

GECCO 2012 Tutorial: Cartesian Genetic Programming



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Abstract



Cartesian Genetic Programming (CGP) is an increasingly popular and efficient form of Genetic Programming that was developed by Julian Miller in 1999 and 2000.

In its classic form, it uses a very simple integer based genetic representation of a program in the form of a directed graph. Graphs are very useful program representations and can be applied to many domains (e.g. electronic circuits, neural networks). In a number of studies, CGP has been shown to be comparatively efficient to other GP techniques. It is also very simple to program.

Since then, the classical form of CGP has been developed made more efficient in various ways. Notably, by including automatically defined functions (modular CGP) and self-modification operators (self-modifying CGP). SMCGP was developed by Julian Miller, Simon Harding and Wolfgang Banzhaf. It uses functions that cause the evolved programs to change themselves as a function of time. Using this technique it is possible to find general solutions to classes of problems and mathematical algorithms (e.g. arbitrary parity, n-bit binary addition, sequences that provably compute pi and e to arbitrary precision, and so on).

The tutorial will cover the basic technique, advanced developments and applications to a variety of problem domains.

Contents

- Classic CGP
- Modular CGP
- Self-modifying CGP
- Developmental CGP
- Cyclic CGP
- Applications
- Resources
- Bibliography



Genetic Programming

- The automatic evolution of computer programs
 - Tree-based, Koza 1992
 - Stack-based, Perkis 1994, Spector 1996 onwards (push-pop GP)
 - Linear GP, Nordin and Banzhaf 1996
 - Cartesian GP, Miller 1997
 - Parallel Distributed GP, Poli 1996
 - Grammatical Evolution, Ryan 1998
 - Lots of others...



Origins of Cartesian Genetic Programming (CGP)

- Grew out of work in the evolution of digital circuits, Miller and Thomson 1997. First actual mention of the term *Cartesian Genetic Programming* appeared at GECCO in 1999.
- Originally, represents programs or circuits as a two dimensional grid of program primitives.
- This is loosely inspired by the architecture of digital circuits called FPGAs (field programmable gate arrays)

What defines CGP?

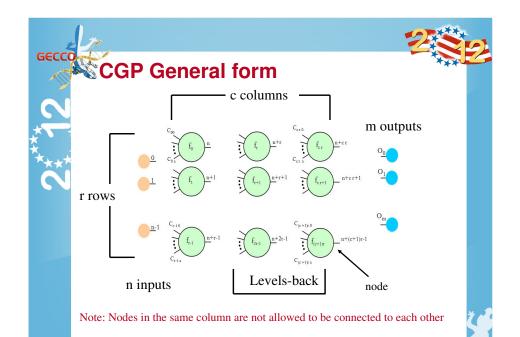


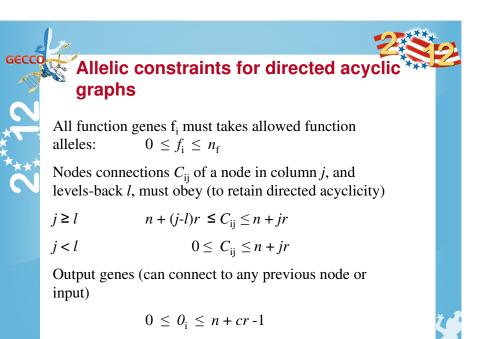
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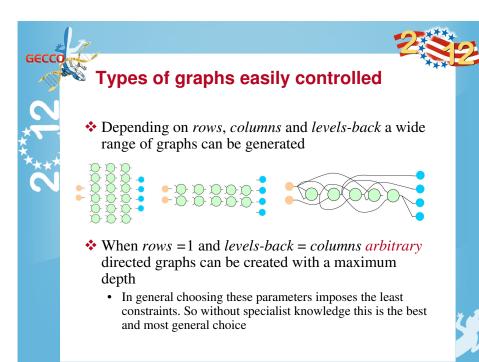
- The genotype is a list of integers (and possibly parameters) that represent the program primitives and how they are connected together
 - CGP represents programs as *graphs* in which there are *non-coding genes*

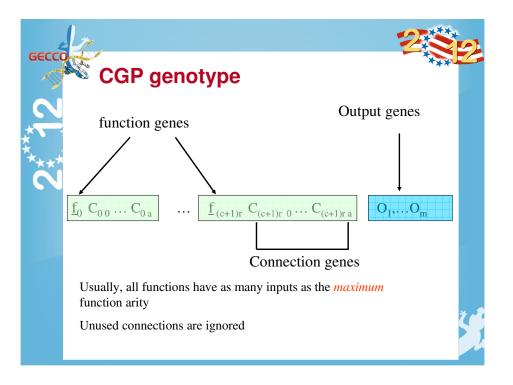
The genes are

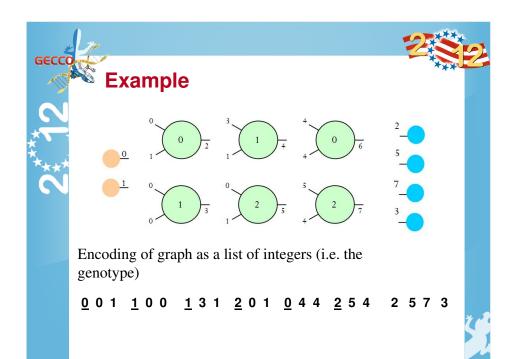
- Addresses in data (connection genes)
- Addresses in a look up table of functions
- Additional parameters
- This representation is very simple, flexible and convenient for many problems

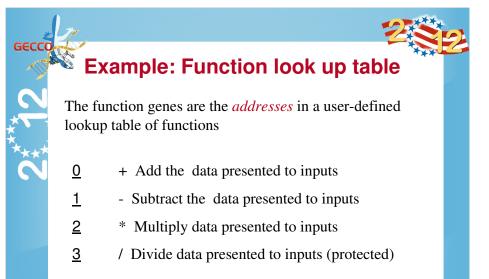


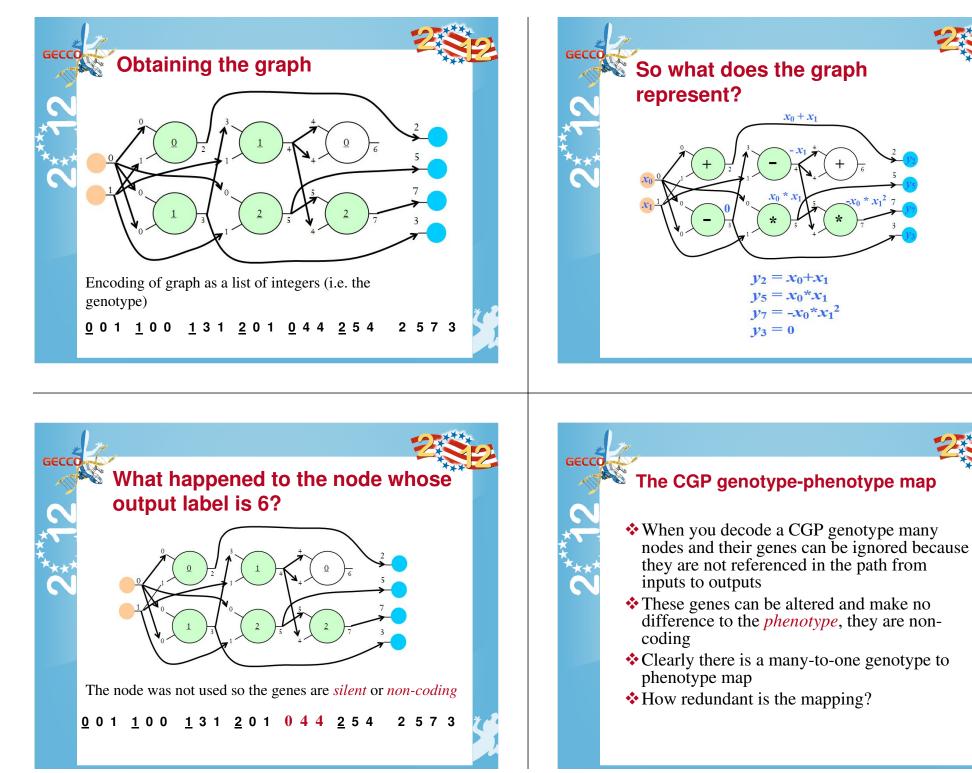














A mathematical aside: CGP and Stirling numbers

- Assume that a CGP graph has the following parameters
- Number of rows_= 1
- $Levels-back = num_cols = n$
- Arity of functions = 1
- There is one input
- * Assume that the output is taken from the last node

$\underline{0} - \underbrace{0}{1} - \underbrace{0}{2} - \underbrace{0}{3} - \underbrace{0}{4} - \underbrace{0}{5} \cdots - \underbrace{N}{6}$

The number of genotypes, *G*, that have a phenotype of size *k*(nodes) can be shown to obey a recurrence relation obeyed by *unsigned Stirling numbers of the first kind*.

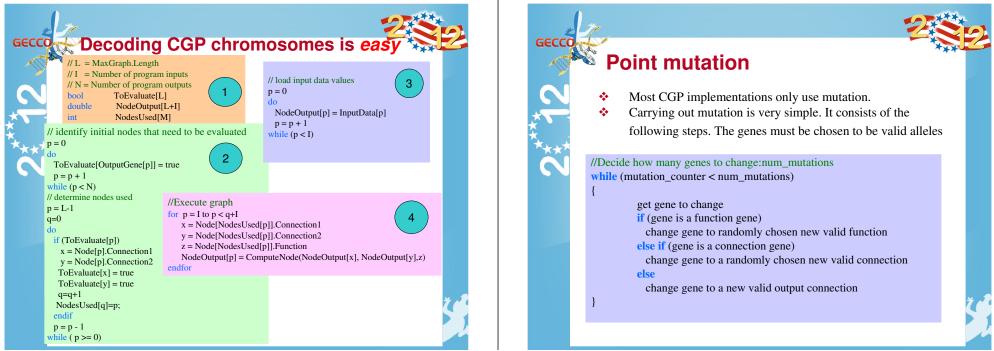
G(n+1, k) = nG(n,k) + G(n, k-1)

How many genotypes of length n map to a phenotypes of length k?

\mathbf{C}			k	5						
	n	1	2	3	4	5	6	7	8	9
	1	1								
***	2	1	1							
\mathbf{C}	3	2	3	1						
	4	6	11	6	1					
	5	24	50	35	10	1				
	6	120	274	225	85	15	1			
	7	720	1764	1624	735	175	21	1		
	8	5040	13068	13132	6759	1960	322	28	1	
	9	40320	109584	118124	67284	22449	4536	546	36	1

Average number of active nodes in a genotype of length 9 is 2.83

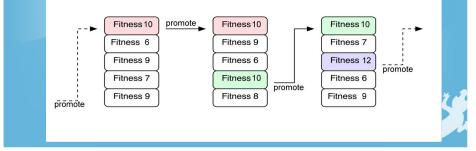
Clearly, with say a genotype of 100 nodes, the number of genotypes that map to a phenotype with say about 10 nodes is an astronomical number



Evolutionary Strategy

GECCO

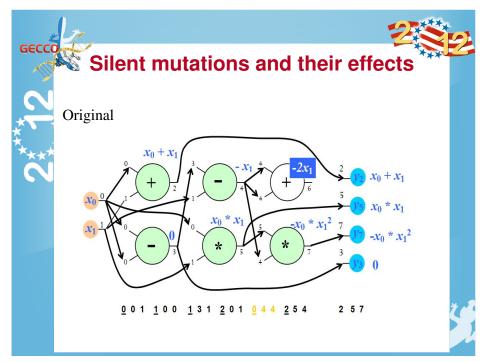
- CGP often uses a variant of a simple algorithm called (1 + 4) Evolutionary Strategy
 - However, an offspring is always chosen if it *is equally as fit* or has better fitness than the parent

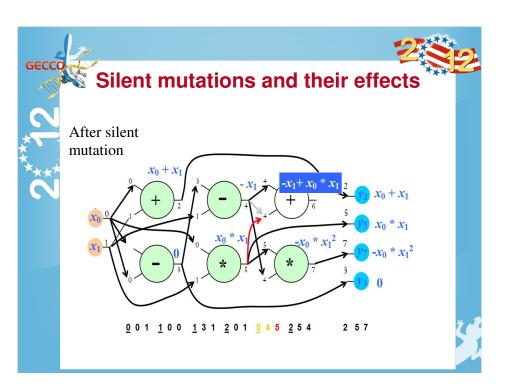


Crossover or not?

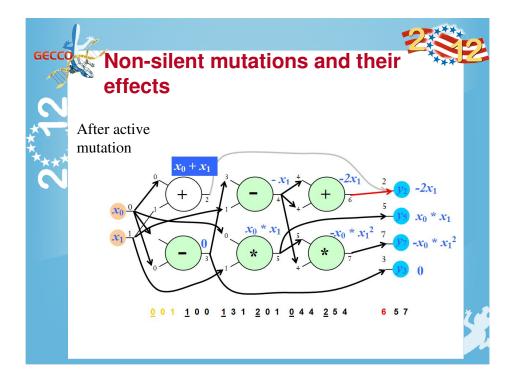
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- Recombination doesn't seem to add anything (Miller 1999, "An empirical study...")
- However if there are multiple chromosomes with independent fitness assessment then it helps a LOT (Walker, Miller, Cavill 2006, Walker, Völk, Smith, Miller, 2009)
- Some work using a floating point representation of CGP has suggested that crossover might be useful (*Clegg, Walker, Miller 2007*)



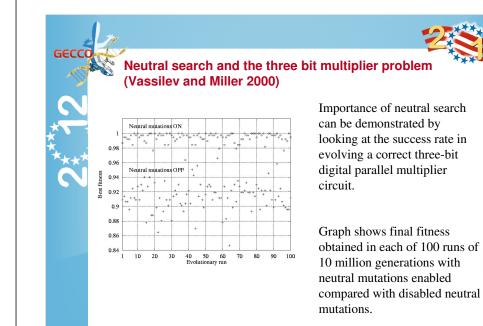


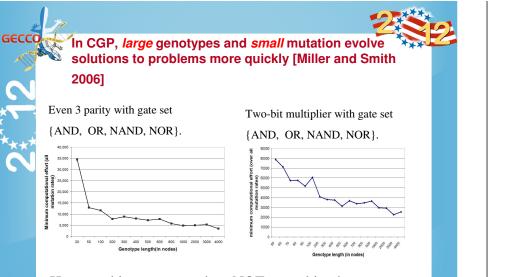
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Neutral search is fundamental to success of CGP

- A number of studies have been carried out to indicate the importance to neutral search
 - Miller and Thomson 2000, Vassilev and Miller 2000, Yu and Miller 2001, Miller and Smith 2006)



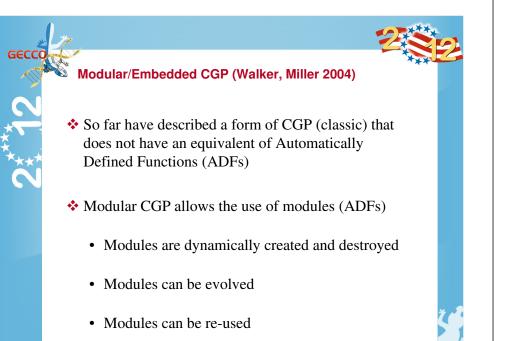


•However big genotypes does NOT mean big phenotypes (programs)....

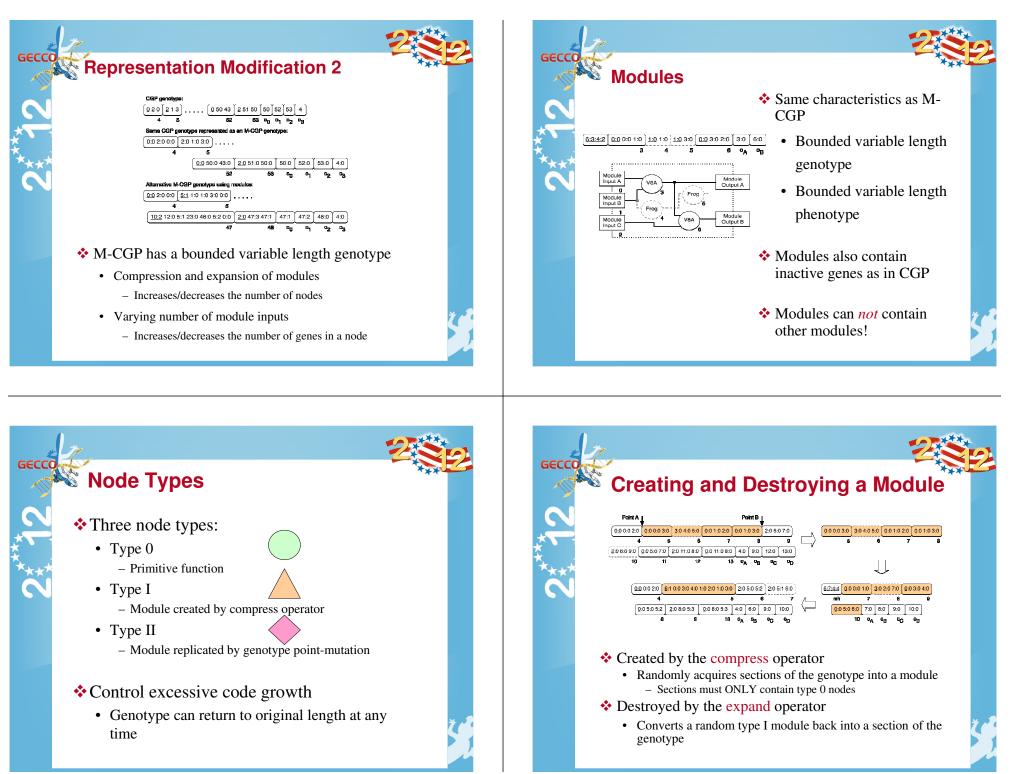
Phenotype length versus genotype length (two-bit multiplier)

Average phenotype length for the initial population contrasted with the average phenotype length at conclusion of evolutionary run versus genotype length with 1% mutation Average proportion of active nodes in genotype at the conclusion of evolutionary run for all mutation rates versus genotype length

SEARCH MOST EFFECTIVE WHEN 95% OF ALL GENES ARE INACTIVE!!



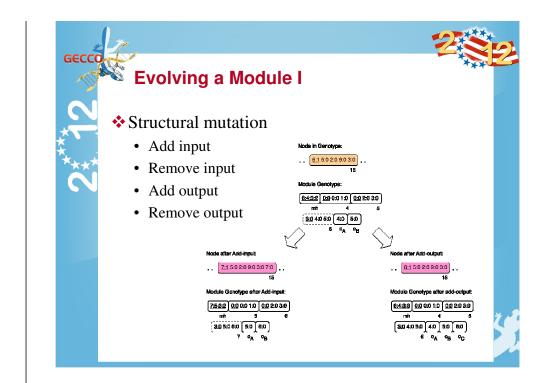
Representation Modification 1 Input 0 gen fn:nt in:00 Output from bFunctio Unction OUTOUT Output o from /-MLCGR Each gene encoded by two integers in M-CGP • Function/module number and node type • Node index and node output - nodes can have multiple outputs

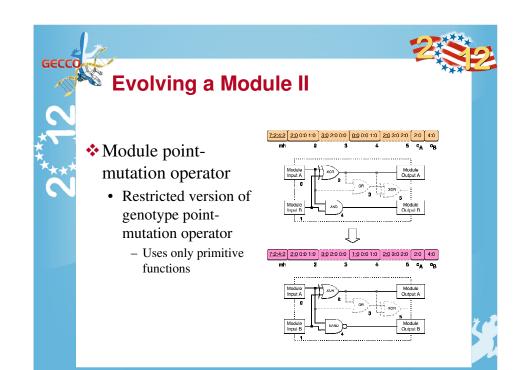


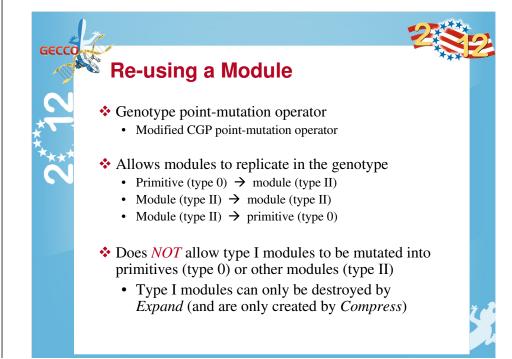
Module Survival

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- Twice the probability of a module being destroyed than created
- Modules have to replicate to improve their chance of survival
 - Lower probability of being removed
- Modules must also be associated with a high fitness genotype in order to survive
 - Offspring inherit the modules of the fittest parent







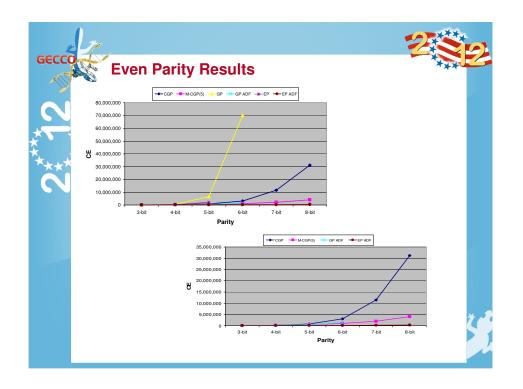
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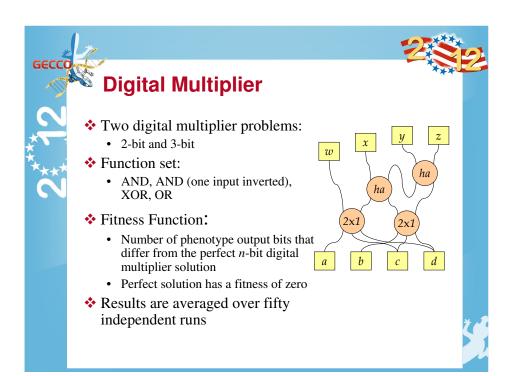
Experimental parameters

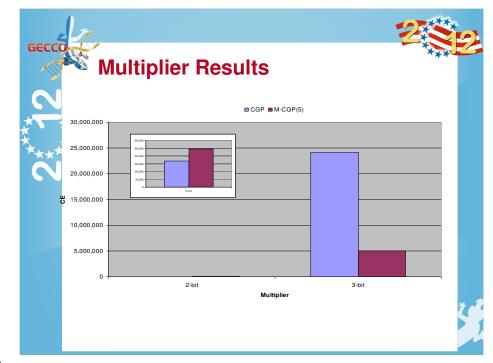
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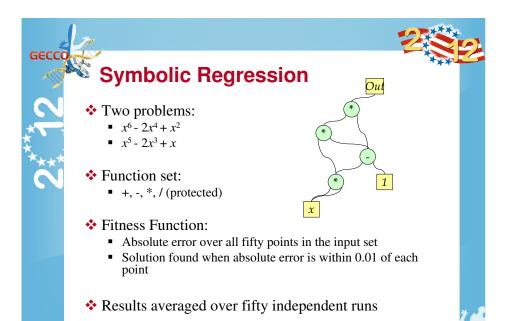
Parameter	Value
Population size	5
Initial genotype size	100 nodes (300 ger
Genotype point mutation rate	3% (9 genes)
Genotype point mutation probability	1
Compress/Expand probability $^\circ$	0.1/0.2
Module point mutation probability $^\circ$	0.04
Add/Remove input probability $^\circ$	0.01/0.02
Add/Remove output probability $^{\diamond}$	0.01/0.02
Module list initial contents $^{\diamond}$	Empty
Number of independent runs	50

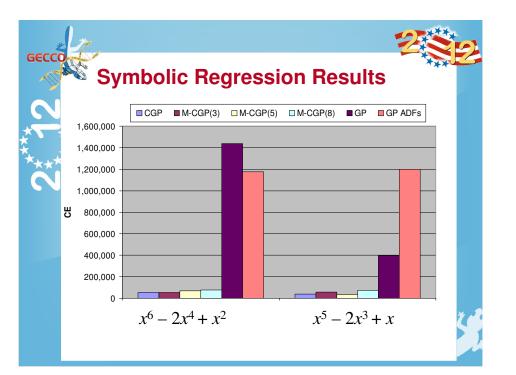
- NOTES: 0 these parameters only apply to Modular (Embedded) CGP
- Results heavily dependent on the maximum number of nodes allowed. Much better results are obtained when larger genotype lengths are used.







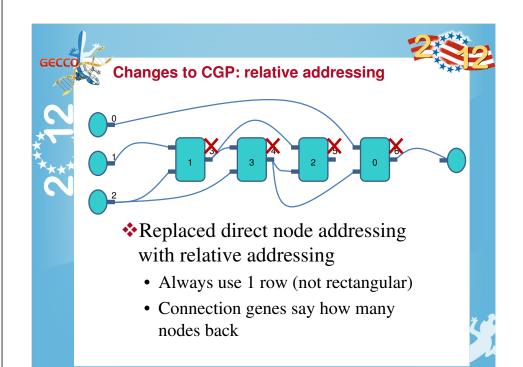


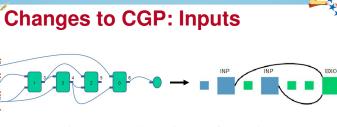


Self-modifying Cartesian Genetic programming

A developmental form of Cartesian Genetic Programming (CGP)

- Includes self modification functions.
- 'General purpose' GP system
- Phenotype can vary over time (with iteration)
- Can switch off its own self-modification

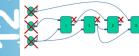




*Replace input calls with a function.

- We call these functions INP, INPP, SKIPINP
- Pointer keeps track of 'current input'.
 - Call to INP returns the current input, and moves the pointer to the next input.
- Connections beyond graph are assigned value 0.

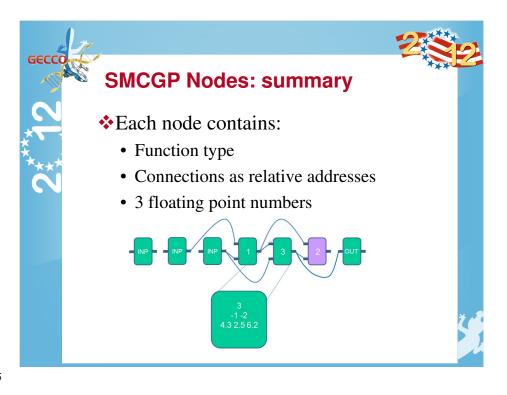




- Removed output nodes.
- Genotype specifies which nodes are outputs.
- If no OUTPUT function then last active node is used
 - Other defaults are used in situations where the number of outputs does not match the number required

Changes to CGP: Arguments

- Nodes also contain a number of 'arguments'.
 - 3 floating point numbers
 - Used in various self-modification instructions
 - Cast to integers when required



SMCGP: Functions

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Two types of functions:

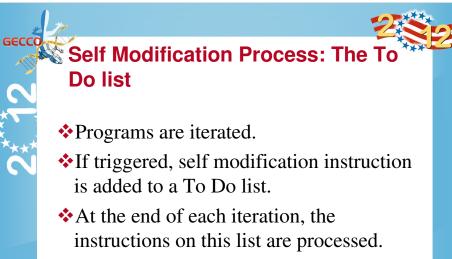
- Computational
 - Usual GP computational functions
- · Self-modifying
 - Passive computational role (see later)

Some Self-Modification Functions				
Operato	r Parameters: use node address and the three node arguments	Function		
MOVE	Start, End, Insert	Moves each of the nodes between Start and End into the position specified by Insert		
DUP	Start, End, Insert	Inserts copies of the nodes between Start and End into the position specified by Insert		
DELETE	Start, End	Deletes the nodes between Start and End indexes		
CHF	Node, New Function	Changes the function of a specified node to the specified function		
CHC	Node, Connection1, Connection2	Changes the connections in the specified node		

SMCGP Execution

Important first step:

- Genotype is duplicated to phenotype.
- Phenotypes are executed:
 - Self modifications are only made to the phenotype.



The maximum size of the To Do list can be predetermined

Computation of a SM node



- Functions are appended to the To Do list if:
 - The first input > the second input.

♦And:

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• The To Do list isn't too big.

Publications using SMCGP

- ♦ General Parity Problem (CEC 2009)
- Mathematical Problems (EuroGP 2009, GECCO 2007)
- ♦ Learning to Learn (GECCO 2009)
- ✤Generating Arbitrary Sequences (GECCO 2007)
- Computing the mathematical constants pi and e (GECCO 2010 in GDS track)
- Contemposities Contemposities Contemposities (GPEM Tenth Anniversary Special Issue, 2010)

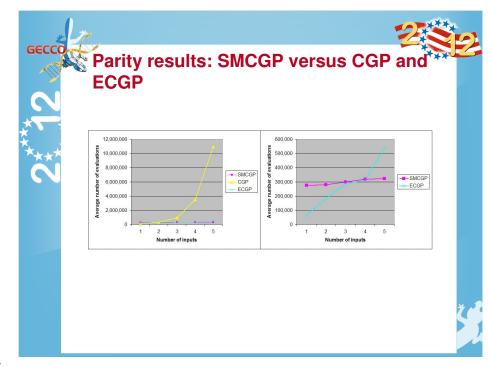
Authors: Harding, Miller, Banzhaf

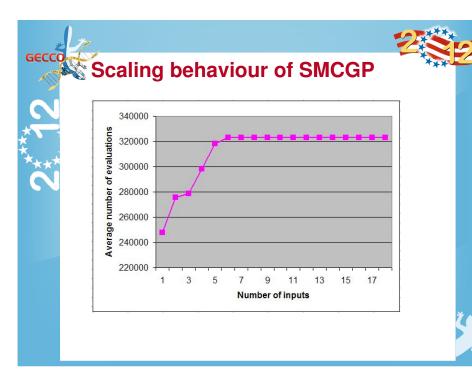
Evolving Parity

- Each iteration of program should produce the next parity circuit.
 - On the first iteration the program has to solve 2 bit parity. On the next iteration, 3 bit ... up to 22 parity
 - Fitness is the cumulative sum of incorrect bits

◆ Aim to find *general* solution

- Solutions can be proved to general
 - See GPEM 2010 paper
- CGP or GP cannot solve this problem as they have a finite set of inputs (terminals)





Evolving pi

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- ✤ Iterate a maximum of 10 times
- If program output does not get closer to pi at the next iteration, the program is stopped and large fitness penalty applied
- Fitness at iteration, *i*, is absolute difference of output at iteration *i* and pi
- ♦ One input: the numeric constant 1.

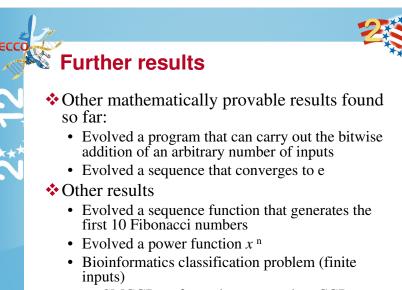
Several Section Evolved Solution

An evolved solution

$$f(i) = \begin{cases} \cos(\sin(\cos(\sin(0)))) & i = 0\\ f(i-1) + \sin(f(i-1)) & i > 0 \end{cases}$$

f(10) is correct to the first 2048 digits of pi

It can be proved that f(i) rapidly converges to pi in the limit as i tends to infinity



- SMCGP performed no worse than CGP

Two dimensional SMCGP (SMCGP2)

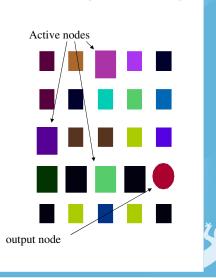
- SMCGP2: genes
 Function
 Connections
 - Connections

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Numeric Constant

Arguments are now

- 2 D vectors
- SM size (SMS)
- SM location (SML)

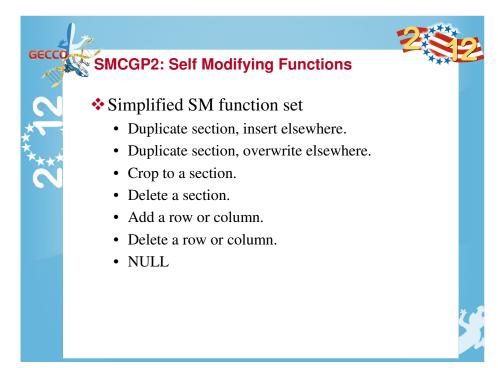


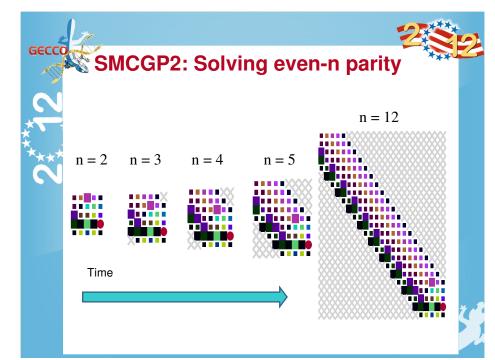
SMCGP2: Vector relative addressing and Empty nodes

There are empty nodes are represented by X

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- The relative address from C to B is (2, 1)
 - meaning 2 nodes to the left, and one node up.
- The relative address of C to A is (4,1).
- Note how the empty nodes are not counted when computing how many nodes back to connect.





SMCGP:Some observations

♦In SMCGP there are implicit

• Loops

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- Recursion
- Modules/functions
- Halting (telomeres)
- Also have "partial" loops/recursion

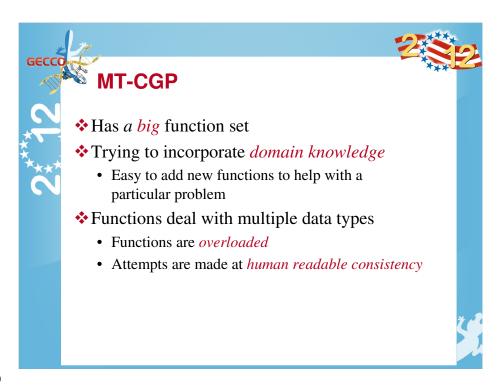
Multi-type CGP (MT-CGP)

- Genotype pretty much classic CGP
 - Genotype is a (partly connected, feed-forward) graph
 - Graph is a list of nodes

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- Each node contains:
 - Function (from a function set)
 - Two connections (to other nodes)
 - real number (to use for parameters)
- ✤ Handles multiple data types
 - So far: reals and vectors
- * Adds lots of functionality
 - Domain knowledge
- See GECCO2012 paper for more details

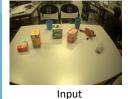
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GECCO	MT-CGP: Example	
2***12	Inputs Evolved program (1,2,3,4) 11 (5,6,7,8) (1,2,3,4) (1,2,3,4) (1,2,3,4) 11 (12,13,14,15) 54 1 55 55 Output value of each node	7 2
		Ż





Evolving Image Filters with CGP

- Detecting/locating objects with the iCub cameras
- * We do this by evolving image filters that take a camera image, and return only the objects we are looking for.

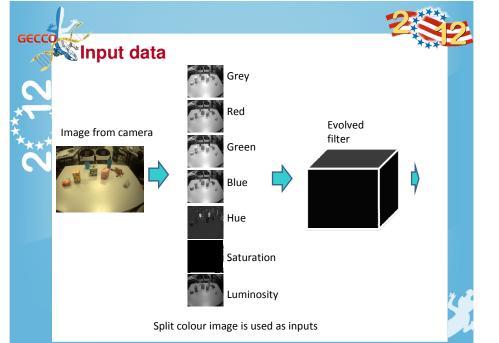


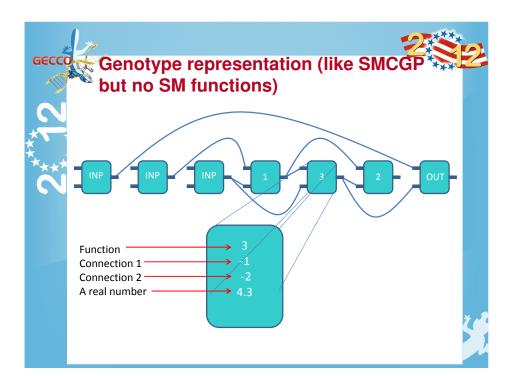




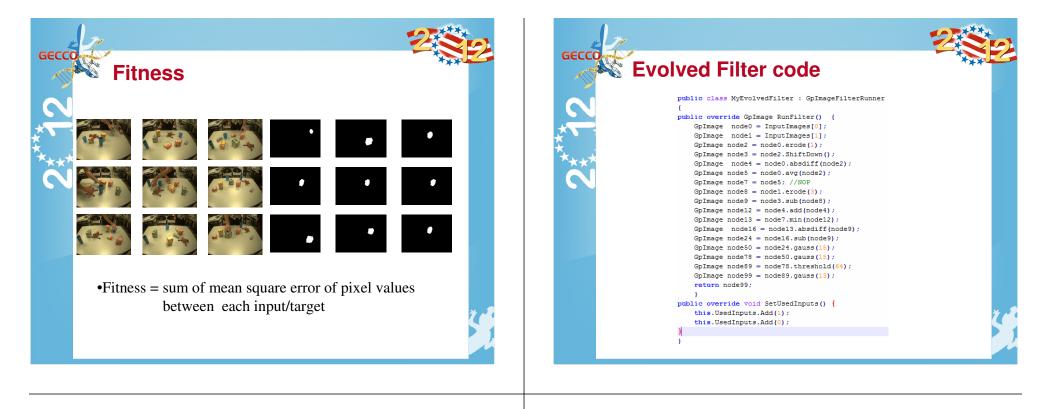
filter



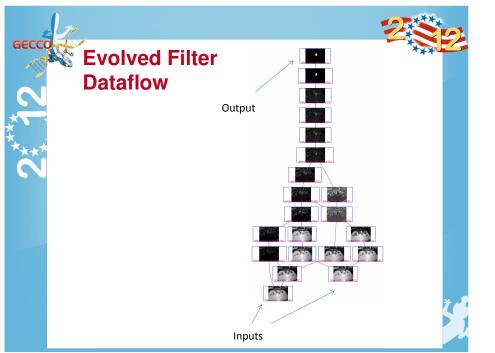




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GECCO	Large Fu	nction Set	- Ara
	NOP	LOG	TRIANGLES
	INP	MAX	LINES
	INPP	MIN	SHIFTDOWN
	SKIP	EQ	SHIFTUP
***	ADD	GAMMA	SHIFTLEFT
	SUB	GAUSS	SHIFTRIGHT
	CONST	SOBELX	SIFTa
	MUL	SOBELY	GABOR
	ADDC	AVG	NORMALIZE
	SUBC	UNSHARPEN	RESCALE
	MULC	THRESHOLD	GRABCUT
	ABSDIFF	THRESHOLDBW	MINVALUE
	CANNY	SMOOTHMEDIAN	MAXVALUE
	DILATE	GOODFEATURESTOTRACK	AVGVALUE
	ERODE	SQUARES	RESCALE
	LAPLACE	CIRCLES	RESIZETHENGABOR



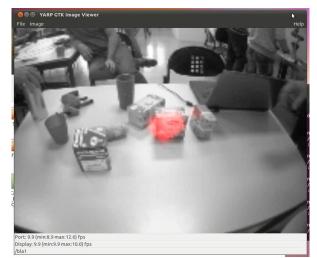
GECC



Things we can do already:

- Generate different filters for other objects.
- Find fast running filters.
- Find them quickly.
- Show that filters are robust.
- Transfer code from offline learning to yarp module.
 - Software emits C# and C++ code
 - Running on Windows/Linux/Mac.

Tea-box filter: demonstration



CGP encoded Artificial Neural Networks (CGPANN)

- CGP has been used to encode both feed-forward ANNs and recursive ANNs. The nodes genes consist of:
 - Connection genes (as usual)
 - Function genes (two)
 - Sigmoid, hyperbolic tangent
- Weights
 - Each connection gene carries a real-numbered weight
- Switch genes
 - Binary genes that switch off or on the connection
- Applied to Markovian and non-Markovian single and double pole-balancing problems
 - Shown to outperform all previously published topology and weights altering evolutionary ANNS (TWEANNS) (*Khan, Khan and Miller* 2010)
- Breast cancer detection (see GECCO 2012 proceedings)

Cyclic CGP



- When outputs are allowed to connect to inputs through a clocked delay (flip-flop) it is possible to allow CGP to include feedback.
- By feeding back outputs generated by CGP to an input, it is possible to get CGP to generate sequences
 - In this way iteration is possible
- There are a couple of recent publications using recursion or iteration in CGP (*Khan*, *Khan and Miller 2010*, *Walker, Liu*, *Tempesti,Tyrrell 2010*)

Applications of CGP Digital Circuit Design ALU, parallel multipliers, digital filters, analogue circuits Mathematical functions Prime generating polynomials Control systems Maintaining control with faulty sensors, helicopter control, general control, simulated robot controller Image processing Image filters Mammary Tumour classification Bio-informatics · Molecular Post-docking filters Artificial Neural Networks Developmental Neural Architectures · Wumpus world, checkers, maze solving Evolutionary Art Artificial Life Regenerating 'organisms' Optimization problems Applying CGP to solve GA problems

CGP Resources

✤ Home site:

Simon Harding

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http://www.evolutioninmaterio.com

SMCGP available at

http://www.cartesiangp.co.uk

http://www.cartesiangp.co.uk

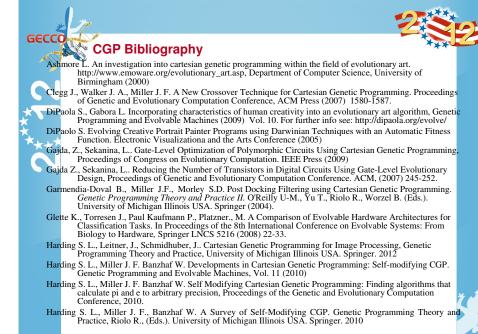
- David Oranchak has implemented CGP in Java. Documentation is available at http://oranchak.com/cgp/doc/
- Cartesian Genetic Programming book
 - Published in 2011 by Springer



Conclusions

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- Cartesian Genetic Programming is a graph based GP method capable of representing many computational structures
 - programs, circuits, neural networks, systems of equations...
- ♦ Genetic encoding is compact, simple and easy to implement and can handle multiple outputs easily.
- ✤ The unique form of genetic redundancy in CGP makes mutational search highly effective
- * The effectiveness of CGP has been compared with many other GP methods and it is very competitive









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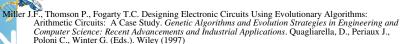
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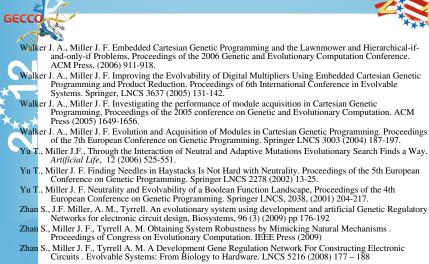


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