

Hyper-heuristics Tutorial

John Woodward (John.Woodward@cs.stir.ac.uk)

CHORDS Research Group, Stirling University
(<http://www.maths.stir.ac.uk/research/groups/chords/>)

Daniel R. Tauritz (dtauritz@acm.org)

Natural Computation Laboratory, Missouri University of Science and Technology (<http://web.mst.edu/~tauritzd/nc-lab/>)

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Instructors

John R. Woodward is a Lecturer at the University of Stirling, within the CHORDS group and is employed on the DAASE project, and for the previous four years was a lecturer with the University of Nottingham. He holds a BSc in Theoretical Physics, an MSc in Cognitive Science and a PhD in Computer Science, all from the University of Birmingham. His research interests include Automated Software Engineering, particularly Search Based Software Engineering, Artificial Intelligence/Machine Learning and in particular Genetic Programming. He has worked in industrial, military, educational and academic settings, and been employed by EDS, CERN and RAF and three UK Universities.



Daniel R. Tauritz is an Associate Professor in the Department of Computer Science at the Missouri University of Science and Technology (S&T), on sabbatical at Sandia National Laboratories for the 2014-2015 academic year, a former Guest Scientist at Los Alamos National Laboratory (LANL), the founding director of S&T's Natural Computation Laboratory, and founding academic director of the LANL/S&T Cyber Security Sciences Institute. He received his Ph.D. in 2002 from Leiden University. His research interests include the design of hyper-heuristics and self-configuring evolutionary algorithms and the application of computational intelligence techniques in cyber security, critical infrastructure protection, and search-based software engineering.



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Conceptual Overview

Combinatorial problem e.g. Travelling Salesman
Exhaustive search -> heuristic?



Genetic Programming
code fragments in for-loops.

Travelling Salesman Instances

TSP algorithm

EXECUTABLE on MANY INSTANCES!!!

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Genetic Algorithm
heuristic – permutations

Travelling Salesman

Tour

Single tour NOT EXECUTABLE!!!

Give a man a fish and he will eat for a day.
Teach a man to fish and he will eat for a lifetime.

Scalable? General?

New domains for GP

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Program Spectrum

Genetic Programming
{+, -, *, /}
{AND, OR, NOT}

First year university course
On Java, as part of a computer
Science degree

Automatically
designed heuristics
(this tutorial)

LARGE
Software
Engineering
Projects

Increasing "complexity"

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Plan: From Evolution to Automatic Design

1. Evolution, Genetic Algorithms and Genetic Programming
2. Motivations (conceptual and theoretical)
3. Examples of Automatic Generation:
 - Evolutionary Algorithms (selection, mutation, crossover)
 - Black Box Search Algorithms
 - Bin packing
 - Evolutionary Programming
4. Visualization
5. Step-by-step guide
6. Wrap up (comparison, history, conclusions, summary, etc.)
7. Questions (during AND after...), please! 😊

Now is a good time to say you are in the wrong room 😊

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Evolution GA/GP

- Generate and test: cars, code, models, proofs, medicine, hypothesis.
- Evolution (select, vary, inherit).
- Fit for purpose

Feedback loop

Humans

Computers

Generate

Test



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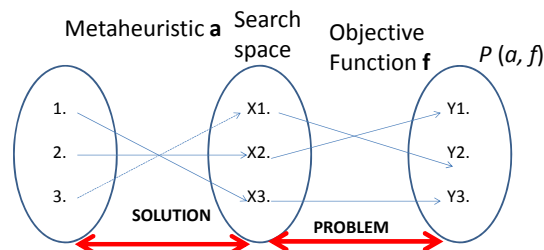
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Inheritance
Off-spring
have similar
Genotype
(phenotype)
PERFECT
CODE [3]

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Theoretical Motivation 1



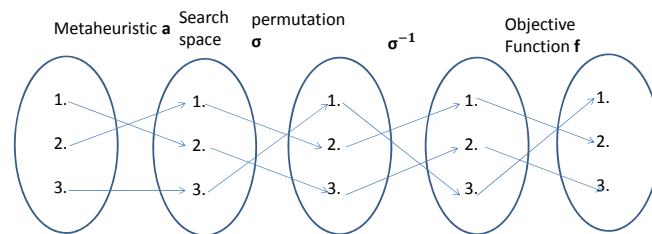
1. A **search space** contains the set of all possible solutions.
2. An **objective function** determines the quality of solution.
3. A (**Mathematical idealized**) **metaheuristic** determines the sampling order (i.e. enumerates i.e. without replacement). It is a (approximate) permutation. What are we learning?
4. **Performance measure** $P(a, f)$ depend only on y_1, y_2, y_3
5. **Aim find a solution with a near-optimal objective value using a Metaheuristic** ANY QUESTIONS BEFORE NEXT SLIDE?

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Theoretical Motivation 2



$$P(a, f) = P(a \sigma, \sigma^{-1} f) \quad P(A, F) = P(A \sigma, \sigma^{-1} F) \text{ (i.e. permute bins)}$$

P is a **performance measure**, (based only on output values).

σ, σ^{-1} are a permutation and inverse permutation.

A and F are probability distributions over algorithms and functions).

F is a **problem class**. **ASSUMPTIONS IMPLICATIONS**

1. Metaheuristic a applied to function $\sigma^{-1} f$ (that is f)

2. Metaheuristic $a\sigma$ applied to function $\sigma^{-1} f$ **precisely identical**.

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Theoretical Motivation 3 [1,14]

- The base-level learns about the function.
- The meta-level learn about the distribution of functions
- The sets do not need to be **finite** (with **infinite sets**, a uniform distribution is not possible)
- The functions do not need to be **computable**.
- We can make claims about the **Kolmogorov Complexity** of the functions and search algorithms.
- $p(f)$ (the probability of sampling a function)is all we can learn in a black-box approach.

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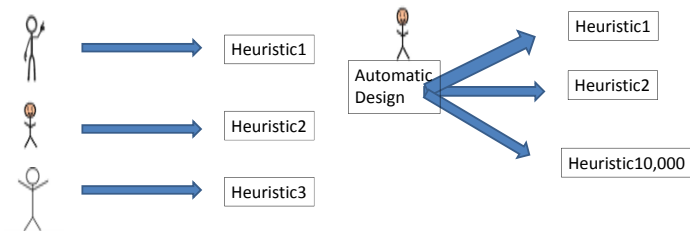
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One Man – One/Many Algorithm

1. Researchers **design heuristics by hand** and test them on problem instances or arbitrary benchmarks off internet.
2. Presenting results at conferences and publishing in journals. In this talk/paper we propose a new algorithm...

1. **Challenge** is defining an algorithmic framework (**set**) that **includes** useful algorithms. **Black art**

2. Let Genetic Programming **select the best algorithm for the problem class at hand**. **Context!!!** Let the data speak for itself without imposing our assumptions. In this talk/paper we propose a 10,000 algorithms...



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Real-World Challenges

- Researchers strive to make algorithms increasingly general-purpose
- But practitioners have very specific needs
- Designing custom algorithms tuned to particular problem instance distributions and/or computational architectures can be very time consuming

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Automated Design of Algorithms

- Addresses the need for custom algorithms
- But due to high computational complexity, only feasible for repeated problem solving
- Hyper-heuristics accomplish automated design of algorithms by searching program space

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Hyper-heuristics

- Hyper-heuristics are a special type of meta-heuristic
 - Step 1: Extract algorithmic primitives from existing algorithms
 - Step 2: Search the space of programs defined by the extracted primitives
- While Genetic Programming (GP) is particularly well suited for executing Step 2, other meta-heuristics can be, and have been, employed
- The type of GP employed matters [24]

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Case Study 1: The Automated Design of Selection Heuristics [16]

- Rank selection**

$$P(i) \propto i$$

Probability of selection is proportional to the **index** in sorted population

- Fitness Proportional**

$$P(i) \propto \text{fitness}(i)$$

Probability of selection is proportional to the **fitness**

Fitter individuals are more likely to be selected in both cases.

Current population (index, fitness, bit-string)

1 5.5 0100010 2 7.5 0101010 3 8.9 0001010 4 9.9 0111010

0001010 0111010 0001010 0100010

Next generation

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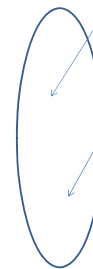
Framework for Selection Heuristics

Selection heuristics operate in the following framework

for all individuals p in population
select p in proportion to $\text{value}(p)$;

- To perform rank selection replace value with index i .
- To perform fitness proportional selection replace value with fitness

Space of Programs.



rank selection is the program.

fitness proportional

- These are just two programs in our search space.

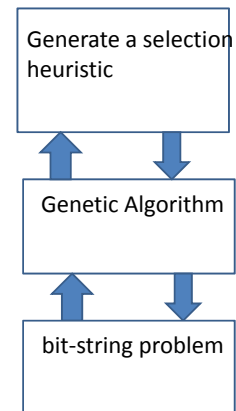
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Selection Heuristic Evaluation

- Selection heuristics are generated by random search in the top layer.
- heuristics are used as for selection in a GA on a bit-string problem class.
- A value is passed to the upper layer informing it of how well the function performed as a selection heuristic.



Generate and test X2

Program space of selection heuristics

Framework for selection heuristics. Selection function plugs into a Genetic Algorithm

Problem class: A probability distribution Over bit-string problems

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Experiments for Selection

- **Train on 50 problem instances** (i.e. we run a single selection heuristic for 50 runs of a genetic algorithm on a problem instance from our problem class).
- The training times are ignored
 - we **are not comparing** our generation method.
 - we **are comparing** our selection heuristic with rank and fitness proportional selection.
- **Selection heuristics are tested on a second set of 50 problem instances drawn from the same problem class.**

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Problem Classes

1. A problem class is a probability distribution of problem instances.
2. Generate values $N(0,1)$ in interval $[-1,1]$ (if we fall outside this range we regenerate)
3. Interpolate values in range $[0, 2^{\{\text{num-bits}\}-1}]$
4. Target bit string given by Gray coding of interpolated value.

The above 3 steps generate a distribution of target bit strings which are used for hamming distance problem instances. “shifted ones-max”

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Results for Selection Heuristics

	Fitness Proportional	Rank	generated-selector
mean	0.831528	0.907809	0.916088
std dev	0.003095	0.002517	0.006958
min	0.824375	0.902813	0.9025
max	0.838438	0.914688	0.929063

Performing t-test comparisons of fitness-proportional selection and rank selection against generated heuristics resulted in a p-value of better than 10^{-15} in both cases. In both of these cases the generated heuristics outperform the standard selection operators (rank and fit-proportional).

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Take Home Points

- **automatically designing** selection heuristics.
- We should design heuristics for **problem classes** i.e. with a context/niche/setting.
- This approach is **human-competitive** (and human cooperative).
- Meta-bias is necessary if we are to tackle multiple problem instances.
- **Think frameworks** not **individual algorithms** – we don’t want to solve problem instances we want to solve classes (i.e. many instances from the class)!

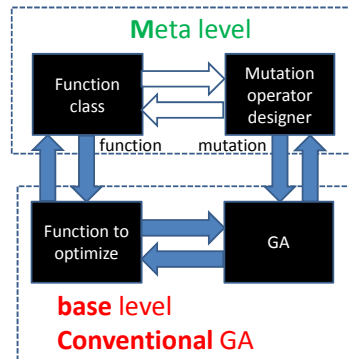
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Meta and Base Learning [15]

1. At the **base** level we are learning about a **specific** function.
2. At the **meta** level we are learning about the probability distribution.
3. We are just doing **"generate and test"** on **"generate and test"**
4. What is being passed with each **blue arrow**?
5. Training/Testing and Validation



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Compare Signatures (Input-Output)

Genetic Algorithm

- $(B^n \rightarrow R) \rightarrow B^n$

Input is an objective function mapping bit-strings of length n to a real-value.

Output is a (near optimal) bit-string i.e. the solution to the problem instance

Genetic Algorithm FACTORY

- $[(B^n \rightarrow R)] \rightarrow ((B^n \rightarrow R) \rightarrow B^n)$

Input is a *list of* functions mapping bit-strings of length n to a real-value (i.e. sample problem instances from the problem class).

Output is a (near optimal) mutation operator for a GA i.e. the solution method (algorithm) to the problem class

We are **raising the level of generality** at which we operate.

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Case Study 2: The Automated Design of Crossover Operators [20]

- Performance Sensitive to Crossover Selection
- Identifying & Configuring Best Traditional Crossover is Time Consuming
- Existing Operators May Be Suboptimal
- Optimal Operator May Change During Evolution

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Some Possible Solutions

- Meta-EA
 - Exceptionally time consuming
- Self-Adaptive Algorithm Selection
 - Limited by algorithms it can choose from

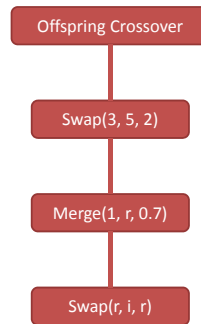
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Self-Configuring Crossover (SCX)

- Each Individual Encodes a Crossover Operator
- Crossovers Encoded as a List of Primitives
 - Swap
 - Merge
- Each Primitive has three parameters
 - Number, Random, or Inline

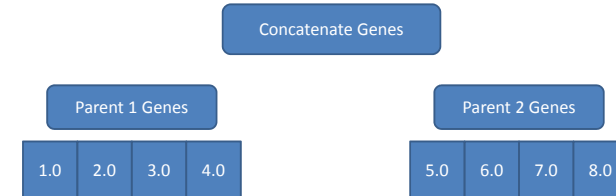


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Applying an SCX



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The Swap Primitive

- Each Primitive has a type
 - Swap represents crossovers that move genetic material
- First Two Parameters
 - Start Position
 - End Position
- Third Parameter Primitive Dependent
 - Swaps use "Width"

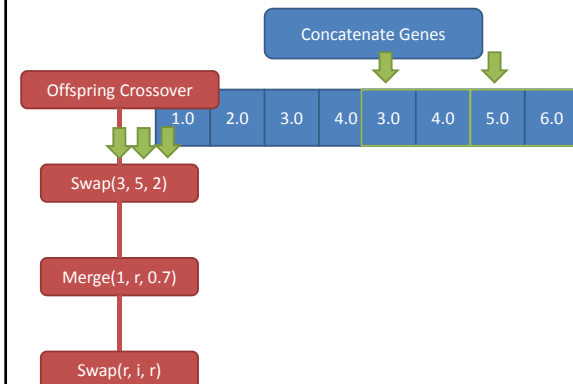


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Applying an SCX



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The Merge Primitive

- Third Parameter Primitive Dependent
 - Merges use “Weight”
- Random Construct
 - All past primitive parameters used the Number construct
 - “r” marks a primitive using the Random Construct
 - Allows primitives to act stochastically

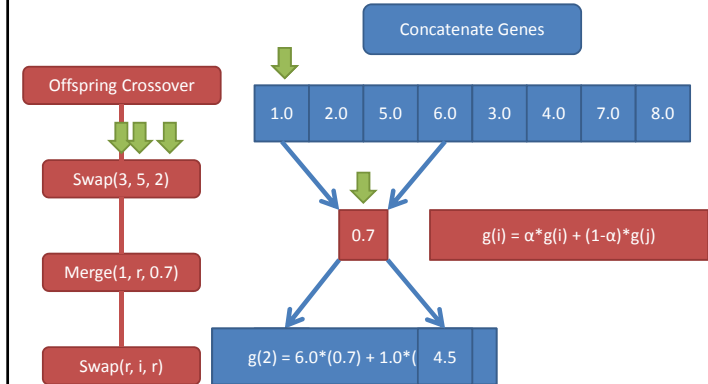
Merge(1, r, 0.7)

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Applying an SCX



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The Inline Construct

- Only Usable by First Two Parameters
- Denoted as “i”
- Forces Primitive to Act on the Same Loci in Both Parents

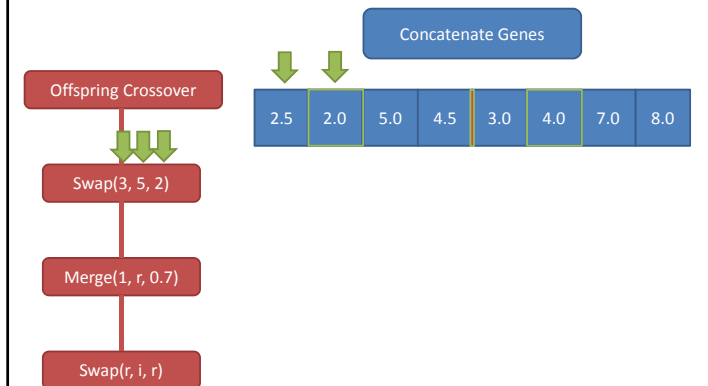
Swap(r, i, r)

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Applying an SCX

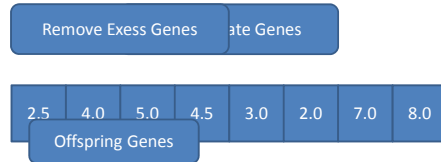


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Applying an SCX

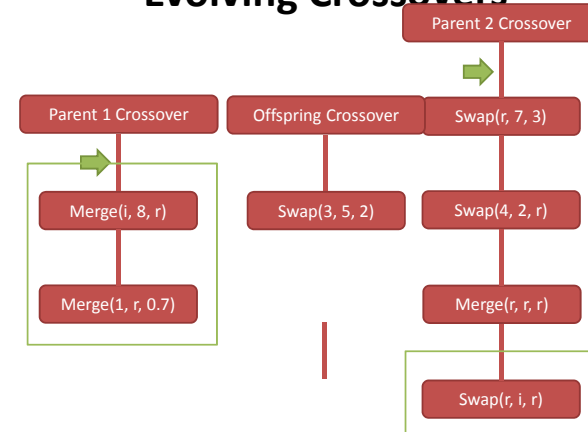


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Evolving Crossovers



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Empirical Quality Assessment

- Compared Against
 - Arithmetic Crossover
 - N-Point Crossover
 - Uniform Crossover

- On Problems
 - Rosenbrock
 - Rastrigin
 - Offset Rastrigin
 - NK-Landscapes
 - DTrap

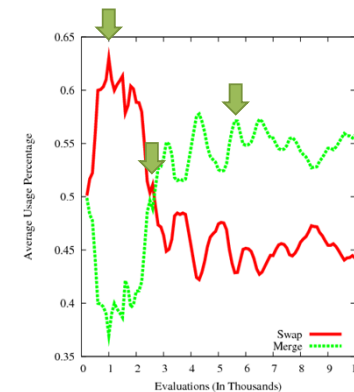
Problem	Comparison	SCX
Rosenbrock	-86.94 (54.54)	-26.47 (23.33)
Rastrigin	-59.2 (6.998)	-0.0088 (0.021)
Offset Rastrigin	-0.1175 (0.116)	-0.03 (0.028)
NK	0.771 (0.011)	0.8016 (0.013)
DTrap	0.9782 (0.005)	0.9925 (0.021)

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Adaptations: Rastrigin

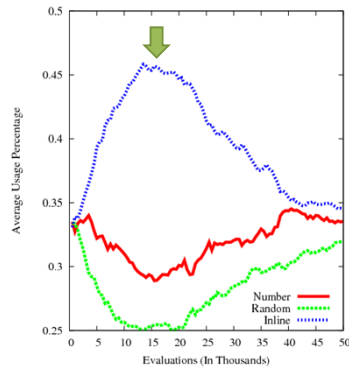


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Adaptations: DTrap



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SCX Overhead

- Requires No Additional Evaluation
- Adds No Significant Increase in Run Time
 - All linear operations
- Adds Initial Crossover Length Parameter
 - Testing showed results fairly insensitive to this parameter
 - Even worst settings tested achieved better results than comparison operators

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Conclusions

- Remove Need to Select Crossover Algorithm
- Better Fitness Without Significant Overhead
- Benefits From Dynamically Changing Operator
- Promising Approach for Evolving Crossover Operators for Additional Representations (e.g., Permutations)

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Additions to Genetic Programming

1. final program is part human constrained part (**for-loop**) machine generated (**body of for-loop**).
2. In GP the initial population is **typically randomly created**. Here we (can) initialize the population with **already known good solutions** (which also confirms that we can express the solutions). (**improving rather than evolving from scratch**) – standing on shoulders of giants. **Like genetically modified crops – we start from existing crops.**
3. Evolving on **problem classes** (samples of problem instances drawn from a problem class) not instances.

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Problem Classes Do Occur

1. Problem classes are probability distributions over problem instances.
2. **Travelling Salesman**
 1. Distribution of cities over different counties
 2. E.g. USA is square, Japan is long and narrow.
3. **Bin Packing & Knapsack Problem**
 1. The items are drawn from some probability distribution.
4. Problem classes do occur in the real-world
5. Next slides demonstrate **problem classes** and **scalability** with on-line bin packing.

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Case Study 3: The Automated Design of Mutation Operators

- **One point mutation** flips **ONE** single bit in the genome (bit-string).

BEFORE
0 1 1 0 0 0

AFTER
0 1 1 0 1 0

(1 point to n point mutation)

- **Uniform mutation** flips **ALL** bits with a **small probability** **p**. No matter how we vary p, it will never be one point mutation.

BEFORE
0 1 1 0 0 0

AFTER
0 0 1 0 0 1

- *Lets invent some more!!!*

- ☹ NO, lets build a general method (for problem class)

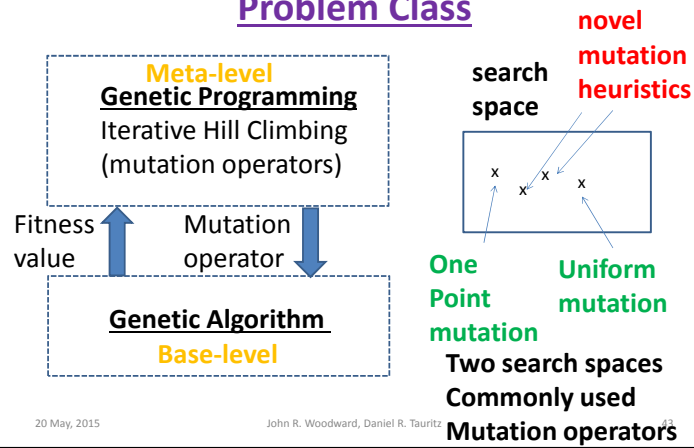
What probability distribution of problem instances are these intended

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Off-the-Shelf metaheuristic to Tailor-Make mutation operators for Problem Class



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Building a Space of Mutation Operators

Inc	0	Program counter		2		
Dec	1	pc				
Add	1,2,3	110	-1	+1	43	...
If	4,5,6	INPUT-OUTPUT REGISTERS				
		-20	-1	+1	20	...

A program is a list of instructions and arguments.

A register is a set of addressable memory (R0,...,R4).

Negative register addresses means **indirection**.

A program can only **affect IO registers indirectly**.

positive (TRUE) negative (FALSE) on output register.

Insert bit-string on IO register, and extract from IO register

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Arithmetic Instructions

These instructions perform arithmetic operations on the registers.

- **Add** $R_i \leftarrow R_j + R_k$
- **Inc** $R_i \leftarrow R_i + 1$
- **Dec** $R_i \leftarrow R_i - 1$
- **lvt** $R_i \leftarrow -1 * R_i$
- **Clr** $R_i \leftarrow 0$
- **Rnd** $R_i \leftarrow \text{Random}([-1, +1])$ //mutation rate
- **Set** $R_i \leftarrow \text{value}$
- **Nop** //no operation or identity

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Control-Flow Instructions

These instructions control flow (NOT ARITHMETIC). They include branching and iterative imperatives.

Note that this set is *not Turing Complete*!

- **If** if($R_i > R_j$) $pc = pc + |R_k|$ why modulus?
- **IfRand** if($R_i < 100 * \text{random}[0,+1]$) $pc = pc + R_j$ //allows us to build mutation probabilities WHY?
- **Rpt** Repeat $|R_i|$ times next $|R_j|$ instruction
- **Stp** terminate

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Expressing Mutation Operators

Line	UNIFORM	ONE POINT MUTATION	
• 0	Rpt, 33, 18	Rpt, 33, 18	• Uniform mutation
• 1	Nop	Nop	Flips all bits with a
• 2	Nop	Nop	fixed probability.
• 3	Nop	Nop	
• 4	Inc, 3	Inc, 3	4 instructions
• 5	Nop	Nop	• One point mutation
• 6	Nop	Nop	flips a single bit.
• 7	Nop	Nop	
• 8	IfRand, 3, 6	IfRand, 3, 6	6 instructions
• 9	Nop	Nop	Why insert NOP?
• 10	Nop	Nop	We let GP start with these
• 11	Nop	Nop	programs and mutate
• 12	lvt,-3	lvt,-3	them.
• 13	Nop	Stp	
• 14	Nop	Nop	
• 15	Nop	Nop	
• 16	Nop	Nop	

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7 Problem Instances

- Problem instances are drawn from a problem class.
- 7 real-valued functions, we will convert to discrete binary optimisations problems for a GA.

number	function
1	x
2	$\sin^2(x/4 - 16)$
3	$(x - 4) * (x - 12)$
4	$(x * x - 10 * \cos(x))$
5	$\sin(\pi * x / 64 - 4) * \cos(\pi * x / 64 - 12)$
6	$\sin(\pi * \cos(\pi * x / 64 - 12) / 4)$
7	$1 / (1 + x / 64)$

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Function Optimization Problem Classes

1. To test the method we use binary function classes
2. We generate a Normally-distributed value $t = -0.7 + 0.5 N(0, 1)$ in the range $[-1, +1]$.
3. We linearly interpolate the value t from the range $[-1, +1]$ into an integer in the range $[0, 2^{\text{num-bits}} - 1]$, and **convert this into a bit-string t'** .
4. To calculate the fitness of an arbitrary bit-string x , the **hamming distance** between x and the target bit-string t' is calculated (giving a value in the range $[0, \text{numbits}]$). This value is then **fed into one of the 7 functions**.

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Results – 32 bit problems

Problem classes	Uniform	One-point	generated-
Means and standard deviations	Mutation	mutation	mutation
p1 mean	30.82	30.96	31.11
p1 std-dev	0.17	0.14	0.16
p2 mean	951	959.7	984.9
p2 std-dev	9.3	10.7	10.8
p3 mean	506.7	512.2	528.9
p3 std-dev	7.5	6.2	6.4
p4 mean	945.8	954.9	978
p4 std-dev	8.1	8.1	7.2
p5 mean	0.262	0.26	0.298
p5 std-dev	0.009	0.013	0.012
p6 mean	0.432	0.434	0.462
p6 std-dev	0.006	0.006	0.004
p7 mean	0.889	0.89	0.901
p7 std-dev	0.002	0.003	0.002

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Results – 64 bit problems

Problem classes	Uniform	One-point	generated-
Means and stand dev	Mutation	mutation	mutation
p1 mean	55.31	56.08	56.47
p1 std-dev	0.33	0.29	0.33
p2 mean	3064	3141	3168
p2 std-dev	33	35	33
p3 mean	2229	2294	2314
p3 std-dev	31	28	27
p4 mean	3065	3130	3193
p4 std-dev	36	24	28
p5 mean	0.839	0.846	0.861
p5 std-dev	0.012	0.01	0.012
p6 mean	0.643	0.643	0.663
p6 std-dev	0.004	0.004	0.003
p7 mean	0.752	0.7529	0.7684
p7 std-dev	0.0028	0.004	0.0031

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p-values T Test for 32 and 64-bit functions on the 7 problem classes

	32 bit	32 bit	64 bit	64 bit
class	Uniform	One-point	Uniform	One-point
p1	1.98E-08	0.0005683	1.64E-19	1.02E-05
p2	1.21E-18	1.08E-12	1.63E-17	0.00353
p3	1.57E-17	1.65E-14	3.49E-16	0.00722
p4	4.74E-23	1.22E-16	2.35E-21	9.01E-13
p5	9.62E-17	1.67E-15	4.80E-09	4.23E-06
p6	2.54E-27	4.14E-24	3.31E-24	3.64E-28
p7	1.34E-24	3.00E-18	1.45E-28	5.14E-23

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Rebuttal to Reviews

1. Did we test the new mutation operators against standard operators (one-point and uniform mutation) on **different problem classes**?
 - **NO** – the mutation operator is designed (evolved) specifically for that class of problem.
2. Are we taking the **training stage** into account?
 - **NO**, we are just comparing mutation operators in the testing phase – Anyway how could we meaningfully compare “brain power” (manual design) against “processor power” (evolution).
3. Train for all functions – **NO**, we are specializing.

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Case Study 4: The Automated Design of Black Box Search Algorithms [21, 23, 25]

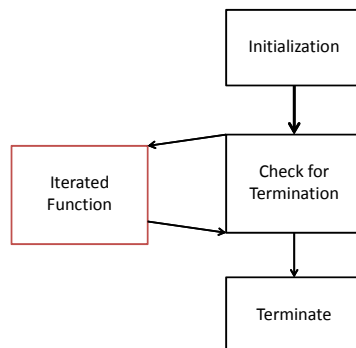
- Hyper-Heuristic employing Genetic Programming
- Post-ordered parse tree
- Evolve the iterated function

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Our Solution



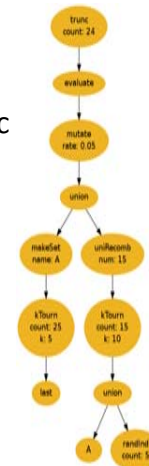
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Our Solution

- Hyper-Heuristic employing Genetic Programming
- Post-ordered parse tree
- Evolve the iterated function
- High-level primitives



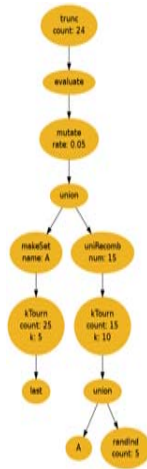
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Parse Tree

- Iterated function
- Sets of solutions
- Function returns a set of solutions accessible to the next iteration



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Primitive Types

- Variation Primitives
- Selection Primitives
- Set Primitives
- Evaluation Primitive
- Terminal Primitives

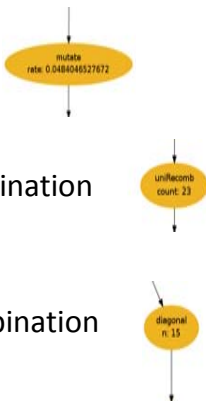
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Variation Primitives

- Bit-flip Mutation
– *rate*
- Uniform Recombination
– *count*
- Diagonal Recombination
– *n*



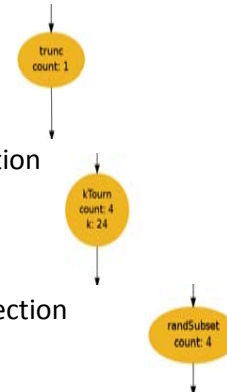
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Selection Primitives

- Truncation Selection
– *count*
- K-Tournament Selection
– *k*
– *count*
- Random Sub-set Selection
– *count*

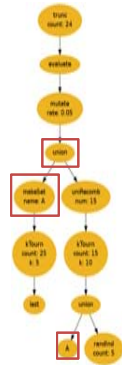


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Set-Operation Primitives



- Make Set
 - *name*
- Persistent Sets
 - *name*
- Union

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Evaluation Primitive

- Evaluates the nodes passed in
- Allows multiple operations and accurate selections within an iteration
 - Allows for deception

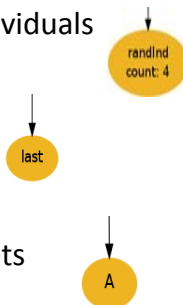
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Terminal Primitives

- Random Individuals
 - *count*
- 'Last' Set
 - *last*
- Persistent Sets
 - *name*

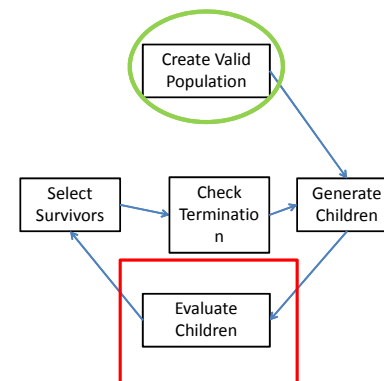


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Meta-Genetic Program

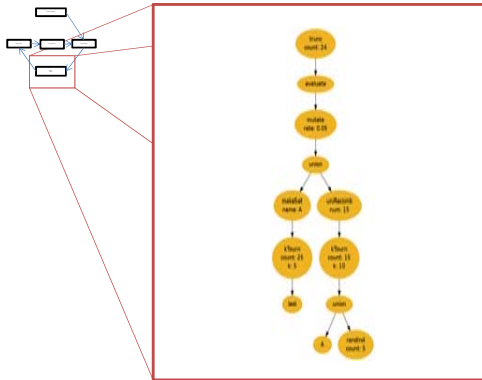


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BBSA Evaluation



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Termination Conditions

- Evaluations
- Iterations
- Operations
- Convergence

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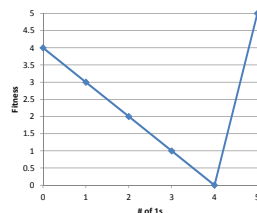
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Proof of Concept Testing

- Deceptive Trap Problem

0	0	1	1	0	1	0	1	1	1	1	1
0				0				0			



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Proof of Concept Testing (cont.)

- Evolved Problem Configuration
 - Bit-length = 100
 - Trap Size = 5
- Verification Problem Configurations
 - Bit-length = 100, Trap Size = 5
 - Bit-length = 200, Trap Size = 5
 - Bit-length = 105, Trap Size = 7
 - Bit-length = 210, Trap Size = 7

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Results

BBSA	EA	Hill-Climber
1	+	+
2	+	+
3	+	+
4	-	-
5	+	+
6	+	+
7	+	+
8	-	-
9	-	-
10	-	-
11	+	+
12	-	-
13	+	+
14	+	+
15	-	-

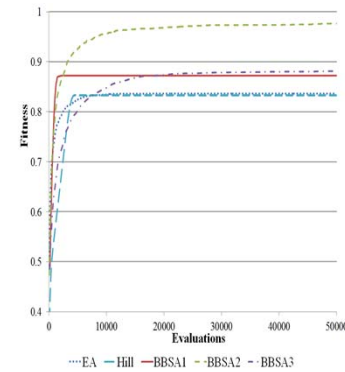
60% Success
Rate

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Results: Bit-Length = 100 Trap Size = 5

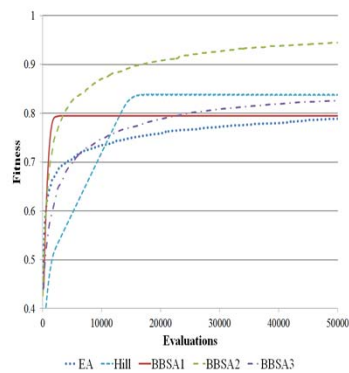


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Results: Bit-Length = 200 Trap Size = 5

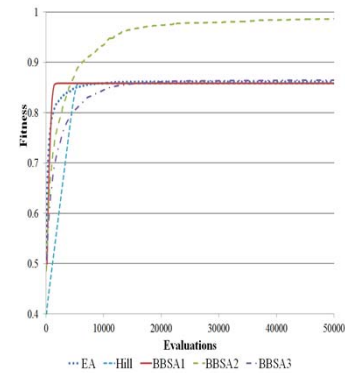


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Results: Bit-Length = 105 Trap Size = 7

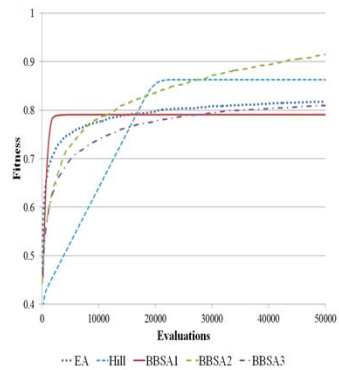


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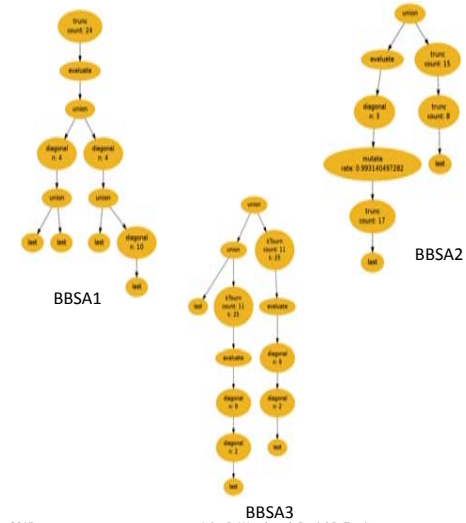
Results: Bit-Length = 210 Trap Size = 7



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Insights

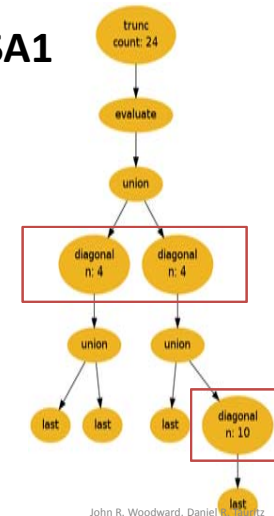
- Diagonal Recombination

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BBSA1

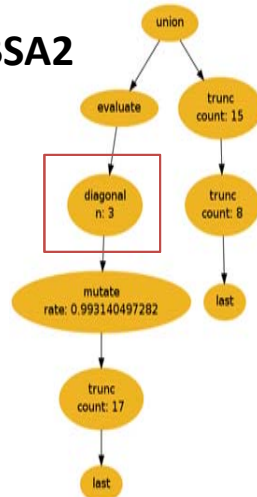


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BBSA2

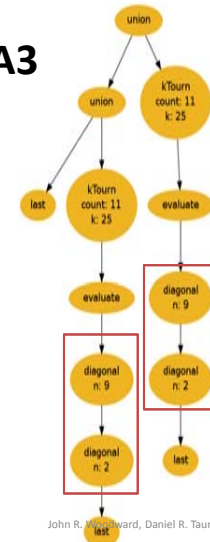


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BBSA3



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Insights

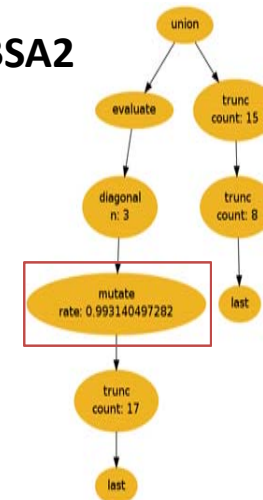
- Diagonal Recombination
- Generalization

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BBSA2



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Insights

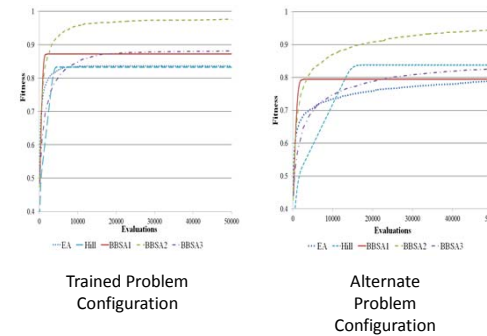
- Diagonal Recombination
- Generalization
- Over-Specialization

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Over-Specialization



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Robustness

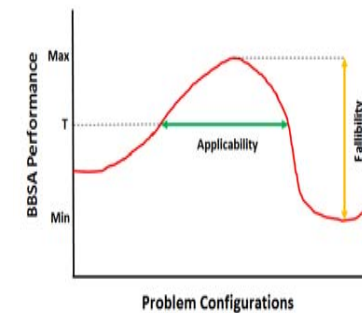
- Measures of Robustness
 - Applicability
 - Fallibility
- Applicability
 - What area of the problem configuration space do I perform well on?
- Fallibility
 - If a given BBSA doesn't perform well, how much worse will I perform?

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Robustness



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Multi-Sampling

- Train on multiple problem configurations
- Results in more robust BBSAs
- Provides the benefit of selecting the region of interest on the problem configuration landscape

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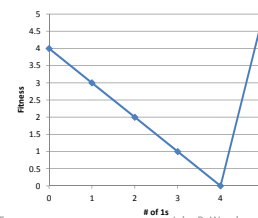
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Multi-Sample Testing

- Deceptive Trap Problem

0 0 1 1	0 1 0 1	1 1 1 1
0	0	0



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Multi-Sample Testing (cont.)

- Multi-Sampling Evolution
 - Levels 1-5
- Training Problem Configurations
 1. Bit-length = 100, Trap Size = 5
 2. Bit-length = 200, Trap Size = 5
 3. Bit-length = 105, Trap Size = 7
 4. Bit-length = 210, Trap Size = 7
 5. Bit-length = 300, Trap Size = 5

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Initial Test Problem Configurations

1. Bit-length = 100, Trap Size = 5
2. Bit-length = 200, Trap Size = 5
3. Bit-length = 105, Trap Size = 7
4. Bit-length = 210, Trap Size = 7
5. Bit-length = 300, Trap Size = 5
6. Bit-length = 99, Trap Size = 9
7. Bit-length = 198, Trap Size = 9
8. Bit-length = 150, Trap Size = 5
9. Bit-length = 250, Trap Size = 5
10. Bit-length = 147, Trap Size = 7
11. Bit-length = 252, Trap Size = 7

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Initial

Level	Run	Train Fit.	Test Fit.	Fallibility
1	1	1.0	0.976	0.094
1	2	1.0	0.999	8.33 E-3
1	3	0.944	0.883	0.082
1	4	0.976	0.894	0.224
2	1	0.997	0.996	0.023
2	2	0.992	0.929	0.130
2	3	0.966	0.970	0.054
2	4	0.979	0.947	0.120
3	1	0.965	0.966	0.050
3	2	0.984	0.980	0.065
3	3	0.899	0.886	0.059
3	4	0.926	0.898	0.073
4	1	0.976	0.999	5.00 E-3
4	2	0.973	0.969	.0903
4	3	0.982	0.975	0.059
4	4	0.993	0.999	5.00 E-3
5	1	0.973	0.977	0.050
5	2	0.893	0.879	0.035
5	3	0.850	0.850	0.045
5	4	0.955	0.986	0.029

Level	Run	+	~	-
1	1	11	0	0
1	2	11	0	0
1	3	11	0	0
1	4	6	2	3
2	1	11	0	0
2	2	11	0	0
2	3	11	0	0
2	4	11	0	0
3	1	11	0	0
3	2	11	0	0
3	3	11	0	0
3	4	11	0	0
4	1	11	0	0
4	2	11	0	0
4	3	11	0	0
4	4	11	0	0
5	1	11	0	0
5	2	10	1	0
5	3	7	4	0
5	4	11	0	0

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Problem Configuration Landscape Analysis

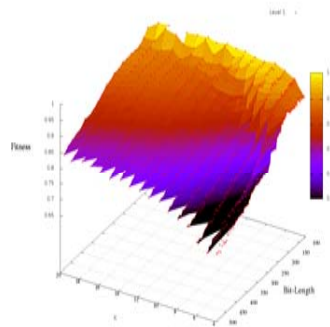
- Run evolved BBSAs on wider set of problem configurations
- Bit-length: ~75~500
- Trap Size: 4-20

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Results: Multi-Sampling Level 1

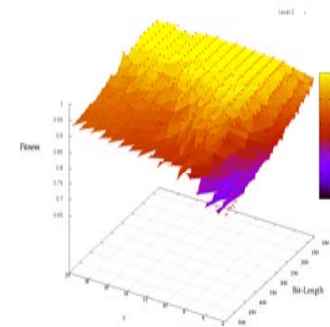


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Results: Multi-Sampling Level 2

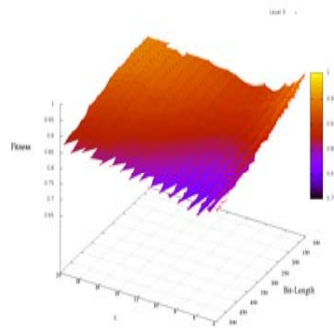


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Results: Multi-Sampling Level 3

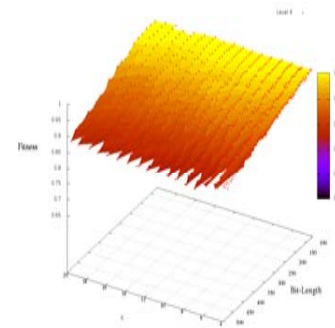


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Results: Multi-Sampling Level 4

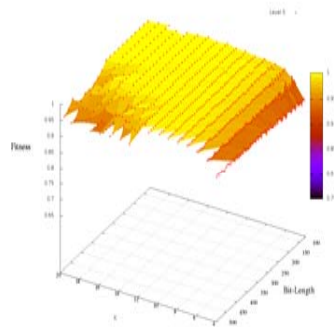


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Results: Multi-Sampling Level 5

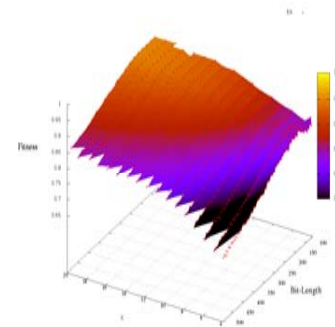


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Results: EA Comparison



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Discussion

- Robustness
 - Fallibility

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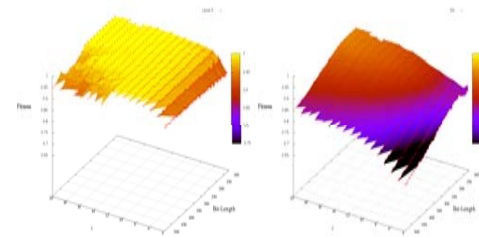
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Robustness: Fallibility

Multi-Sample Level 5

Standard EA



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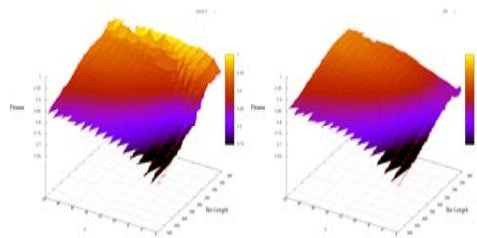
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Robustness: Fallibility

Multi-Sample Level 1

Standard EA



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Discussion

- Robustness
- Fallibility
- Applicability

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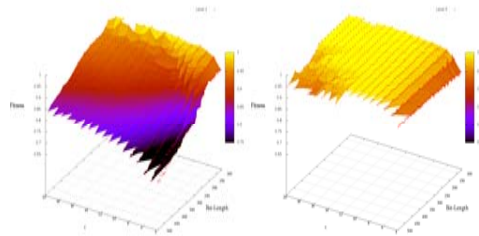
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Robustness: Applicability

Multi-Sample Level 1

Multi-Sample Level 5



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Robustness: Applicability

Level	Run	Train Fit.	Test Fit.	Fallibility
5	1	0.973	0.977	0.050
5	2	0.893	0.879	0.035
5	3	0.850	0.850	0.045
5	4	0.955	0.986	0.029

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Drawbacks

- Increased computational time
 - More runs per evaluation (increased wall time)
 - More problem configurations to optimize for (increased evaluations)

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Summary of Multi-Sample Improvements

- Improved Hyper-Heuristic to evolve more robust BBSAs
- Evolved custom BBSA which outperformed standard EA and were robust to changes in problem configuration

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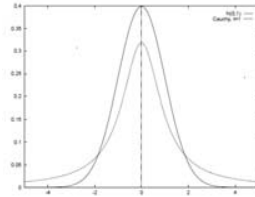
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Case Study 5: The Automated Design of Mutation Operators for Evolutionary Programming [18]

1. **Evolutionary programming** optimizes functions by evolving a population of real-valued vectors (genotype).
2. **Variation** has been provided (manually) by probability distributions (**Gaussian, Cauchy, Levy**).
3. We are **automatically generating** probability distributions (using genetic programming).
4. **Not from scratch**, but from already well known distributions (**Gaussian, Cauchy, Levy**). We are “genetically improving probability distributions”.
5. We are evolving mutation operators for a **problem class** (a probability distributions over functions).
6. **NO CROSSOVER**

Genotype is
(1.3,...,4.5,...,8.7)
Before mutation



Genotype is
(1.2,...,4.4,...,8.6)
After mutation

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(Fast) Evolutionary Programming

Heart of algorithm is mutation
SO LETS AUTOMATICALLY DESIGN

$$x'_i(j) = x_i(j) + \eta_i(j)D_j$$

1. **EP** mutates with a **Gaussian**
2. **FEP** mutates with a **Cauchy**
3. A **generalization** is mutate with a **distribution D** (generated with genetic programming)

1. Generate the initial population of μ individuals, and set $k = 1$. Each individual is taken as a pair of real-valued vectors (x_i, η_i) , $\forall i \in \{1, \dots, \mu\}$.
2. Evaluate the fitness score for each individual (x_i, η_i) , $\forall i \in \{1, \dots, \mu\}$, of the population based on the objective function, $f(x_i)$.
3. Each parent (x_i, η_i) , $i = 1, \dots, \mu$, creates a single offspring (x'_i, η'_i) by: for $j = 1, \dots, n$,

$$x'_i(j) = x_i(j) + \eta_i(j)N(0, 1), \quad (1)$$

$$\eta'_i(j) = \eta_i(j) \exp(\tau^2 N(0, 1) + \tau N(0, 1)) \quad (2)$$
 where $x_i(j)$, $x'_i(j)$, $\eta_i(j)$ and $\eta'_i(j)$ denote the j -th component of the vectors x_i , x'_i , η_i and η'_i , respectively. $N(0, 1)$ denotes a normally distributed one-dimensional random number with mean zero and standard deviation one. $N(0, 1)$ indicates that the random number is generated anew for each value of j . The factors τ and τ' have commonly set to $(\sqrt{2/n})$ and $(\sqrt{2/n})^{-1}$ [9, 8].
4. Calculate the fitness of each offspring (x'_i, η'_i) , $\forall i \in \{1, \dots, \mu\}$.
5. Conduct pairwise comparison over the union of parents (x_i, η_i) and offspring (x'_i, η'_i) , $\forall i \in \{1, \dots, \mu\}$. For each individual, q opponents are chosen randomly from all the parents and offspring with an equal probability. For each comparison, if the individual's fitness is no greater than the opponent's, it receives a "win".
6. Select the μ individuals out of (x_i, η_i) and (x'_i, η'_i) , $\forall i \in \{1, \dots, \mu\}$, that have the most wins to be parents of the next generation.
7. Stop if the stopping criterion is satisfied; otherwise, $k = k + 1$ and go to Step 3.

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Optimization & Benchmark Functions

A set of 23 benchmark functions is typically used in the literature. **Minimization** $\forall x \in S : f(x_{min}) \leq f(x)$
We use them as **problem classes**.

Table 1: The 23 test functions used in our experimental studies, where n is the dimension of the function, f_{min} the minimum value of the function, and $S \subseteq R^n$.

Test function	n	S	f_{min}
$f_1(x) = \sum_{i=1}^n x_i^2$	30	$[-100, 100]^n$	0
$f_2(x) = \sum_{i=1}^n x_i + \prod_{i=1}^n x_i$	30	$[-10, 10]^n$	0
$f_3(x) = \sum_{i=1}^n (\sum_{j=1}^n x_j)^2$	30	$[-100, 100]^n$	0
$f_4(x) = \max_i \{x_i, 1 \leq i \leq n\}$	30	$[-100, 100]^n$	0
$f_5(x) = \sum_{i=1}^n [1000x_{i+1} - x_i^2]^2 + (x_i - 1)^2$	30	$[-30, 30]^n$	0
$f_6(x) = \sum_{i=1}^n [x_i + 0.5]$	30	$[-100, 100]^n$	0
$f_7(x) = \sum_{i=1}^n ix_i^2 + \text{random}[0, 1]$	30	$[-1.28, 1.28]^n$	0
$f_8(x) = \sum_{i=1}^n -x_i \sin(\sqrt{x_i})$	30	$[-500, 500]^n$	42569.5
$f_9(x) = \sum_{i=1}^n [x_i^2 - 10 \cos(2\pi x_i) + 10]$	30	$[-5.12, 5.12]^n$	0
$f_{10}(x) = -20 \exp\left(-0.2 \sqrt{\frac{1}{n} \sum_{i=1}^n x_i^2}\right) - \exp\left(\frac{1}{n} \sum_{i=1}^n \cos 2\pi x_i\right) + 20 + \epsilon$	30	$[-32, 32]^n$	0

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Function Class 1

1. Machine learning needs to generalize.
2. We generalize to function classes.
3. $y = x^2$ (**a function**)
4. $y = ax^2$ (parameterised function)
5. $y = ax^2$, $a \sim [1, 2]$ (**function class**)
6. We do this for all benchmark functions.
7. The mutation operators is evolved to fit the probability distribution of functions.

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Function Classes 2

Function Classes	S	b	f_{min}
$f_1(x) = a \sum_{i=1}^n x_i^2$	$[-100, 100]^n$	N/A	0
$f_2(x) = a \sum_{i=1}^n x_i + b \prod_{i=1}^n x_i $	$[-10, 10]^n$	$b \in [0, 10^{-5}]$	0
$f_3(x) = \sum_{i=1}^n (a \sum_{j=1}^i x_j)^2$	$[-100, 100]^n$	N/A	0
$f_4(x) = \max_i \{a x_i , 1 \leq i \leq n\}$	$[-100, 100]^n$	N/A	0
$f_5(x) = \sum_{i=1}^n [a(x_{i+1} - x_i^2)^2 + (x_i - 1)^2]$	$[-30, 30]^n$	N/A	0
$f_6(x) = \sum_{i=1}^n (ax_i + 0.5)^2$	$[-100, 100]^n$	N/A	0
$f_7(x) = a \sum_{i=1}^n ix_i^4 + \text{random}[0, 1]$	$[-1.28, 1.28]^n$	N/A	0
$f_8(x) = \sum_{i=1}^n -(x_i \sin(\sqrt{ x_i }) + a)$	$[-500, 500]^n$	N/A	$[-12629.5, -12599.5]$
$f_9(x) = \sum_{i=1}^n [ax_i^2 + b(1 - \cos(2\pi x_i))]$	$[-5.12, 5.12]^n$	$b \in [5, 10]$	0
$f_{10}(x) = -a \exp(-0.2 \sqrt{\frac{1}{n} \sum_{i=1}^n x_i^2}) - \exp(\frac{1}{n} \sum_{i=1}^n \cos 2\pi x_i) + a + e$	$[-32, 32]^n$	N/A	0

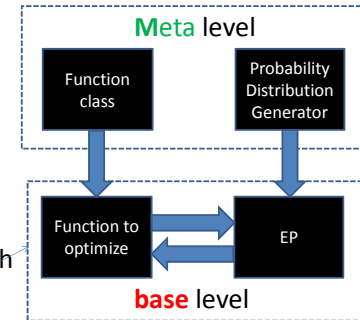
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Meta and Base Learning

- At the **base** level we are learning about a **specific** function.
- At the **meta** level we are learning about the problem **class**.
- We are just doing “generate and test” at a higher level
- What is being passed with each **blue arrow**?
- Conventional EP



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Compare Signatures (Input-Output)

Evolutionary Programming Designer

$(R^n \rightarrow R) \rightarrow R^n$

Input is a function mapping real-valued vectors of length n to a real-value.

Output is a (near optimal) real-valued vector (i.e. the solution to the problem instance)

Evolutionary Programming Designer

$[(R^n \rightarrow R)] \rightarrow ((R^n \rightarrow R) \rightarrow R^n)$

Input is a *list of functions* mapping real-valued vectors of length n to a real-value (i.e. sample problem instances from the problem class).

Output is a (near optimal) (mutation operator for) Evolutionary Programming (i.e. the solution method to the problem class)

We are **raising the level of generality** at which we operate.

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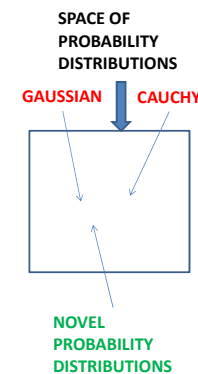
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Genetic Programming to Generate Probability Distributions

- GP Function Set $\{+, -, *, \%\}$
 - GP Terminal Set $\{N(0, \text{random})\}$
- $N(0,1)$ is a normal distribution.

For example a Cauchy distribution is generated by $N(0,1)\%N(0,1)$.

Hence the search space of probability distributions contains the two existing probability distributions used in EP but also **novel probability distributions**.



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A Brief History (Example Applications) [5]

1. **Image Recognition** – Roberts Mark
2. **Travelling Salesman Problem** – Keller Robert
3. **Boolean Satisfiability** – Holger Hoos, Fukunaga, Bader-El-Den
4. **Data Mining** – Gisele L. Pappa, Alex A. Freitas
5. **Decision Tree** - Gisele L. Pappa et al
6. **Crossover Operators** – Oltean et al, Daniel Tauritz et al
7. **Selection Heuristics** – Woodward & Swan, Daniel Tauritz et al
8. **Bin Packing 1,2,3 dimension** (on and off line) Edmund Burke et. al. & Riccardo Poli et al
9. **Bug Location** – Shin Yoo
10. **Job Shop Scheduling** – Mengjie Zhang
11. **Black Box Search Algorithms** – Daniel Tauritz et al

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Comparison of Search Spaces

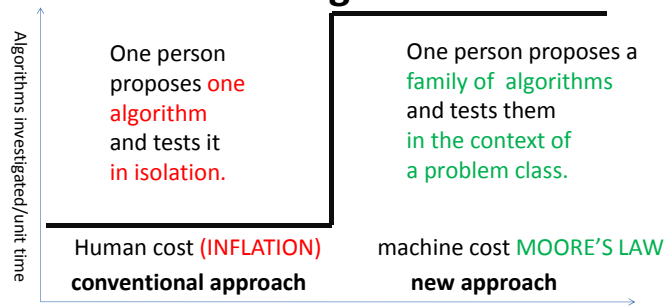
- If **we tackle a problem instance directly**, e.g. Travelling Salesman Problem, we get a **combinatorial explosion**. The search space consists of *solutions*, and therefore explodes as we tackle larger problems.
- If we tackle a generalization of the problem, **we do not get an explosion** as the distribution of functions expressed in the search space tends to a limiting distribution. The search space consists of *algorithms to produces solutions* to a problem instance of any size.
- The algorithm to tackle TSP of size 100-cities, is the same size as The algorithm to tackle TSP of size 10,000-cities

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A Paradigm Shift?



- Previously **one** person proposes **one** algorithm
- Now **one** person proposes **a set of** algorithms
- Analogous to “**industrial revolution**” from hand made to machine made. Automatic Design.

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Conclusions

1. Heuristic are **trained to fit a problem class**, so are designed in context (like evolution). Let's close the feedback loop! **Problem instances live in classes.**
2. We can design algorithms on **small** problem instances and **scale** them apply them to **large** problem instances (TSP, child multiplication).

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Overview of Applications

	SELECTION	MUTATION GA	BIN PACKING	MUTATION EP	CROSSOVER	BBSA
Scalable performance	Not yet tested	Not yet tested	Yes - why	No - why	Not yet tested	Yes
Generation zero human comp.	Rank, fitness proportional	No – needed to seed	Best fit	Gaussian and Cauchy	No	No
Problem classes tested	Shifted function	Parameterized function	Item size	Parameterized function	Rosenbrock, NK-Landscapes, Rastrigin, etc.	DTrap, NK-landscapes
Results Human Competitive	Yes	Yes	Yes	Yes	Yes	Yes
Algorithm iterate over	Population	Bit-string	Bins	Vector	Pair of parents	Population
Search Method	Random Search	Iterative Hill-Climber	Genetic Programming	Genetic Programming	Linear Genetic Programming	Tree-based GP
Type Signatures	$R^2 \rightarrow R$	$B^n \rightarrow B^n$	$R^3 \rightarrow R$	$() \rightarrow R$	$R^n \rightarrow R^m$	Population \rightarrow Population
Reference	[16]	[15]	[6,9,10,11]	[18]	[20]	[21,23,25]
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SUMMARY

1. We can automatically design algorithms that **consistently outperform human designed algorithms (on various domains)**.
2. **Humans should not provide variations**—genetic programming can do that.
3. We are altering the heuristic to suit the set of problem instances presented to it, in the hope that it will generalize to new problem instances (**same distribution - central assumption in machine learning**).
4. The “best” heuristics **depends on the set of problem instances (feedback)**
5. Resulting algorithm is **part man-made part machine-made** (synergy)
6. **not evolving from scratch like Genetic Programming**,
7. improve existing algorithms and adapt them to the new problem instances.
8. Humans are working at a **higher level of abstraction** and more creative. Creating search spaces for GP to sample.
9. **Algorithms are reusable**, “**solutions**” **aren’t**. (e.g. tsp algorithm vs route)
10. **Opens up new problem domains**. E.g. bin-packing.

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Related hyper-heuristics events

- Evolutionary Computation for the Automated Design of Algorithms (ECADA) workshop @GECCO 2015
- Combinatorial Black Box Optimization Competition (CBOC) @GECCO 2015

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End of File ☺

- Thank you for listening !!!
- We are glad to take any
 - comments (+,-)
 - suggestions/criticisms
 Please email us any missing references!
 John Woodward (<http://www.cs.stir.ac.uk/~jrw/>)
 Daniel Tauritz (<http://web.mst.edu/~tauritzd/>)

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