

# Enhancing the Differential Evolution with Convergence Speed Controller for Continuous Optimization Problems

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## ABSTRACT

In this paper, we proposed a convergence speed controller (denoted as CSC) framework to improve the performance of differential evolution for continuous optimization problems.

## Categories and Subject Descriptors

G.1.6 [Numerical Analysis]: Optimization—*Global optimization*

## Keywords

convergence speed controller; differential evolution; locally optimal

## 1. SUMMARY

In this paper, we introduced a DE algorithm with convergence speed controller (CSC) framework for continuous optimization problem, which can generally avoid premature convergence. According to the cosine similarity and the relative fitness error between two randomly selected individuals from the DE population, CSC provides a period strategy to detect whether the DE stagnates local optimums. Once the cosine similarity and fitness values are out of the threshold bound, CSC will regenerate the population on the basis of  $N$  top ranking individuals (denoted as  $topN$ ) to protect the DE from premature convergence. Moreover, CSC implements a mechanism for unimproved individuals, which will regenerate the individual on the basis of the best-so-far individual, to accelerate the convergence velocity of the target individual. The test results of 25 standard numerical benchmark functions reveal that the proposed algorithm outperforms three other DE algorithms.

## 2. THE CSC-DE ALGORITHM

The pseudo code of CSC-DE is illustrated by Table 1.

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Table 1: the pseudo code of CSC-DE

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```

{ $x_i \dots$   $i$ -th individual of population}
{ $MaxIte \dots$  maximum number of Iterations }
{ $x_{best} \dots$  the best-so-far solution}
Initialization()
for  $ite = 0; ite < MaxIte; ite = ite + 1$  do
  {**Update the  $topN$ **}
  {**Perform one iteration of the DE**}
  if  $condition1$  is met then
    Run  $Rule1$ : renew  $x_1, x_2, \dots, x_{NP}$  to slow down
    the convergence speed;
  end if
  if  $condition2$  is met then
    Run  $Rule2$ : renew the stopping individual  $x_i$  to
    accelerate the convergence speed;
  end if
  Update  $x_{best}$ 
end for

```

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## 2.1 Initialization

CSC-DE starts with a population of  $NP$   $D$ -dimensional individuals within the search space constrained by the prescribed minimum and maximum bounds  $\vec{X}_{min} = [x_{1,min}, x_{2,min}, \dots, x_{D,min}]$  and  $\vec{X}_{max} = [x_{1,max}, x_{2,max}, \dots, x_{D,max}]$ . The initial value of the  $j$ -th component of the  $i$ -th individual at generation  $G=0$  as

$$x_{i,j,0} = x_{j,min} + rand(0, 1) \cdot (x_{j,max} - x_{j,min}) \quad (1)$$

where  $rand(0, 1)$  is a uniformly distributed random variable within the range  $[0, 1]$ .

## 2.2 History information based $topN$ updating

In order to record the information during the optimization process, we designed a set named  $topN$  which contains  $N$  excellent individuals. Moreover, to make all the individuals in  $topN$  cover a wide search space, the cosine similarity between any two individuals in  $topN$  is set to less than  $sim$  ( $sim$  is a threshold). Given two individuals  $x_a$  and  $x_b$ , their cosine similarity is calculated by Expression (2).

$$cos(x_a, x_b) = \frac{\sum_{j=1}^D x_{a,j} \cdot x_{b,j}}{\sqrt{\sum_{j=1}^D x_{a,j}^2} \cdot \sqrt{\sum_{j=1}^D x_{b,j}^2}} \quad (2)$$

Once CSC-DE detects out that DE falls into a local minima possibly, it can generate a new population according to the information of the individuals in  $topN$ .

### 2.3 Condition 1 and Rule 1

One of the most accepted idea to detect convergence is that individuals of the entire population are very similar in position and fitness to each other. Therefore, we use cosine similarity and the ratio of two randomly selected individuals for the convergence condition. Hence, the condition of convergence detection (condition 1 in Table 1) is designed as Expression (3). The condition of convergence detection (condition 1 in Table 1) is designed as Expression (3).

$$\begin{cases} \cos(x_a, x_b) > sim \\ \frac{|f(x_a) - f(x_b)|}{f(x_a)} < dif \end{cases} \quad (3)$$

where  $sim$  and  $dif$  are threshold values. Index  $a \in \{1, \dots, NP\}$  and  $b \in \{1, \dots, NP\}$  are randomly chosen integers ( $a \neq b$ ).

### 2.4 Condition 2 and Rule 2

Rapid convergence to better solution is regarded as an advantage of DE. Besides Rule 1 plays a role as convergence speed slower, an acceleration of convergence speed is also necessary to make CSC more heuristic and robust. For the acceleration, Rule 2 will be implemented when condition 2 is satisfied. As can be seen from the process of DE algorithm, it may happen that an individual unchanged after a number of iterations. This may slow down the convergence of the algorithm. Therefore, condition 2 is presented as

$$t_i > \tau \quad (4)$$

where the range of index  $i$  is  $\{0, \dots, NP\}$ .  $t_i$  denotes the number of consecutive iterations that the  $i$ th individual has not been improved. And  $\tau$  is a threshold value.

## 3. EXPERIMENTS AND RESULTS

### 3.1 Algorithms Compared and Parametric Set-up

CSC-DE algorithm is tested with twenty-five test problems from CEC-2005 benchmark functions[1]. The performance of the CSC-DE algorithm is compared with the DE/current-to-best/1/bin[2], JADE [3] and MDE- $\rho$ BX [4]. To make the comparison fair, we adopt the best parameter settings from their respective literature.

### 3.2 Results on Numerical Benchmarks

Tables 5 show the mean and the standard deviation of the best-of-run errors for 25 independent runs of each of the four algorithms on 25 benchmark benchmarks. As can be seen, CSC-DE defeated DE/current-to-best/1/bin in almost all functions but  $f_{24}$  and  $f_{25}$ . In short, these simulation results show that CSC-DE can greatly improve the original algorithm's global convergence ability and running accuracy. Compared to all other algorithms, CSC-DE managed to win on 17 functions. It is competitive compared to state-of-the-art algorithms

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**Table 2: MEAN AND STANDARD DEVIATION OF VALUES OBTAINED FROM DE/current-to-best/i/bin, JADE, MDE- $\rho$ BX AND CSC-DE ON 2005 BENCHMARKS WITH D=30.**

	DE/current-to-best/i/bin	JADE	MDE- $\rho$ BX	CSC-DE
f01	0.00E+00 (0.00E+00)	<b>0.00E+00</b> <b>(0.00E+00)</b>	0.00E+00 (0.00E+00)	<b>0.00E+00</b> <b>(0.00E+00)</b>
f02	2.21E-07 (1.858E-07)	1.02E-26 (8.42E-27)	2.40E-08 (8.21E-08)	<b>1.79E-27</b> <b>(5.10E-28)</b>
f03	2.55E+05 (2.05E+05)	<b>1.03E+04</b> <b>(7.07E+03)</b>	1.20E+06 (384621.9)	5.37E+04 (39797.17)
f04	0.010474 (0.011039)	1.72E-09 (5.60E-09)	1.16E+00 (1.65E+00)	<b>1.26E-11</b> <b>(5.21E-11)</b>
f05	3.76E+01 (4.42E+01)	<b>1.19E-07</b> <b>(4.17E-07)</b>	2.86E+03 (4.72E+02)	3.03E+01 (3.00E+01)
f06	9.57E-01 (1.73E+00)	9.35E+00 (2.55E+01)	5.43E+04 (1.50E+05)	<b>2.05E-06</b> <b>(7.08E-06)</b>
f07	5.91E-03 (0.007621)	5.63E+03 (5.60E+03)	1.06E+01 (1.98E+01)	<b>1.18E-03</b> <b>(3.34E-03)</b>
f08	2.10E+01 (4.32E-02)	2.08E+01 (1.93E-01)	2.09E+01 (4.76E-02)	<b>2.00E+01</b> <b>(1.54E-02)</b>
f09	1.14E+02 (6.11E+01)	<b>0.00E+00</b> <b>(0.00E+00)</b>	1.28E+01 (3.63E+00)	1.14E+01 (4.33E+00)
f10	1.92E+02 (1.73E+01)	<b>2.56E+01</b> <b>(4.32E+00)</b>	2.94E+01 (14.1601)	4.23E+01 (12.526)
f11	3.94E+01 (1.82E+00)	2.51E+01 (1.54E+00)	2.58E+01 (6.08E+00)	<b>4.24E+00</b> <b>(1.48E+00)</b>
f12	9.69E+05 (1.03E+05)	6.51E+03 (4.76E+03)	1.14E+04 (8.77E+03)	<b>5.86E+03</b> <b>(6.95E+03)</b>
f13	1.56E+01 (1.13E+00)	<b>1.44E+00</b> <b>(1.47E-01)</b>	2.98E+00 (6.75E-01)	2.83E+00 (4.56E-01)
f14	1.39E+01 (1.37E-01)	1.21E+01 (4.27E-01)	1.21E+01 (1.02E+00)	<b>1.18E+01</b> <b>(2.74E-01)</b>
f15	3.64E+02 (7.95E+01)	3.21E+02 (9.70E+01)	3.20E+02 (5.79E+01)	<b>2.39E+02</b> <b>(2.72E+01)</b>
f16	2.40E+02 (1.01E+02)	1.16E+02 (1.40E+02)	7.74E+01 (9.99E+01)	<b>5.18E+01</b> <b>(7.91E+00)</b>
f17	2.80E+02 (9.34E+01)	1.87E+02 (1.03E+02)	1.71E+02 (2.03E+02)	<b>1.67E+02</b> <b>(1.51E+02)</b>
f18	8.97E+02 (2.88E+01)	9.04E+02 (1.37E+00)	9.15E+02 (5.17E+00)	<b>8.77E+02</b> <b>(4.90E+01)</b>
f19	8.95E+02 (3.20E+01)	9.04E+02 (1.80E-01)	9.14E+02 (3.68E+00)	<b>8.00E+02</b> <b>(3.58E-02)</b>
f20	8.93E+02 (3.47E+01)	9.04E+02 (6.10E-01)	9.11E+02 (2.33E+01)	<b>8.64E+02</b> <b>(5.33E+01)</b>
f21	5.00E+2 (00E+00)	5.00E+02 (1.74E-01)	5.01E+02 (4.81E+00)	<b>5.00E+02</b> <b>(8.20E-03)</b>
f22	9.21E+02 (9.49E+00)	<b>8.56E+02</b> <b>(1.49E+01)</b>	9.02E+02 (1.33E+01)	8.74E+02 (3.70E+01)
f23	6.16E+02 (1.63E+02)	5.34E+02 (1.60E-01)	5.34E+02 (3.46E-01)	<b>5.34E+02</b> <b>(1.27E-03)</b>
f24	<b>2.00E+02</b> <b>(00E+00)</b>	2.00E+02 (1.53E+02)	2.00E+02 (9.17E-05)	2.00E+02 (9.10E-03)
f25	2.10E+02 (5.90E-01)	1.27E+03 (1.20E+01)	<b>2.01E+02</b> <b>(3.61E+00)</b>	2.11E+02 (9.94E-01)

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