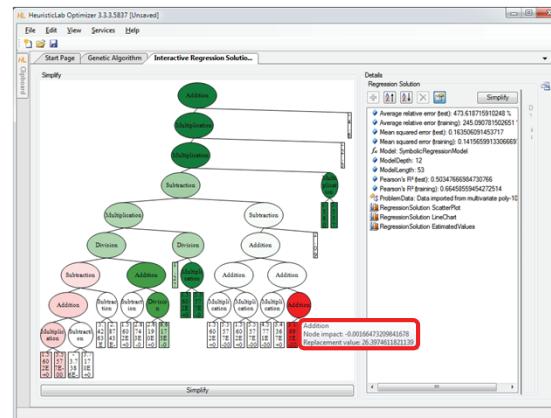
## Detailed Model Analysis and Simplification



87



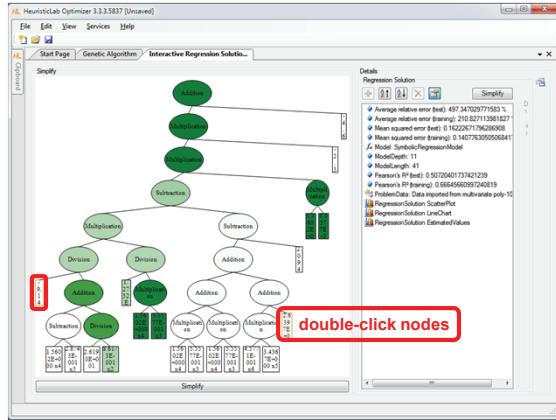
## Symbolic Simplification and Node Impacts



88



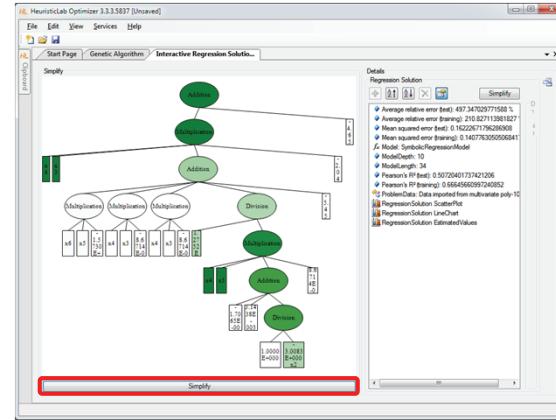
## Manual Simplification



89



## Automatic Symbolic Simplification



90



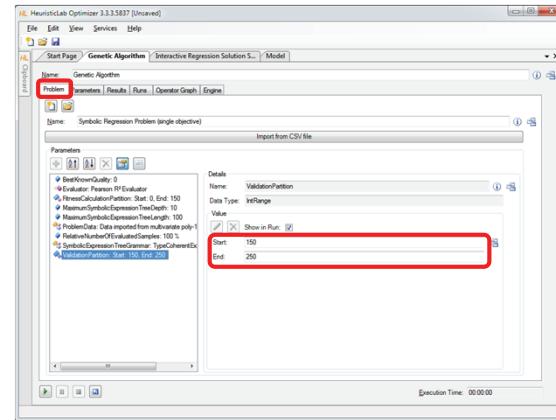
## LaTeX Export

A screenshot of the HeuristicLab Optimizer interface. A large text area on the left shows a complex mathematical equation in LaTeX format. Below the equation, there are line numbers from 1 to 293, corresponding to each line of the LaTeX code. The right side of the screen shows a "Model" tab with some parameters and values.

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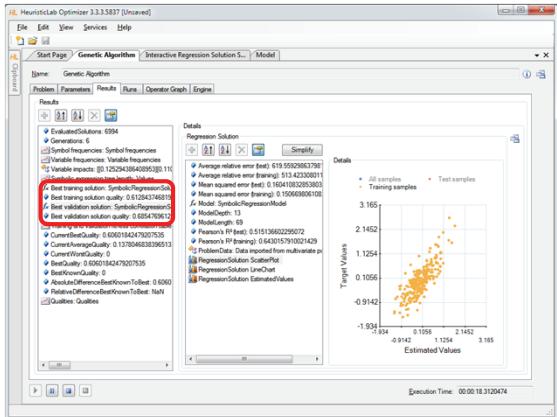
## Configuration of Validation Partition



92



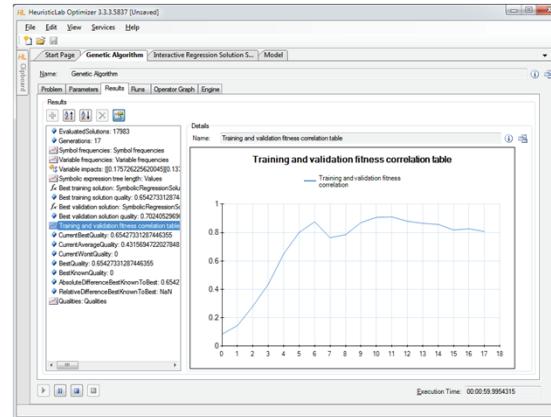
## Inspect Best Model on Validation Partition



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## Inspect Linechart of Correlation of Training and Validation Fitness



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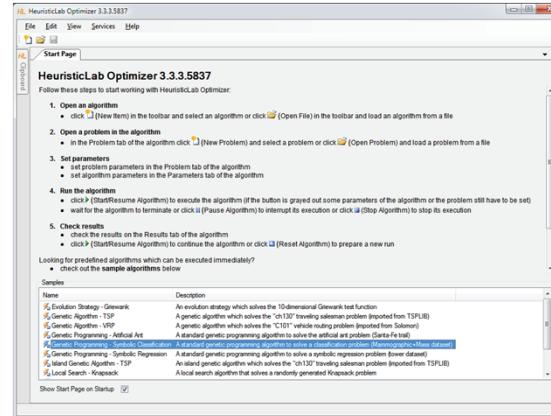
## Case study: Classification

- ❖ Real world medical dataset (*Mammographic Mass*) from UCI Machine Learning Repository (Frank & Asuncion)
  - data from non-invasive mammography screening
  - variables:
    - patient age
    - visual features of inspected mass lesions: shape, margin, density
  - target variable: severity (malignant, benign)
  - Download:
    - <http://dev.heuristiclab.com/AdditionalMaterial#GECCO2011>

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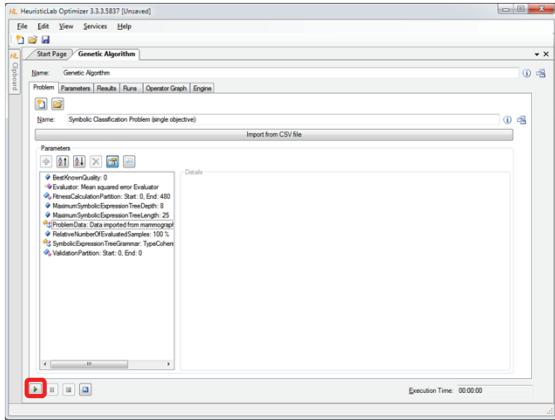
## Open Sample



96



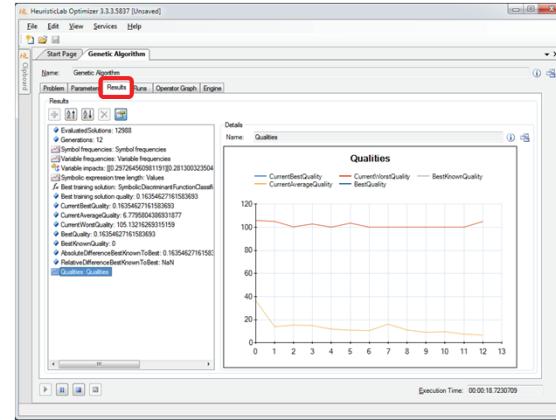
## Configure and Run Algorithm



97



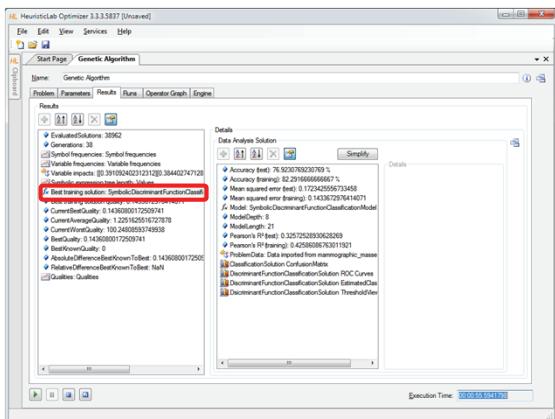
## Inspect Quality Linechart



98



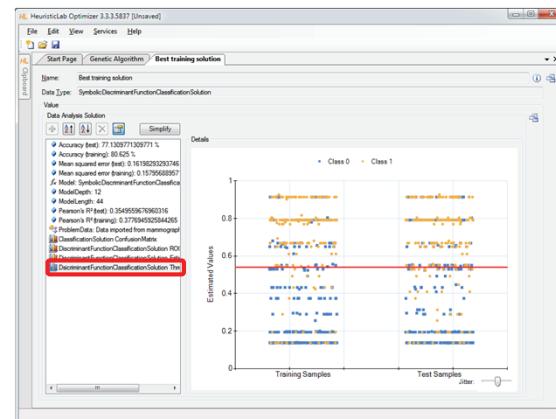
## Inspect Best Training Solution



99



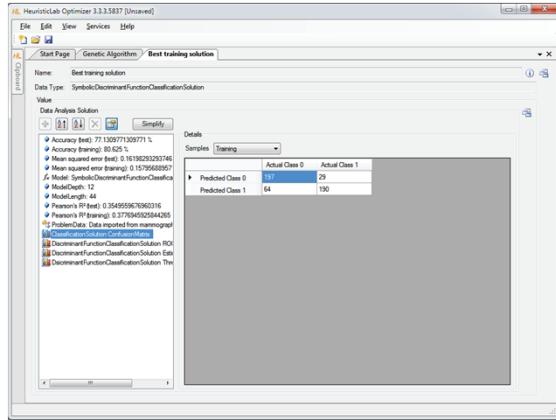
## Inspect Model Output and Thresholds



100



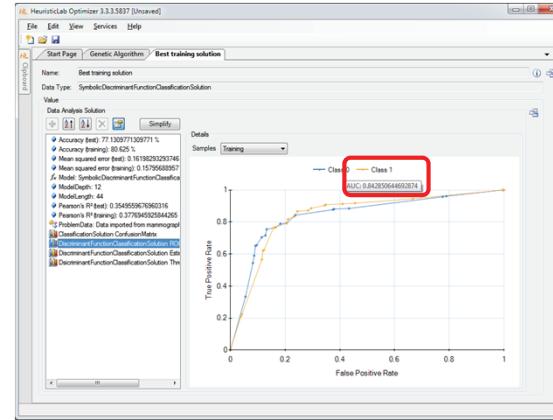
## Inspect Confusion Matrix



101



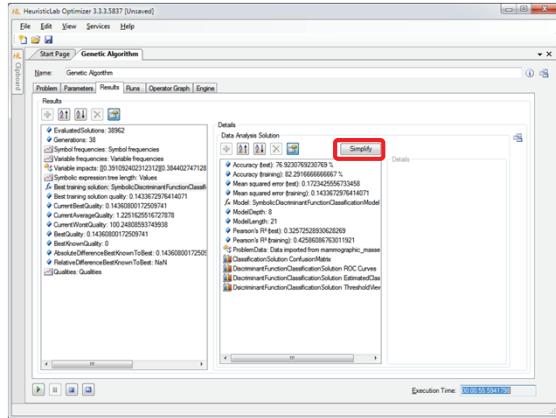
## Inspect ROC curve



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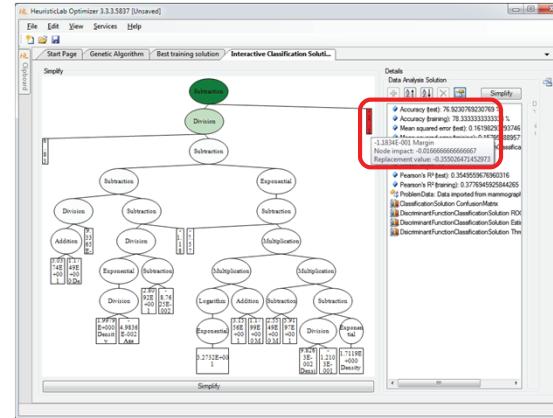
## Analyse and Simplify Best Training Solution



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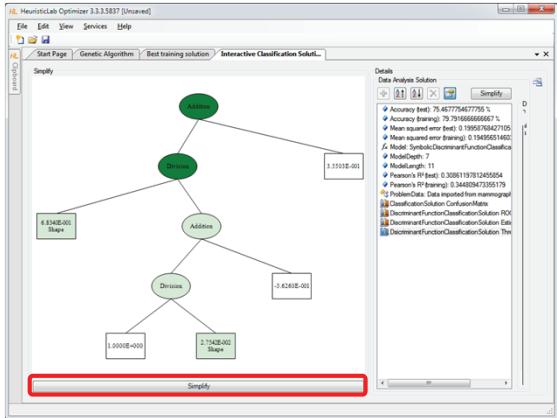
## Analyse and Simplify Model



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## Symbolically Simplified Model



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## Some Additional Features

- ❖ HeuristicLab Hive
  - parallel and distributed execution of algorithms and experiments on many computers in a network
- ❖ Optimization Knowledge Base (OKB)
  - database to store algorithms, problems, parameters and results
  - open to the public
  - open for other frameworks
  - analyze and store characteristics of problem instances and problem classes
- ❖ External solution evaluation and simulation-based optimization
  - interface to couple HeuristicLab with other applications (MatLab, AnyLogic, ...)
  - supports different protocols (command line parameters, TCP, ...)
- ❖ Parameter grid tests and meta-optimization
  - automatically create experiments to test large ranges of parameters
  - apply heuristic optimization algorithms to find optimal parameter settings for heuristic optimization algorithms



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## Planned Features

- ❖ Algorithms & Problems
  - steady-state genetic algorithm
  - unified tabu search for vehicle routing
  - scatter search
  - ...
- ❖ Cloud Computing
  - port HeuristicLab Hive to Windows Azure
- ❖ Linux
  - port HeuristicLab to run on Mono and Linux machines
- ❖ Have a look at the HeuristicLab roadmap
  - <http://dev.heuristiclab.com/trac/hl/core/roadmap>
- ❖ Any other ideas, requests or recommendations?
  - please write an e-mail to support@heuristiclab.com

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## HeuristicLab Team



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AUSTRIA

<http://heal.heuristiclab.com>



Heuristic and Evolutionary  
Algorithms Laboratory



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## Suggested Readings

- ❖ S. Voß, D. Woodruff (Edts.)  
**Optimization Software Class Libraries**  
Kluwer Academic Publishers, 2002



109



## Bibliography

- ❖ S. Wagner, M. Affenzeller  
**HeuristicLab: A generic and extensible optimization environment**  
*Adaptive and Natural Computing Algorithms*, pp. 538-541  
Springer, 2005
- ❖ S. Wagner, S. Winkler, R. Braune, G. Kronberger, A. Beham, M. Affenzeller  
**Briefcase of plugin-based heuristic optimization software systems**  
*Computer-Aided Systems Theory - EUROCAST 2007*, Lecture Notes in Computer Science, vol. 4739, pp. 747-754  
Springer, 2007
- ❖ S. Wagner, G. Kronberger, A. Beham, S. Winkler, M. Affenzeller  
**Modeling of heuristic optimization algorithms**  
*Proceedings of the 20th European Modeling and Simulation Symposium*, pp. 106-111  
DIITEM University of Genova, 2008
- ❖ S. Wagner, G. Kronberger, A. Beham, S. Winkler, M. Affenzeller  
**Model driven rapid prototyping of heuristic optimization algorithms**  
*Computer-Aided Systems Theory - EUROCAST 2009*, Lecture Notes in Computer Science, vol. 5717, pp. 729-736  
Springer, 2009
- ❖ S. Wagner  
**Heuristic optimization software systems - Modeling of heuristic optimization algorithms in the HeuristicLab software environment**  
*Ph.D. thesis*, Johannes Kepler University Linz, Austria, 2009.
- ❖ S. Wagner, A. Beham, G. Kronberger, M. Kommenda, E. Pitzer, M. Kofler, S. Vonolfen, S. Winkler, V. Dorfer, M. Affenzeller  
**HeuristicLab 3.3: A unified approach to metaheuristic optimization**  
*Actas del séptimo congreso español sobre Metaneurísticas, Algoritmos Evolutivos y Bioinspirados (MAEB'2010)*, 2010
- ❖ Detailed list of all publications of the HEAL research group: <http://research.fh-ooe.at/de/orgunit/detail/356#showpublications>

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## Questions & Answers

<http://dev.heuristiclab.com>

[support@heuristiclab.com](mailto:support@heuristiclab.com)

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