

A Clustering Routing Protocol for Wireless Sensor Networks Based on Type-2 Fuzzy Logic and ACO

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Abstract—Aiming at the problem of load balancing and lifetime prolonging for wireless sensor networks (WSNs), and considering complex uncertainties existed in WSNs, this paper proposes a clustering routing protocol CRT2FLACO for WSN based on type-2 fuzzy logic and ant colony optimization (ACO). Specifically, in the cluster set-up phase, a type-2 Mamdani fuzzy logic system (T2MFLS) is built to handle rule uncertainty better and balance the network load, in which three important factors—residual energy, the number of neighbor nodes and the distance to the base station (BS) of a node—are considered as inputs, and the probability of the node to be a candidate cluster head (CH) and the CH competition radius as outputs of our T2MFLS, to select the final CHs; in the steady-state phase, in order to reduce the transmission consumption, all the CHs are linked into a chain using ACO algorithm, then each CH send its data packet to the leader along link, which is a CH eventually transmitting packets to the BS. The simulation results show that the proposed routing protocol can effectively balance network load and reduce the transmission energy consumption of CHs, thus greatly prolong the lifetime of WSN.

Index Terms—Wireless sensor network, clustering algorithm, unequal competition radius, type-2 fuzzy logic, ant colony optimization

I. INTRODUCTION

As a product of the development and combination of the sensor technology, embedded computer technology, wireless communication technology and distributed information processing technology, wireless sensor networks (WSNs) provide a kind of brand-new information acquisition and processing method, and have broad application prospects in military, environmental protection, agriculture and health and other fields [1]. WSN is commonly composed of tiny, cheap, low power consumption sensor nodes which are deployed in monitoring area with wide coverage. The nodes are generally tiny embedded systems, which have relatively weak processing capacity, storage capacity and communication ability, carry energy limited battery and not easy to replace or recharge. Therefore, the main challenge for WSN is balance the network load and reduce the overall energy consumption, and consequently prolong the network lifetime.

To solve this problem, researchers have proposed many routing protocol to extend the life cycle of WSN. In presence, clustering routing protocol is commonly used, in which each cluster is formed by a number of adjacent nodes, consists of

a cluster head (CH) and many cluster members, CHs can be further divided into clusters [2]. The CHs of low level network is the cluster members of a high level network, and the CHs of the top level network communicate with the base station (BS). It is low energy adaptive clustering hierarchy (LEACH) protocol [3] which first suggested clustering routing protocol, the main way of LEACH is to prolong the lifetime of network by balancing the energy consumption of the sensor nodes.

Since the CHs randomly form in LEACH, it easily causes CHs gathering and unevenly distribution etc. To deal with these problem, many scholars have put forward various kinds of improved algorithm [2] to improve the distribution of the CHs, among them many algorithms employ fuzzy logic to handle uncertainties in WSN, such as CHEF [4], CEFL [5], [6], [7], etc. In addition, some scholars adopt multi-hop routing to reduce the data transmission energy consumption, such as EEUC [8], EAUCF [9], IFUC [10]. There are some other improved routing protocols that are based on chain, see PEGASIS [11], PEGASIS-ACO [12], etc.

As an extension of the concept of an ordinary fuzzy set (i.e., a type-1 fuzzy set), the concept of a type-2 fuzzy set was introduced by Zadeh [13]. Type-2 fuzzy sets can handle linguistic uncertainties, just as “Words can mean different things to different people.” The type-2 fuzzy logic system (T2FLS) was first proposed by N. N. Karnik and J. M. Mendel in [14] to deal with rule uncertainties, the detail of the system method was developed in [15]. Since then, type-2 FLSs have been widely used in communication, finance, medicine, control etc [16]–[18]. More recently, type-2 FLSs also have been used for lifetime analysis of WSN in [19] or other applications, e.g. [20]. And last year the authors employed a type-2 Takagi-Sugeno-Kang (TSK) FLS for clustering routing protocol design [21] of WSN, which greatly prolonged the lifetime of WSN and balanced the network load better.

So, as a continuation of the idea in [21], this paper would like to present another clustering routing protocol called CRT2FLACO based on the type-2 fuzzy logic, in which a type-2 Mamdani FLS (T2MFLS) is employed to select the CHs. Specifically, in the first set-up phase, the three important factors—residual energy, the number of neighbor nodes and the distance to BS are taken into consideration as inputs of

our T2MFLS to compute the probability of a node to be a candidate CH and the size of CH competition radius, and then select the final CHs; in the second data-transmission phase, the ant colony optimization (ACO) algorithm is introduced to build a chain to link all the CHs, each CH communicates only with a close neighbor and takes turns transmitting packets to the BS like PEGASIS (Power-Efficient GATHERing in Sensor Information Systems) [11]. This method cut the total transmission distance and balance the network load effectively.

The rest of this paper is organized as follows: Section II gives an overview of related work. The third section describes the system model adopted in the protocol; Section IV introduces the proposed clustering algorithm based on type-2 fuzzy logic (T2FLCA) and multi-hop routing mechanism based on ACO in detail. In the fifth section, we conduct the simulation experiments to evaluate our clustering routing protocol compared with LEACH, PEGASIS and EEUC and present the simulation results. In the last section of this paper, we make a summary and put forward some proposals of our future work.

II. RELATED WORK

In recent years, many clustering protocols and algorithms have been proposed for WSN, and many of them are based on LEACH. In this section, we briefly introduce some of them that are relevant to our protocol.

LEACH [3] is a self-organized clustering protocol, in which the operation is divided into rounds. Each round begins with a set-up phase when the clusters are formed, followed by a steady-phase when data are transmitted from the nodes to the CHs and then on to the BS. In the first set-up phase, each node generates a random number between 0 and 1, if this random number is smaller than a threshold $T(n)$, given in (1), the node becomes a CH in the current round. Other ordinary nodes determine their cluster by choosing the CH that requires the minimum communication energy. In the second steady-phase, the CHs use TDMA (Time Division Multiple Access) to communicate with the nodes in their clusters and fuse the data packet, then transmit the packet to the BS.

$$T(n) = \begin{cases} \frac{P}{1 - P \times (r \bmod \frac{1}{P})} & \text{if } n \in G \\ 0 & \text{otherwise} \end{cases} \quad (1)$$

where, P is the CH probability, r is the number of the current round and G is the set of nodes that have not been CHs in the last $1/P$ rounds.

Fuzzy logic systems (FLSs), which can manipulate the linguistic rules in a natural way, are suitable in respects that the environment or system is not accurate [17], [18], [22]. Due to this, researchers have proposed many protocols based on FLSs [4]–[7], [9], [10]. CEFL [5] is an improved protocol based on LEACH, in which the BS uses a FLS to select CHs based on three descriptors—energy, concentration and centrality. Whereas, [6] uses a FLS to select CHs based on three descriptors—distance to BS, node density and battery level. [4] and [7] are another two algorithms using FLS, and

residual energy and local distance are considered in [4] to build a FLS for CH selection, while in [7], residual energy and centrality of the nodes are used to build the FLS.

So far, the clustering protocols that we mentioned above are all single-hop algorithms, that is, the CHs transmit their data packet to the BS directly. However, there are also many multi-hop algorithms developed in the literatures, such as [8]–[10], in which CHs cooperate with each other to forward their data to the BS, the CHs closer to the BS play the role of relay stations at the same time. EEUC [8] is a distributed competitive unequal clustering algorithm where the CHs are elected by local competition. To address the hot spot problem in multi-hop wireless sensor networks, it wisely organizes the network via unequal clustering and multi-hop routing. In EEUC, every node has a preassigned competitive radius which decreases as its distance to the BS decreases. So the CHs closer to the BS support smaller cluster sizes. EAUCF [9] adjusts the CH radius considering residual energy and the distance to the BS of sensor nodes. IFUC [10] develops another unequal clustering scheme based on fuzzy logic, they also design the inter-cluster routing based on ACO, which makes the hot spot problem alleviated effectively.

Unlike multi-cluster structure, the main idea of PEGASIS [11] is to form a chain linked all the nodes. Based on the chain topology architecture, each node transmits data packet to the neighbor node which is nearer to leader, then the neighbor node fuses the received data and its own data and send the fusion data to its neighbor node. Data moves node by node along the chain, get fused, and eventually arrive in the leader that will transmit it to the BS. Compared with LEACH, PEGASIS extends the network lifetime approximately twice. The success of PEGASIS has brought out many researchers of routing optimization to shorten chain of PEGASIS. Among them, [12] presents an improved algorithm based on ACO, balances the network load effectively.

Many of these proposals consider the improvement on the process of CHs election through a FLS that allows a better estimate of the imprecise knowledge by means of multiple criteria. However, most of them use type-1 FLSs, for which the ability to deal with uncertainty model is relatively limited. Very recently, the authors have proposed a clustering routing protocol named ICT2TSK [21], in which a type-2 TSK FLS is employed to handle rule uncertainties, and a fixed competition radius for each CH is introduced to balance the network, it can prolong the lifetime of WSN greatly and balance the network loads better. For these reasons, in this paper we would like to employ a type-2 Mamdani FLS to deal with rule uncertainties better and use the unequal competition radius for each CH to balance the network load. Furthermore, we will adopt the idea of PEGASIS to build a single-chain using ACO algorithm to link all the CHs, then transmit the fusion data CH by CH via multi-hop routing.

III. SYSTEM MODEL

A. Network model

During the study, we randomly deploy N sensor nodes in a monitored area, and assume that the sensor network has the following characteristics:

- (1) The position of the BS in the sensor network is fixed.
- (2) All nodes are homogeneous, stationary and have the same initial energy.
- (3) All the nodes are randomly deployed in the target area, and can establish the connection with the base station.
- (4) Communication channel is symmetric.

B. Energy consumption model

In LEACH, the first order radio model is utilized for calculating hardware energy dissipation. For comparative purposes, this paper uses the same model. In this model, the energy consumption of radio dissipation of sending data and receiving data are both expressed as E_{elec} ; the free space (d^2 power loss) and the multi-path fading (d^4 power loss) channel models with amplifying index ε_{fs} and ε_{amp} are used respectively; the energy consumption of data fusion is denoted by E_{DA} .

The energy spent of a node that transmits l -bits packet over distance d is:

$$E_{Tx}(l, d) = E_{Tx-elec}(l) + E_{Tx-amp}(l, d) = \begin{cases} E_{elec} * l + \varepsilon_{fs} d^2 * l & d < d_0 \\ E_{elec} * l + \varepsilon_{amp} d^4 * l & d \geq d_0 \end{cases} \quad (2)$$

where $d_0 = \sqrt{\frac{\varepsilon_{fs}}{\varepsilon_{amp}}}$, and the energy consumption of receiving this message is:

$$E_{Rx}(l) = E_{elec} * l \quad (3)$$

IV. THE PROPOSED CLUSTERING ROUTING PROTOCOL CRT2FLACO

In this paper, CHs are selected by the BS in each round using our T2FLCA clustering algorithm. In our opinion, a central control algorithm in the BS will produce better CHs since the BS has a global knowledge about the network. Moreover, the BS usually are many times more powerful than the sensor nodes, and have sufficient memory, power and storage [4].

Strictly speaking, residual energy, location, neighbor nodes density, computing power and mobility of sensor nodes are all factors that we should consider when we choose the CHs. Moreover, the influence of these various factors on CH selection is not the same, so overall consideration and adding some weights is helpful for choosing better CHs. In this paper, we take a compromise between important factors and computation simplicity, and just consider three factors—residual energy, the number of neighbor nodes and the distance to BS of each node—for CHs election. And in order to avoid CHs gathering, we also introduce a strategy of unequal competition radius.

Before the sensor network begins to collect data, the BS broadcasts a control signal of fixed power level to all sensor nodes. According to the strength of the received signal,

sensor nodes can calculate the distance to BS, then send the distance and residual energy information to BS. Similarly, at the beginning of each round, each node reports its residual energy to BS. Based on the received information the BS simulates sensor network and applies the proposed T2FLCA algorithm to calculate the CHs list, then generates and sends control package to each sensor node, and each ordinary node determines which cluster it can join in based on the distance factor, and sends control package and data packet to their CHs. Finally all the CHs are linked into a chain using ACO algorithm, each CH send fusion data packet to the leader along link, and the leader transmits eventually packets to BS.

A. Architecture of a type-2 fuzzy logic system

In this paper, a type-2 Mamdani FLS (T2MFLS) is established by T2FLCA algorithm, including four parts [17]: Fuzzifier, Rules, Inference Engine, Output processing (Type-reducer and Defuzzifier), as shown in Fig. 1.

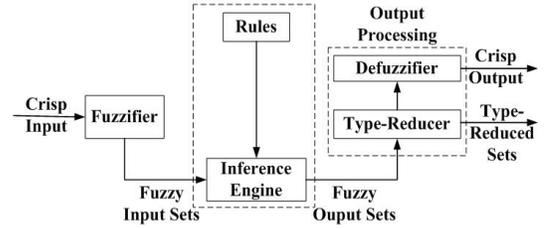


Fig. 1. The structure of a type-2 Mamdani fuzzy logic system

In the algorithm, the input variables include the residual energy, the number of neighbor nodes and the distance to BS of each node; two output variables are the probability of a node becoming the candidate CH and the competition radius of each candidate CH.

1) *Fuzzifier and division of fuzzy variables*: In order to simplify the calculation, we use singleton fuzzifier, that is, for $\forall i = \tilde{1}, \dots, p$, the membership function of the fuzzified input set \tilde{X}_i is defined as [17]:

$$\mu_{\tilde{X}_i}(x_i) = \begin{cases} 1/1 & x_i = x'_i \\ 1/0 & x_i \neq x'_i \end{cases} \quad (4)$$

and $\mu_{\tilde{X}}(\mathbf{x}) = \sqcap_{i=1}^p \mu_{\tilde{X}_i}(x_i)$, where the notation \sqcap denotes the operation of intersection of type-2 fuzzy sets [17].

For convenience, the domains of three inputs are all taken to be the unit interval [0,1]. We get the input values of the residual energy, the number of neighbor nodes and the distance to BS by using the corresponding real values divided by the initial energy, maximum number of neighbor nodes and maximum distance, respectively. To reduce the computation complexity, we divide all the three inputs into three levels, that is, the residual energy (denoted by Energy): *low, medium, high*; the number of neighbor nodes (denoted by Density): *sparse, medium, dense*; the distance to BS (denoted by Distance): *near, medium, far*. All secondary membership functions (MFs) are taken to be interval sets (this means our FLS are interval type-2), and the primary memberships are triangular

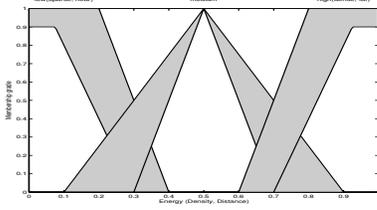


Fig. 2. Membership functions of input variables

TABLE I
RULES

Rule NO.	Input variables			Output variables	
	Energy	Density	Distance	Probability	Radius
1	Low	Sparse	Far	Very weak	Medium
2	Low	Sparse	Medium	Weak	Little small
3	Low	Sparse	Near	Little weak	Little small
4	Low	Medium	Far	Weak	Little small
5	Low	Medium	Medium	Little weak	Little small
6	Low	Medium	Near	Lower medium	Small
7	Low	Dense	Far	Little weak	Little small
8	Low	Dense	Medium	Lower medium	small
9	Low	Dense	Near	Medium	small
...
25	High	Dense	Far	Little strong	Little large
26	High	Dense	Medium	Strong	Medium
27	High	Dense	Near	Very strong	Medium

or trapezoid (see [17] for the concepts of secondary MFs and primary memberships). Besides, we use the same membership functions for the three inputs. Fig. 2 shows the three inputs and their membership functions. The two output variables are the probability of the node becoming the candidate CH (denoted by Probability) and the competition radius of each candidate CH (denoted by Radius). Their domains are the real values. They are divided into nine levels: *very weak*, *weak*, *little weak*, *lower medium*, *medium*, *higher medium*, *little strong*, *strong*, *very strong* and five levels: *small*, *litte small*, *medium*, *little large*, *large*, respectively. We also take triangular or trapezoid primary membership for the two outputs.

2) *Rules*: In our T2MFLS, we establish 27 IF-THEN rules. Let us denote three input variables (Energy, Density and Distance) as x_1 , x_2 and x_3 , respectively, and denote two output variables (Probability and Radius) as y_1 and y_2 , respectively. The basic form of the l th ($l = 1, \dots, 27$) rule can be described as follows:

R^l : IF x_1 is \tilde{F}_1^l , x_2 is \tilde{F}_2^l , x_3 is \tilde{F}_3^l , THEN y_1 is \tilde{G}_1^l , y_2 is \tilde{G}_2^l .

where \tilde{F}_i^l ($i = 1, 2, 3$) are the type-2 antecedent fuzzy sets, \tilde{G}_j^l ($j = 1, 2$) are the type-2 consequent fuzzy sets. Some rules are showed in the TABLE I.

3) *Inference and output processing*: In this paper, we would like to use the center of sets (COS) type-reducer [17]. For the j th ($j = 1, 2$) type-2 fuzzy output set, the COS type-reducer replaces each type-2 consequent set, \tilde{G}_j^l , by its centroid, $C_{\tilde{G}_j^l}$ (which itself is a type-1 set), and finds a weighted average of these centroids. The weight associated with the l th centroid is

the degree of firing corresponding to the l th rule, namely the firing interval. The j th ($j = 1, 2$) extend output $Y_{\text{COS}}^j(\mathbf{x})$ of our T2MFLS is expressed as [17]:

$$Y_{\text{COS}}^j(\mathbf{x}) = [y_{jl}, y_{jr}] = \int_{y_j^1 \in [y_{j1}^1, y_{j1}^1]} \dots \int_{y_j^M \in [y_{j1}^M, y_{j1}^M]} \int_{f^1 \in [\underline{f}^1, \bar{f}^1]} \dots \int_{f^M \in [\underline{f}^M, \bar{f}^M]} 1 / \frac{\sum_{i=1}^M f^i y_j^i}{\sum_{l=1}^M f^l} \quad (5)$$

where $Y_{\text{COS}}^j(\mathbf{x})$ ($j = 1, 2$) is an interval type-1 set determined by its two endpoints, y_{jl} and y_{jr} ; the interval $[y_{j1}^l, y_{j1}^l]$ ($l=1, \dots, 27$) corresponds to the centroid of the type-2 interval consequent set \tilde{G}_j^l ; and $[\underline{f}^l, \bar{f}^l]$ ($l=1, \dots, 27$) is the firing interval of the rule R^l . This extend output can be computed by KM algorithm [17] and it reveals the uncertainty at the output of a T2MFLS due to rule uncertainties. For the detail of COS type-reducer see [17].

Finally, we defuzzify the j th extend output Y_{COS}^j using the average of y_{jl} and y_{jr} , that is, the j th defuzzified output of our T2MFLS is

$$y_j = \frac{y_{jl} + y_{jr}}{2} \quad (6)$$

B. Cluster head selection algorithm

After T2MFLS operation, every node i alive has its probability s_i .probability to be a candidate CH. The node with highest probability is determined to be a CH. If a node become a CH, then the nodes within its competition radius will not be selected as CHs. With the death of the nodes, the number of nodes alive is changing, and the optimal cluster number is changing as well. In this paper, we choose k_{opt} CHs in turn, in which k_{opt} is the optimal cluster number for each round, it is calculated as follows:

$$k_{opt} = \lfloor n * P * (\frac{n - \text{dead}}{n}) + 0.5 \rfloor \quad (7)$$

where n is the number of nodes, and dead is the the number of energy-exhausted nodes, P is the CH probability as in (1).

The pseudocode of CH selection is given in Algorithm 1.

Algorithm 1 Cluster heads selection

```

1: if BS receives nodes' info. then
2:   Compute probability and radius using T2MFLS
3:   node  $i \leftarrow$  alive
4:    $s_i$ .probability,  $s_i$ .radius  $\leftarrow$  T2MFLS( $s_i$ .energy,
5:      $s_i$ .density,  $s_i$ .distance)
6: end if
7: [Pro]=sort([s.probability], 'descend')
8: cluster = 1;  $i = 1$ ;
9: while cluster  $\leq k_{opt} + 1$  do
10:   $Pro(i) \leftarrow$  beClusterHead
11:  cluster = cluster + 1;
12:  if  $d(Pro(i), s_j) < s_{Pro(i)}$ .radius then
13:     $s_j \leftarrow$  noClusterHead
14:  end if
15:   $i = i + 1$ ;
16: end while

```

C. Multi-hop routing mechanism using ACO

After clusters have been formed, the intra-cluster data transmission will begin. In this paper, we adopt the idea of PAGESIS [11], link all the CHs into a chain, however, we do not use the greedy algorithm but the ant colony optimization (ACO) algorithm [23] to form the link, because ACO algorithm has good performance on multi-path optimization problem. Then, each CH send data packet along chain to the leader, which is a CH that eventually transmit packets to the BS.

1) *Chain building using ACO*: At first, for each CH i and each CH j , call $path_{ij}$ the shortest path between CHs i and j . Let $\tau_{ij}(t)$ be the intensity of pheromone trail on $path_{ij}$ at time t . At the beginning (when $t = 0$), $\tau_{ij}(t)$ is set to be the same for each CH i and each CH j , we set it to be 1. We use ANT-cycle algorithm introduced in [23] to update $\tau_{ij}(t)$, that is, $\Delta\tau_{ij}^k$ is not computed at every step, but after a complete tour (nC steps, and nC is the number of CHs).

The value of $\Delta\tau_{ij}^k(t, t + nC)$ is given by:

$$\Delta\tau_{ij}^k(t, t + nC) = \begin{cases} \frac{1 - \frac{L_k}{Q}}{1 + 5\frac{L_k}{Q}}, & \text{if the } k\text{-th ant uses } path_{ij} \\ 0, & \text{otherwise} \end{cases} \quad (8)$$

where L_k is the tour length of the k -th ant, and Q is the maximum of L_k . It worths to mention that the value of the first line in equation (8) in the original ANT-cycle algorithm [23] is defined as $\frac{Q}{L_k}$, where Q is a constant. We modify this value by the Sugeno fuzzy complement operator $\frac{1 - \frac{L_k}{Q}}{1 + 5\frac{L_k}{Q}}$, in which the coefficient 5 is chosen by trial and error. The value of the trail intensity is also updated every nC steps according to the following formula

$$\tau_{ij}(t + nC) = (1 - \rho) \cdot \tau_{ij}(t) + \Delta\tau_{ij}(t, t + nC) \quad (9)$$

in which $\Delta\tau_{ij}(t, t + nC) = \sum_{k=1}^m \Delta\tau_{ij}^k(t, t + nC)$, and ρ is the evaporation rate, we set it to be 0.7 in this paper.

The visibility function η_{ij} is also defined by the same Sugeno fuzzy complement operator:

$$\eta_{ij} = (1 - d_{ij}) / (1 + 5d_{ij}) \quad (10)$$

where d_{ij} is the ratio of the distance between CHs i and j to the maximum distance.

Secondly, there are h ants going to start their travel. At the beginning, each ant is randomly placed in a CH as the starting node to visit other CHs. To take the tour of ant k as an example. When ant k arrives at CH i , we need to calculate the transition probability P_{ij} of CH i to CH j in the set N_i of the nodes that not visited by ant k as follows:

$$P_{ij} = \frac{[\tau_{ij}(t)]^\alpha [\eta_{ij}]^\beta}{\sum_{s \in N_i} [\tau_{is}(t)]^\alpha [\eta_{is}]^\beta} \quad (11)$$

In this paper, we select a CH as the next visiting CH randomly from the set N_{select} which is defined as

$$N_{select} = \{c_j \mid P_{ij} \geq \zeta * \max(P_{ij})\}. \quad (12)$$

ζ is a parameter that dominates the randomness, in this paper we set $\zeta = 0.3$.

Finally, when all the ants finish their journey exactly as ant k does, we have recorded the path of all the ants in "Route[]", calculating the length of all the routes, then memorize the shortest path in $path_{ij}$. After $t = NC_{max}$ iterations as above, we can obtain the final route from $path_{ij}$. In this paper, we set $NC_{max} = 8$.

2) *Leader selection and data transmission*: Unlike PEGASIS, we select a CH nearest to BS as the leader because that CHs have been chosen according to the factor of energy. Under the leader control as PEGASIS, starting from the end CH of the chain, each CH fuses the received data packet (if it has) with its own and transmits its data packet to the next CH along the chain. Ultimately, the BS will receive the final fusion data packet from the leader.

Algorithm 2 shows the pseudocode of multi-hop routing.

Algorithm 2 Multi-hop routing mechanism

```

1: for each edge do
2:   set initial pheromone value  $\tau_{ij}(t) = 1$ 
3: end for
4: for each CH do
5:   compute the visibility  $\eta_{ij}$ 
6: end for
7: while not stop do
8:   for each ant  $k$  do
9:     randomly choose a CH
10:    for  $i=1$  to  $n$  do
11:      compute probability  $P_{ij}$  and select next CH  $j$  with
        probability  $P_{ij}$ 
12:    end for
13:  end for
14:  calculate the route length  $L_k$  of the  $k$ th ant
15:  put the shortest path into  $path_{ij}$ 
16:  for each edge do
17:    update the pheromone value  $\tau_{ij}(t)$ 
18:  end for
19: end while
20: select the shortest path from  $path_{ij}$ 
21: choose the CH nearest to BS as leader
22: for each CH do
23:   send packet under leader control
24: end for

```

V. SIMULATION RESULTS

In this section, we conduct simulation experiments in MATLAB environment, and present the experiment results that we have done to evaluate our protocol CRT2FLACO. We make a comparative analysis with other three protocols named LEACH [3], EEUC [8] and PEGASIS [11].

In [24], Handy et al. use the metrics FND (First Node Dies), HNA (Half of the Nodes Alive) and LND (Last Node Dies) to evaluate the lifetime of WSNs. FND denotes an estimated value for the round in which the first node dies. For some

TABLE II
PARAMETERS OF WSN

Parameters	Value
Initial energy	0.5J
Date packet length	4000 bits
Control packet length	200 bits and 100 bits
$E_{Tx-elec} = E_{Rx-elec}$	50nJ/bit
f_s	10nJ/bit/m ²
amp	0.0013pJ/bit/m ⁴
E_{DA}	5nJ/bit/signal
d_0	87m

sparingly deployed WSNs, data of every sensor node may be of great importance, so the metric FND plays a significant role. However, the death of one node is not an important issue in densely deployed WSNs. Therefore, the metric HNA which denotes an estimated value for the round in which half of the nodes alive is proposed to estimate the WSN lifetime. Additionally, the metric LND denotes an estimated value for the overall lifetime of the network.

In order to evaluate our proposed protocol CRT2FLACO, we consider three different scenarios. We fix the network with dimensions 200m×200m and 200 sensor nodes, and the three scenarios are with different BS locations (100m, 100m), (100m, 250m) and (100m, 400m), respectively.

A. Scenario I

In this scenario, the BS is located at the center (100m, 100m) of the WSN. The parameters of the network model are illustrated in TABLE II. In order to optimize the result of EEUC, in the scenario the maximum competition radius and the distance threshold TD-MAX are set to be 80m and 60m, respectively. LEACH uses a probability of 0.05 and the other related parameters of EEUC and PEGASIS are the same as that in [8] and [11], respectively. Simulation results are as follows.

Fig. 3 shows histograms of FND, HNA and LND graphically and numerically for the four protocols. As shown in the graph, our proposed CRT2FLACO protocol outperforms LEACH, EEUC and PEGASIS for almost all metrics FND, HNA and LND. Fig. 4 shows the alive nodes distributions with respect

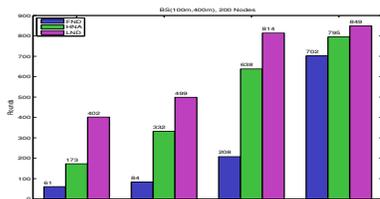


Fig. 3. FND, HNA and LND for BS (100m, 100m)

to the rounds for the four protocols. Fig. 5 compares the energy consumption per round (ECPR) of four protocols. From them we see that the energy consumption of our CRT2FLACO protocol are also the lowest one.

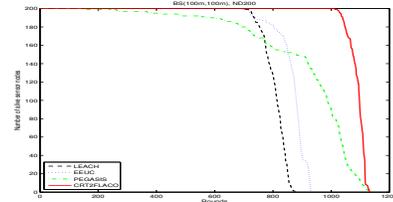


Fig. 4. The number of alive nodes over 1200 rounds for BS (100m, 100m)

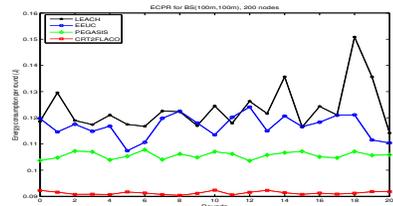


Fig. 5. The amount of energy consumption per round for BS (100m, 100m)

B. Scenario II

In this scenario, the BS is located at (100m, 250m), outside of the WSN, but not very far from it. The parameters of the network model are the same as in TABLE II. The only difference from scenario I is that the distance threshold TD-MAX in EEUC are set to be 150m. Simulation results are as follows.

Fig. 6 shows histograms of FND, HNA and LND graphically and numerically for the four protocols. As shown in the graph, our proposed CRT2FLACO protocol outperforms LEACH, EEUC and PEGASIS for all metrics FND, HNA and LND. Fig. 7 shows the alive nodes distributions with respect to the

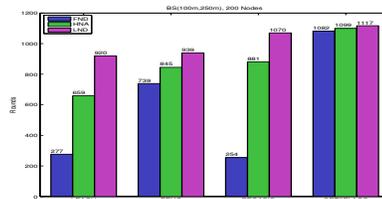


Fig. 6. FND, HNA and LND for BS (100m, 250m)

rounds for the four protocols. Fig. 8 compares the energy consumption per round (ECPR) of four algorithms. From them we see that the energy consumption of our CRT2FLACO protocol are also the lowest one.

C. Scenario III

In this scenario, the BS is located at (100m, 400m), far from the WSN. The parameters of the network model are same as in TABLE II. The only difference from scenario I and II is that the distance threshold TD-MAX in EEUC are set to be 250m. Simulation results are as follows.

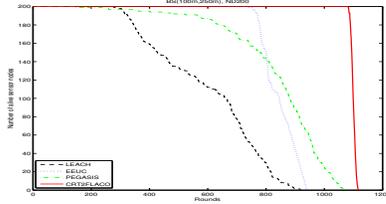


Fig. 7. The number of alive nodes over 1200 rounds for BS (100m, 250m)

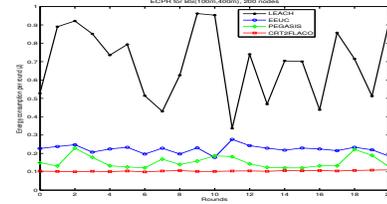


Fig. 11. The amount of energy consumption per round for BS (100m, 400m)

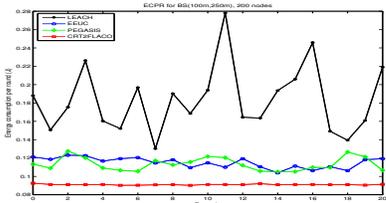


Fig. 8. The amount of energy consumption per round for BS (100m, 250m)

Fig. 9 shows histograms of FND, HNA and LND graphically and numerically for the four protocols. As shown in the graph, our proposed CRT2FLACO protocol outperforms LEACH, EEUC and PEGASIS for all metrics FND, HNA and LND. Fig. 10 shows the alive nodes distributions with respect to the

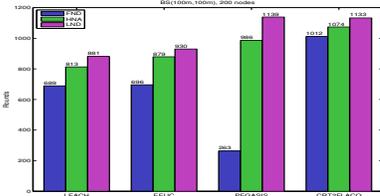


Fig. 9. FND, HNA and LND for BS (100m, 400m)

rounds for the four protocols. Fig. 11 compares the energy consumption per round (ECPR) of four algorithms. From them we see that the energy consumption of our CRT2FLACO protocol are still the lowest one.

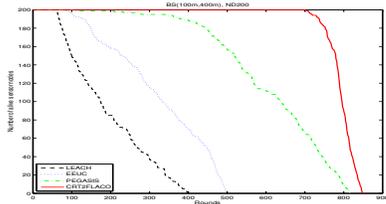


Fig. 10. The number of alive nodes over 900 rounds for BS (100m, 400m)

D. Result analysis

From the above three scenarios of our simulations, we obtain the following observations:

(1) In Scenario III, because of multi-cluster structure and all the CHs send data package to BS that is placed far away from WSN, some CHs consume so much energy that they die prematurely for LEACH and EEUC, while only one node is needed to transmit data to the BS for PEGASIS and CRT2FLACO.

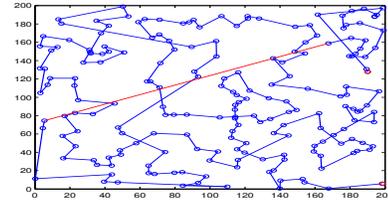


Fig. 12. Long link in the process of chain construction of PEGASIS

(2) In Scenario I and II, the FND of PEGASIS is the minimum one, because in the process of chain construction the inevitability of long link leads to the premature death of some nodes which consume more energy than other nodes. Fig. 12 shows a long link in the process of chain construction of PEGASIS. Although PEGASIS is poorest one for FND, it outperforms LEACH and EEUC for HNA and LND. However, for the three scenarios, LEACH's performance is almost the poorest one, because the method of CHs selection of LEACH is totally random, which causes the CHs distribution is unreasonable, some CHs may bear the heavier load and consume more energy lead to uneven energy consumption of WSN. In addition, the number of CHs per round is not stable, which generates the instability of network.

(3) From the shapes of the curve in Fig. 4, Fig. 7 and Fig. 10, we observe that the remain nodes of our CRT2FLACO protocol will die very fast when the first node dies, which means all the nodes' energy were consumed very averagely. This also shows that our proposed protocol is more balanced compare with the other protocols. From Fig. 5, Fig. 8 and Fig. 11 we see that the ECPR of our CRT2FLACO protocol is lower than any other protocols, and LEACH is the poorest one.

(4) No matter what kind of the three scenarios, our proposed protocol outperforms other three protocols with more lasting lifetime and the best load balancing. Analyzing the reasons, on the one hand, CRT2FLACO comprehensively considers the three important factors of the residual energy, neighbor

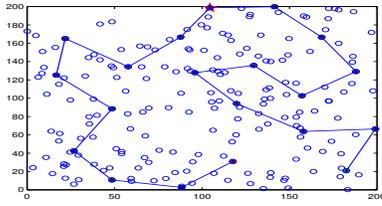


Fig. 13. The CHs distribution and the chain for data transmission of CRT2FLACO for some round

nodes and the distance to the BS of a node to calculate the probability of the node to be the candidate CH. It does not only eliminate the randomness of CHs selection, but also deals with better the uncertainty existed in WSN by using type-2 fuzzy logic; On the other hand, introducing fuzzy competition radius mechanism, CRT2FLACO rules out other candidates CHs in the competition radius of the selected CH, and makes the final CHs distribution more uniform and reasonable. Moreover, inspired by PEGASIS, all the CHs are linked into a chain using ACO algorithm, that not only reduces the energy consumption of CHs transmitting data package to BS, but also balances the energy consumption of CHs. Fig. 13 shows the CHs distribution and the chain of transmitting data of our CRT2FLACO protocol in one round.

VI. CONCLUSION

In order to balance the network load and prolong the lifetime of WSN, this paper proposes a novel clustering routing protocol CRT2FLACO based on type-2 fuzzy logic and ACO. The proposed protocol comprehensively considers the three important factors of residual energy, neighbor nodes and the distance to BS as inputs of a type-2 Mamdani FLS to calculate the probability of a node becoming the candidate CH and the CH competition radius. The use of type-2 fuzzy logic can handle uncertainties existing in WSN better, the introduction of fuzzy unequal competition radius and using multi-hop routing mechanism for data transmission can balance the network load better. Consequently, our CRT2FLACO protocol can effectively balance the network load and prolong the network lifetime greatly. Good performance of our proposed protocol has also been demonstrated by the simulation experiments.

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