#### **Introducing Rule-Based Machine Learning:** A Practical Guide

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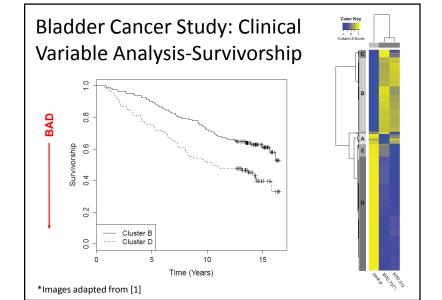
#### Instructors

Ryan Urbanowicz is a post-doctoral research associate at the University of Pennsylvania in the Pearlman School of Medicine. He completed a Bachelors and Masters degree in Biological Engineering at Cornell University (2004 & 2005) and a Ph.D in Genetics at Dartmouth College (2012). His research focuses on the methodological development and application of learning classifier systems to complex, heterogeneous problems in bioinformatics, genetics, and epidemiology.



Will Browne is an Associate Professor at the Victoria University of Wellington. He completed a Bachelors of Mechanical Engineering at the University of Bath, a Masters and EngD from Cardiff, post-doc. Leicester and lecturer in Cybernetics at Reading, UK. His research focuses on applied cognitive systems. Specifically how to use inspiration from natural intelligence to enable computers/ machines/ robots to behave usefully. This includes cognitive robotics, learning classifier systems, and modern heuristics for industrial application.





# Course Agenda

- Introduction (What and Why?)
  - LCS Applications
  - Distinguishing Features of an LCS
  - Historical Perspective
- Driving Mechanisms
  - Discovery
- Learning
- LCS Algorithm Walk-Through (How?)
  - Rule Population
  - Set Formation
  - Covering
  - Prediction/Action Selection
  - Parameter Updates/Credit Assignment
  - Subsumption
  - Genetic Algorithm
  - Deletion
- Michigan vs. Pittsburgh-style
- Advanced Topics
- Resources



#### **Introduction:** What is Rule-Based Machine Learning?

- Rule Based Machine Learning (RBML)
- What types of algorithms fall under this label?
  - Learning Classifier Systems (LCS)\*
    - Michigan-style LCS
    - Pittsburgh-style LCS
  - Association Rule Mining
  - Related Algorithms
    - Artificial Immune Systems
- Rule-Based The solution/model/output is collectively comprised of individual rules typically of the form (IF: THEN).
- Machine Learning "A subfield of computer science that evolved from the study of pattern recognition and computational learning theory in artificial intelligence. Explores the construction and study of algorithms that can learn from and make predictions on data." – Wikipedia
- Keep in mind that machine learning algorithms exist across a continuum.
  - Hybrid Systems
  - Conceptual overlaps in addressing different types of problem domains.

\* LCS algorithms are the focus of this tutorial.

#### **Introduction:** Why LCS Algorithms? {1 of 3}

- Adaptive Accommodate a changing environment. Relevant parts of solution can evolve/update to accommodate changes in problem space.
- ❖ Model Free Limited assumptions about the environment\*
  - Can accommodate complex, epistatic, heterogeneous, or distributed underlying patterns.
  - No assumptions about the number of predictive vs. non-predictive attributes (feature selection).
- Ensemble Learner (unofficial) No single model is applied to a given instance to yield a
  prediction. Instead a set of relevant rules contribute a 'vote'.
- Stochastic Learner Non-deterministic learning is advantageous in large-scale or high complexity problems, where deterministic learning becomes intractable.
- ❖ Multi-objective (Implicitly) Rules evolved towards accuracy and generality/simplicity.
- Interpretable (Data Mining/Knowledge Discovery) Depending on rule representation, individual rules are logical and human readable IF:THEN statements. Strategies have been proposed for global knowledge discovery over the rule population solution [ X X ].
- \* The term `environment' refers to the source of training instances for a problem/task.

#### **Introduction:** Comparison of RBML Algorithms

#### Learning Classifier Systems (LCS)

- Developed primarily for modeling, sequential decision making, classification, and prediction in complex adaptive system.
- ❖ IF:THEN rules link independent variable states to dependent variable states. e.g. {V<sub>1</sub>, V<sub>2</sub>, V<sub>3</sub>} → Class/Action

#### Association Rule Mining (ARM)

- Developed primarily for discovering interesting relations between variables in large datasets.
- F:THEN rules link independent variable(s) to some other independent variable e.g. {V₁, V₂, V₃} → V₄

#### Artificial Immune Systems (AIS)

- Developed primarily for anomaly detection (i.e. differentiating between self vs. not-self)
- Multiple `Antibodies' (i.e. detectors) are learned which collectively characterize 'self' or "not-self' based on an affinity threshold.

#### What's in common?

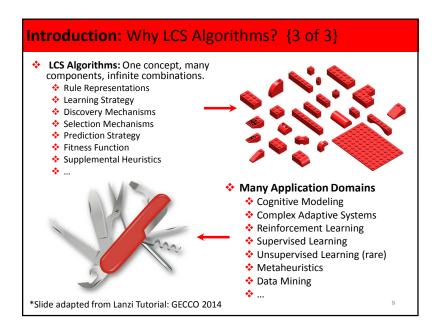
- In each case, the solution or output is determined piece-wise by a set of `rules' that each cover part of the problem at hand. No single, `model' expression is output that seeks to describe the underlying pattern(s).
- This tutorial will focus on LCS algorithms, and approach them initially from a supervised learning perspective (for simplicity).

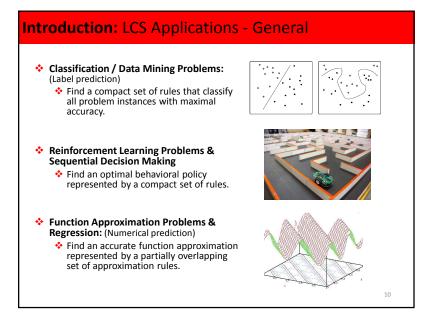
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#### **Introduction:** Why LCS Algorithms? {2 of 3}

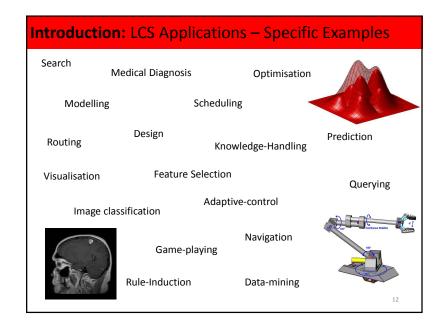
#### Other Advantages

- Applicable to single-step or multi-step problems.
- Representation Flexibility: Can accommodate discrete or continuous-valued endpoints\* and attributes (i.e. Dependent or Independent Variables)
- Can learn in clean or very noisy problem environments.
- Accommodates missing data (i.e. missing attribute values within training instances).
- Classifies binary or multi-class discrete endpoints (classification).
- Can accommodate balanced or imbalanced datasets (classification).
  - \* We use the term `endpoints' to generally refer to dependent variables .

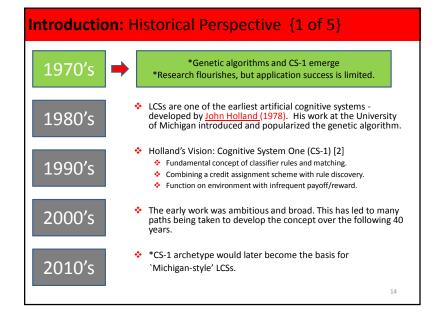


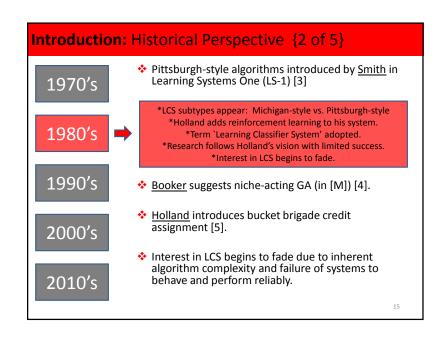


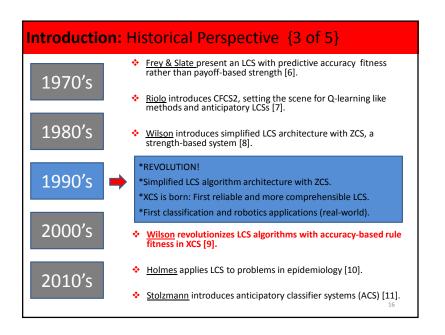
# **Introduction:** LCS Applications – Uniquely Suited Uniquely Suited To Problems with... Dynamic environments Perpetually novel events accompanied by large amounts of noisy or irrelevant data. Continual, often real-time, requirements for actions. Implicitly or inexactly defined goals. Sparce payoff or reinforcement obtainable only through long action sequences [Booker 89]. And those that have... High Dimensionality Noise Multiple Classes Epistasis Heterogeneity Hierarchical dependencies Unknown underlying complexity or dynamics



#### **Introduction:** Distinguishing Features of an LCS Learning Classifier Systems typically combine: Global search of evolutionary computing (e.g. Genetic Algorithm) Local optimization of machine learning (supervised or reinforcement) THINK: Trial and error meets neo-Darwinian evolution. Solution/output is given by a set of IF:THEN rules. Learned patterns are distributed over this set. · Output is a distributed and generalized probabilistic prediction F:THEN rules can specify any subset of the attributes available in the environment IF:THEN rules are only applicable to a subset of possible instances. F:THEN rules have their own parameters (e.g. accuracy, fitness) that reflect performance on the instances they match. Rules with parameters are termed 'classifiers. Incremental Learning (Michigan-style LCS) Rules are evaluated and evolved one instance from the environment Online or Offline Learning (Based on nature of environment) 13

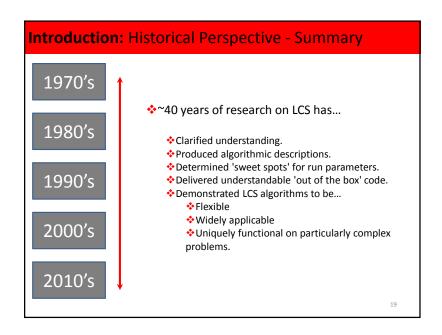


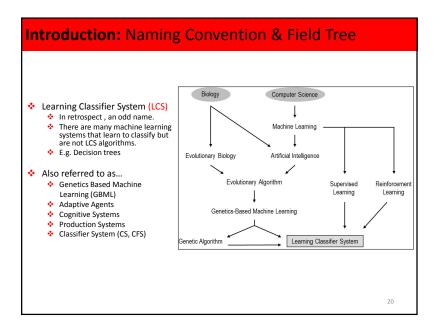




#### **Introduction:** Historical Perspective {4 of 5} Wilson introduces XCSF for function approximation [12]. Kovacs explores a number of practical and theoretical LCS 1970's questions [13,14]. Bernado-Mansilla introduce UCS for supervised learning [15]. Bull explores LCS theory in simple systems [16]. Bacardit introduces two Pittsburgh-style LCS systems GAssist and 1980's BioHEL with emphasis on data mining and improved scalability to larger datasets[17,18]. ❖ Holmes introduces EpiXCS for epidemiological learning. Paired with the first LCS graphical user interface to promote accessibility and ease of use [19]. 1990's Butz introduces first online learning visualization for function approximation [20]. Lanzi & Loiacono explore computed actions [21]. LCS algorithm specializing in supervised learning and data 2000's mining start appearing. \*LCS scalability becomes a central research theme. \*Increasing interest in epidemiological and bioinformatics. 2010's \*Facet-wise theory and applications

#### **Introduction:** Historical Perspective {5 of 5} Franco & Bacardit explored GPU parallelization of LCS for scalability [22]. Urbanowicz & Moore introduced statistical and visualization strategies for 1970's knowledge discovery in an LCS [23]. Also explored use of 'expert knowledge' to efficiently guide GA [24], introduced attribute tracking for explicitly characterizing heterogeneous patterns [25]. Browne and Iqbal explore new concepts in reusing building blocks (i.e., code 1980's fragments). Solved the 135-bit multiplexer reusing building blocks from simpler multiplexer problems [26]. ❖ <u>Bacardit</u> successfully applied BioHEL to large-scale bioinformatics problems also exploring visualization strategies for knowledge discovery [27]. 1990's Urbanowicz introduced ExSTraCS for supervised learning [28]. Applied ExSTraCS to solve the 135-bit multiplexer directly . \*Increased interest in supervised learning applications persists. 2000's \*Emphasis on solution interpretability and knowledge discovery. \*Scalability improving – 135-bit multiplexer solved! \*GPU interest for computational parallelization. \*Broadening research interest from American & European to 2010's nclude Australasian & Asian.





#### **Driving Mechanisms**

Two mechanisms are primarily responsible for driving LCS algorithms.

#### Discovery

- \* Refers to "rule discovery".
- Traditionally performed by a genetic algorithm (GA).
- Can use any directed method to find new rules.

#### Learning

- The improvement of performance in some environment through the acquisition of knowledge resulting from experience in that environment.
- $\ ^{\diamondsuit}$  Learning is constructing or modifying representations of what is being experienced.
- \* AKA: Credit Assignment
- \* LCSs traditionally utilized reinforcement learning (RL).
- Many different RL schemes have been applied as well as much simpler supervised learning schemes.

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#### **Driving Mechanisms:** LCS Rule Discovery {1 of 2}

Create hypothesised better rules from existing rules & genetic material.

#### Genetic algorithm

- · Original and most common method
- · Well studied
- Stochastic process
- · The GA used in LCS is most similar to niching GAs

#### Estimation of distribution algorithms

- Sample the probability distribution, rather than mutation or crossover to create new rules
- · Exploits genetic material
- \* Bayesian optimisation algorithm
  - · Use Bayesian networks
  - · Model-based learning

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#### **Driving Mechanisms:** LCS Rule Discovery {2 of 2}

#### When to learn

- Too frequent: unsettled [P]
- Too infrequent: inefficient training

#### What to learn

- Most frequent niches or...
- Underrepresented niches

#### How much to learn

- How many good rules to keep (elitism)
- Size of niche

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# **Driving Mechanisms:** Genetic Algorithm (GA)

- Inspired by the neo-Darwinist theory of natural selection, the evolution of rules is modeled after the evolution of organisms using four biological analogies.
  - ❖ Genome → Coded Rule (Condition)

n) Example Rules (Ternary Representation)

- ❖ Phenotype → Class (Action)
- ❖ Survival of the Fittest → Rule Competition
- ❖ Genetic Operators → Rule Discovery
- Condition ~ Action
- #101# ~ 1
- #10## ~ 0
- 00#1# ~ 0 1#011 ~ 1

- Elitism (Essential to LCS)
  - LCS preserves the majority of top rules each learning iteration.
  - Rules are only deleted to maintain a maximum rule population size (N).

#### **Driving Mechanisms:** GA – Crossover Operator

- Select parent rules  $r_1 = \frac{00010001}{r_2 = 01110001}$
- Set crossover point  $r_1 = 00010001$  $r_2 = 01110001$
- Apply Single Point Crossover
  - $r_1 = 00010001$   $r_2 = 01110001$
  - $c_1 = 00110001$  $c_2 = 01010001$
- Many variations of crossover possible:
  - Two point crossover
  - Multipoint crossover
  - Uniform crossover

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# **Driving Mechanisms**: GA – Mutation Operator

- Select parent rule  $r_1 = 01110001$
- ❖ Randomly select bit to mutate r₁ = 01110001
- Apply mutation  $r_1 = 01100001$

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#### **Driving Mechanisms**

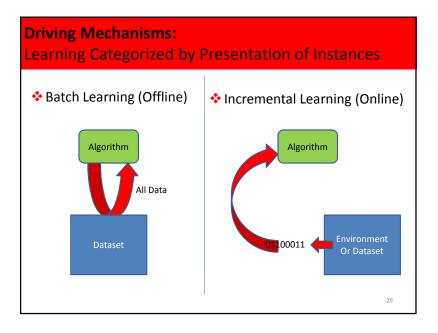
Two mechanisms are primarily responsible for driving LCS algorithms.

- Discovery
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  - \* AKA: Credit Assignment
  - LCSs traditionally utilized reinforcement learning (RL).
  - Many different RL schemes have been applied as well as much simpler supervised learning (SL) schemes.

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#### **Driving Mechanisms:** Learning

- With the advent of computers, humans have been interested in seeing how artificial 'agents' could learn. Either learning to...
  - Solve problems of value that humans find difficult to solve
  - For the curiosity of how learning can be achieved.
- Learning strategies can be divided up in a couple ways.
- Categorized by presentation of instances
  - Batch Learning (Offline)
  - Incremental Learning (Online or Offline)
- Categorized by feedback
  - Reinforcement Learning
  - Supervised Learning
  - Unsupervised Learning



# **Driving Mechanisms: Learning Categorized by Feedback**

Supervised learning: The environment contains a teacher that directly provides the correct response for environmental states.

#### Unsupervised learning:

The learning system has an internally defined teacher with a prescribed goal that does not need utility feedback of any kind.

Reinforcement learning: The environment does not directly indicate what the correct response should have been. Instead, it only provides reward or punishment to indicate the utility of actions that were actually taken by the system.

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#### **Driving Mechanisms:** LCS Learning

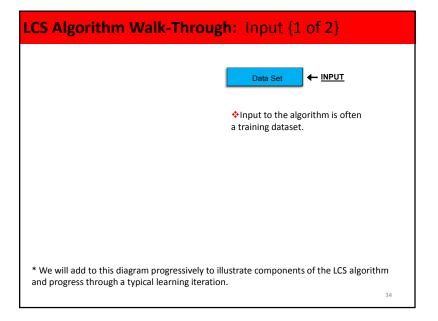
- LCS learning primarily involves the update of various rule parameters such as...
  - Reward prediction (RL only)
  - Error
  - Fitness
- Many different learning strategies have been applied within LCS algorithms.
  - Bucket Brigade [5]
  - Implicit Bucket Brigade
  - One-Step Payoff-Penalty
  - Symmetrical Payoff Penalty
  - Multi-Objective Learning
  - Latent Learning
  - Widrow-Hoff [8]
  - Supervised Learning Accuracy Update [15]
  - Q-Learning-Like [9]
- Fitness Sharing
  - Give rule fitness some context within niches.

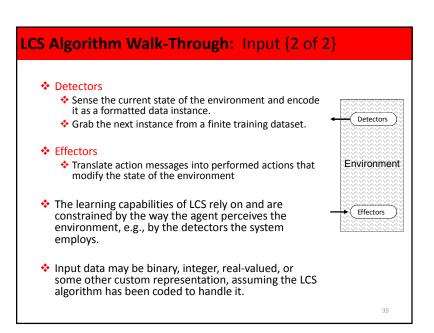
# **Driving Mechanisms:** Assumptions for Learning

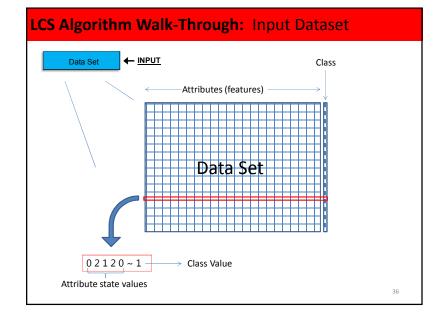
- In order for artificial learning to occur data containing the patterns to learn is needed.
- This can be through recorded past experiences or interactive with current events.
- ❖ If there are no clear patterns in the data, then LCSs will not learn.

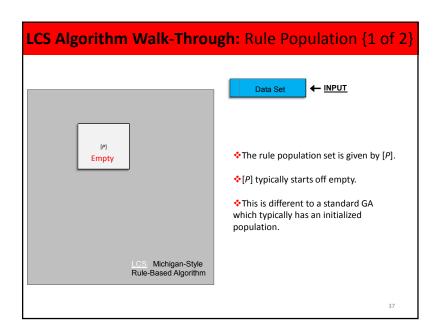
## **LCS Algorithm Walk-Through**

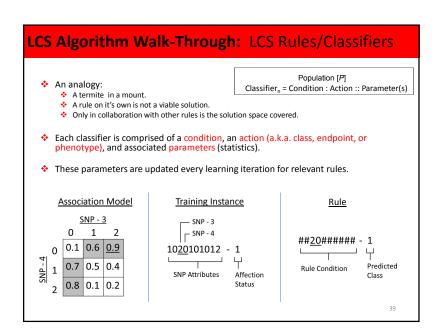
- Demonstrate how a fairly typical modern Michigan-style LCS algorithm...
  - is structured.
  - \* is trained on a problem environment,
  - \* makes predictions within that environment
- We use as an example, an LCS architecture most similar to UCS [15], a supervised learning LCS.
- We assume that it is learning to perform a classification/prediction task on a training dataset with discrete-valued attributes, and a binary endpoint.
- We provide discussion and examples beyond the UCS architecture throughout this walk-through to illustrate the diversity of system architectures available.











#### LCS Algorithm Walk-Through: Rule Population {2 of 2} ❖ A finite set of rules [P] which collectively explore the 'search space'. Every valid rule can be thought of as part of a candidate solution (may or may not be good) The space of all candidate solutions is termed the 'search' space'. [P] The size of the search space is determined by both the encoding of the LCS itself and the problem itself. The maximum population size (N) is one of the most critical run parameters. User specified N = 200 to 20000 rules but success depends on dataset dimensions and problem complexity. ❖ Too small → Solution may not be found ❖ Too large → Run time or memory limits too extreme.

LCS Algorithm Walk-Through: Rule Rep	resentation -
Ternary	
<ul> <li>LCSs can use many different representation schemes.</li> <li>Also referred to as `encodings'</li> </ul>	(Ternary Representation)  Condition ~ Class
Suited to binary input or	#101# ~ 1
Suited to real-valued inputs and so forth	#10## ~ 0
<ul> <li>Ternary Encoding – traditionally most commonly used</li> </ul>	00#1# ~ 0
The ternary alphabet matches binary input	1#011 ~ 1
<ul> <li>A attribute in the condition that we don't care about is given the symbol '#' (wild card)</li> </ul>	
<ul><li>For example,</li></ul>	
101~1 - the Boolean states 'on off on' has action 'on'	
<ul> <li>001~1 - the Boolean states 'off off on' has action 'on'</li> </ul>	
<ul> <li>Can be encoded as</li> </ul>	
#01~1 - the Boolean states ' either off on' has action '	on'
In many binary instances, # acts as an OR function on {0,1}	
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#### LCS Algorithm Walk-Through: Rule Representation -Other {1 of 4} (Quaternary Encoding) Quaternary Encoding [29] ❖ 3 possible attribute states {0,1,2} plus '#'. ##20##### - 1 For a specific application in genetics. Predicted **Rule Condition** Real-valued interval (XCSR [30]) Interval is encoded with two variables: center and spread ❖ i.e. [center,spread] → [center-spread, center+spread] i.e. [0.125,0.023] → [0.097, 0.222] Real-valued interval (UBR [31]) Interval is encoded with two variables: lower and upper bound i.e. [lower, upper]

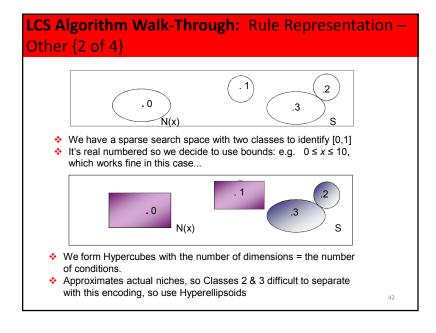
Messy Encoding (Gassist, BIOHel, ExSTraCS [17,18,28])

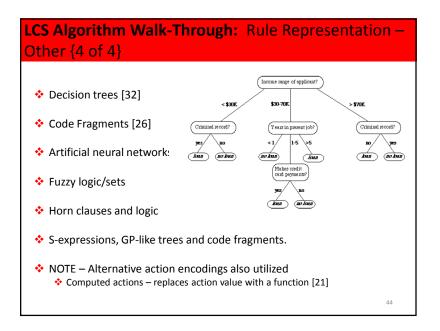
Improves transparency, reduces memory and speeds processing

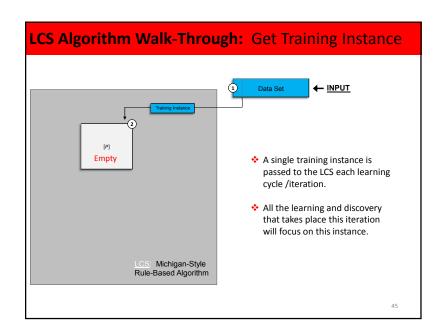
Attribute-List Knowledge Representation (ALKR) [33]
 11##0:1 shorten to 110:1 with reference encoding

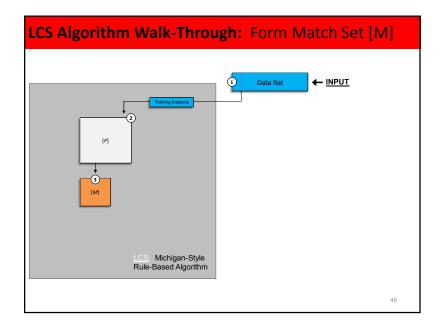
i.e. [0.097, 0.222]

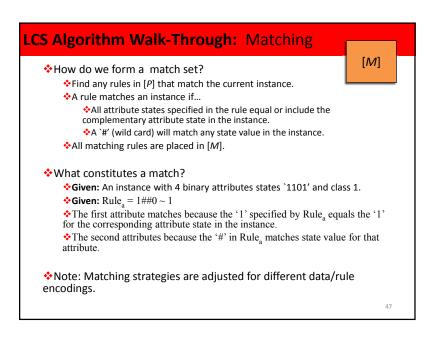
#### LCS Algorithm Walk-Through: Rule Representation -Other {3 of 4} Mixed Discrete-Continuous ALKR [28] Attribute 5 7 34 35 49 71 Useful for big and data with multiple Rule attribute types Discrete (Binary, Integer, String) Classification Continuous (Real-Valued) Continuous Discrete Similar to ALKR (Attribute List Knowledge Representation): [Bacardit et al. 09] Ternary Mixed ##20##### - 1 Intervals used for continuous Predicted Rule Condition attributes and direct encoding used Condition for discrete. Classification 1 43

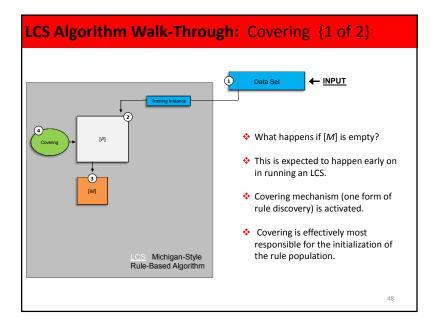










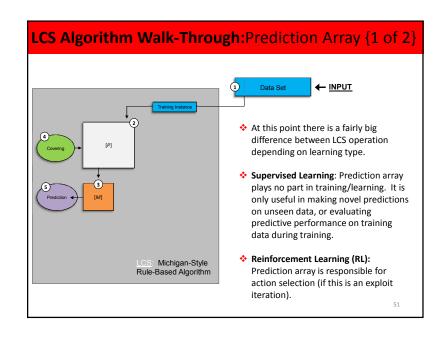


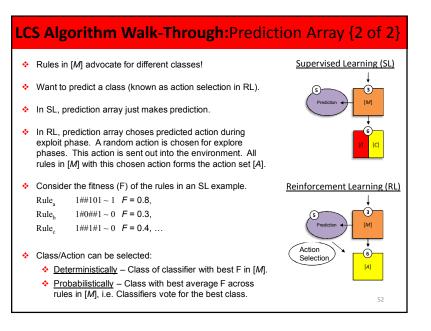
#### LCS Algorithm Walk-Through: Covering {2 of 2} \* Covering initializes a rule by generalizing an instance. **Condition**: Generalization of instance attribute states. Covering Class: If supervised learning: Assigned correct class ❖ If reinforcement learning: Assigned random class/action (Instance) Covering adds #'s to a new rule with probability of 02120~1 generalization (P<sub>#</sub>) of 0.33 - 0.5 (common settings). New rule is assigned initial rule parameter values. 0 # 1 2 # ~ 1(New Rule) NOTE: Covering will only add rules to the population that match at least one data instance.

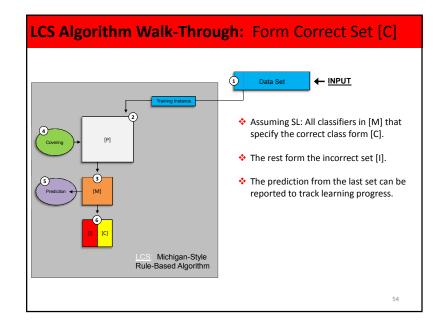
\* This avoids searching irrelevant parts of the search space.

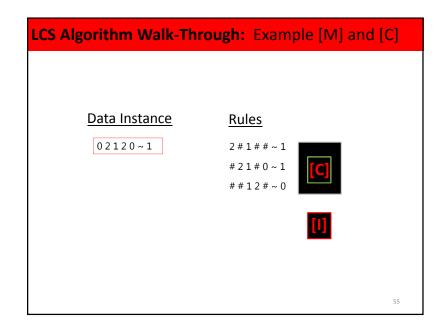
#### LCS Algorithm Walk-Through: Special Cases for Matching and Covering Matching: \* Continuous-valued attributes: Specified attribute interval in rule must include instance value for attribute. E.g. [0.2, 0.5] includes 0.34. Alternate strategy-❖ Partial match of rule is acceptable (e.g. 3/4 states). Might be useful in high dimensional problem spaces. • For supervised learning – also activated if no rules are found for [C] Alternate activation strategies-Having an insufficient number of matching classifiers for: Given class (Good for best action mapping) ❖ All possible classes (Good for complete action mapping and reinforcement learning) Alternate rule generation-\* Rule specificity limit covering [28]: Removes need for P<sub>#</sub>, useful/critical for problems with many attributes or high dimensionality. \* Picks some number of attributes from the instance to specify up to a datasetdependent maximum.

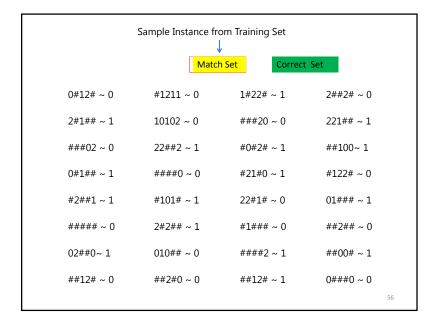
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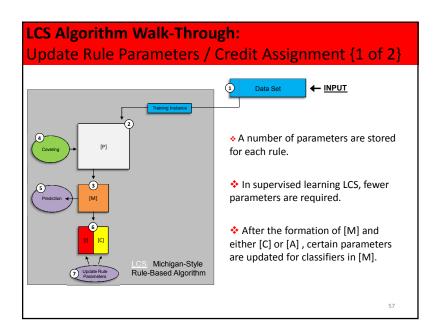


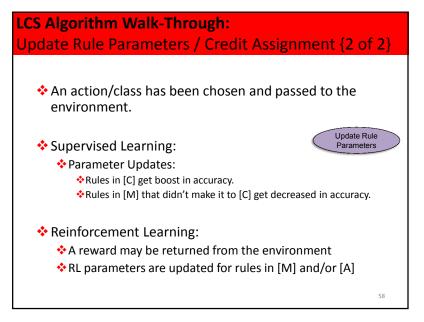


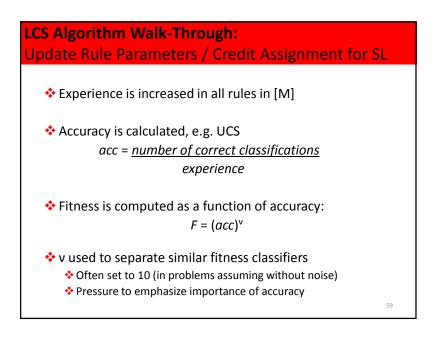


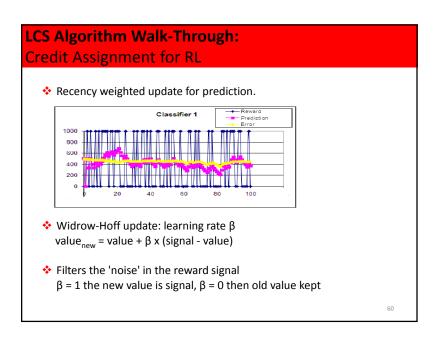












# LCS Algorithm Walk-Through:

# Credit Assignment for RL + Fitness Sharing

- Classifier considered accurate if:
  - Error < tolerance, otherwise scaled.
- Accuracy relative to action set
- Fitness based on relative accuracy, e.g. XCS

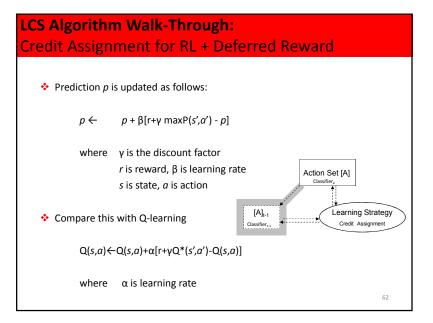
$$p \leftarrow p + \beta(R - p),$$
  
 $\varepsilon \leftarrow \varepsilon + \beta(|R - p| - \varepsilon),$ 

$$\kappa = \begin{cases} 1 & \text{if } \varepsilon < \varepsilon_0 \\ \alpha (\varepsilon / \varepsilon_0)^{-\nu} & \text{otherwise} \end{cases}$$

 $K' = \frac{K}{\sum_{x \in [A]} K_x},$ 

$$F \leftarrow F + \beta(\kappa' - F)$$

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# LCS Algorithm Walk-Through:

#### Why not Strength-based Fitness?

- Different niches of the environment usually have different payoff levels -Phenotypic niche
- In fitness sharing classifier's strength no longer correctly predicts payoff Fitness sharing prevents takeover
- Fitness sharing does not prevent more renumerative niches gaining more classifiers -Niche rule discovery helps
- Rule discovery cannot distinguish an accurate classifier with moderate payoff from an overly general classifier having the same payoff on average – Over-generals proliferate
- No reason for accurate generalizations to evolve
- Unnecessarily specific rules survive

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# **LCS Algorithm Walk-Through:** Subsumption {1 of 2} Data Set **←** <u>INPUT</u> Subsumption adds an explicit rule generalization pressure to LCS. This mechanism has been applied at two points in an LCS learning iteration. Among rules in [C] right after its formation. (Rarely used anymore) Following GA rule discovery offspring rules checked for Michigan-Style subsumption against parent Rule-Based Algorithm classifiers and classifiers in [C]. 64

## LCS Algorithm Walk-Through: Subsumption {2 of 2}

In sparse or noisy environments over-specific rules can take over population.

> Want  $\rightarrow$  10011###1~1 But got  $\rightarrow$  10011#011~1, 100111111~1, ...

- Starvation of generals, so delete specific 'sub-copies'
- Need accurate rules first:
  - How to set level of accuracy (often not 100%)
  - \* If rule A is completely accurate  $(\epsilon < \epsilon_0)$  Then can delete rule B from the population without loss of performance
- Subsumption mechanisms:
  - GA subsumption
  - Action set [A] subsumption



- Subsumption = General rule (A) absorbs a more specific one (B)
  - Increases rule numerosity

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# LCS Algorithm Walk-Through: Numerosity {1 of 2}

- Numerosity is a useful concept (trick):
- Reduces memory usage
  - Instead of population carrying multiple copies of the same classifier it just carries one copy.
  - Each rule has a numerosity value (initialised as 1)
- Protects rule from deletion
  - Stabilises rule population
- Numerosity is increased by 1
  - When subsumes another rule
  - When RD makes a copy
- Numerosity is decreased by 1
  - Rule is selected for deletion

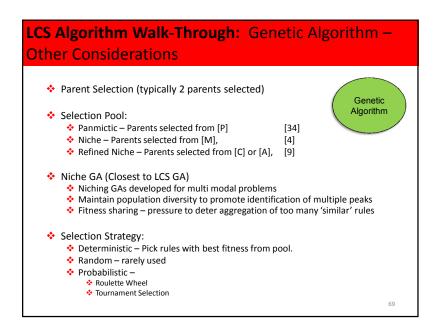
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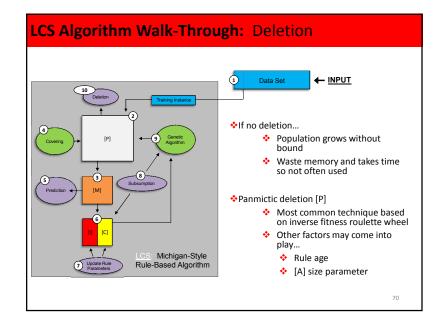
#### LCS Algorithm Walk-Through: Numerosity {2 of 2}

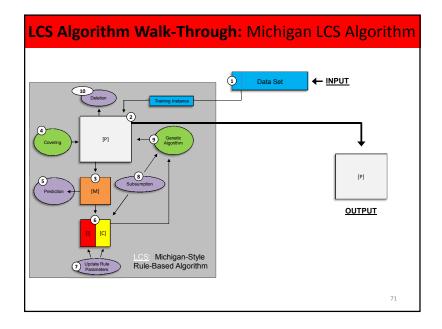
- Numerosity (n) affects action selection and update procedures:
- The fitness sums take numerosity into account:
- Terminology:
  - Macroclassifiers: all unique classifiers n ≥ 1
  - Microclassifiers: all individual classifiers (n copies of macroclassifiers)
- Ratio of macroclassifiers to microclassifiers often used as a measure of training progress.
- Numerosity is also often applied as a `best-available' strategy to ranking rules for manual rule inspection (i.e. knowledge discovery).

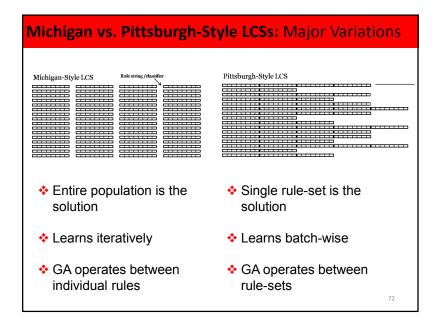
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# LCS Algorithm Walk-Through: Genetic Algorithm • GA rule discovery is activated if average experience of classifiers in selection pool is above a user defined cut-off. • Classifier experience is the number of instances that the classifier has matched.









# Michigan vs. Pittsburgh-Style LCSs: Implementations

- Michigan Style LCS
  - ZCS (Strength Based)
  - ❖XCS (Accuracy Based Most popular)
  - ❖UCS (Supervised Learning)
  - ❖ ACS (Anticipatory)
  - ExSTraCS (Extended Supervised Tracking and Learning)
- Pittsburgh Style LCS
  - ❖ GALE (Spatial Rule Population)
  - GAssist (Data mining Pitt Style Archetype)
  - ❖ BIOHEL (Focused on Biological Problems and Scalability)
- ❖ Other Hybrid Styles also exist!

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# **LCS Disadvantages**

- Not widely known.
- \* Relatively limited software accessibility.
- Rule population interpretation and knowledge extraction can be challenging.
- Can suffer from overfitting, despite explicit and implicit pressures to generalize rules.
- \* Relatively little theoretical work or convergence proofs.
- Many run parameters to consider/optimize.

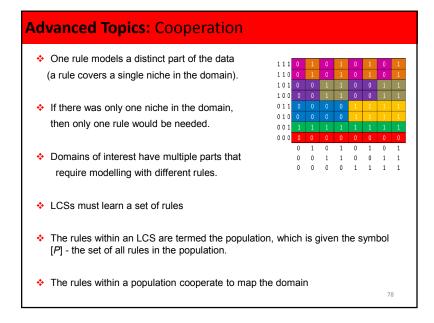
/4

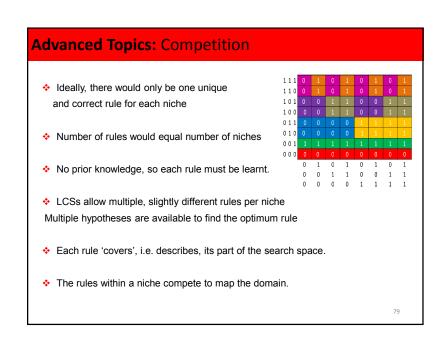
# **Advanced Topics:** Learning Parameters {1 of 2}

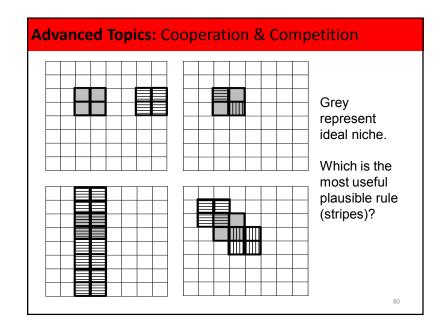
Symbol	Meaning
N	Maximum size of the population (In micro-classifiers, N is the number sum of the classifier numerosities)
β	Learning rate for p, $\epsilon$ , f, and as
α, ε <sub>0</sub> , ν	Used in calculating the fitness of a classifier
γ	Discount factor used (in multi-step problems) in updating classifier predictions
$\theta_{GA}$	GA threshold  The GA is applied when the average time since the last GA in the lest is greater than the threshold.
χ	Probability of applying crossover in GA
μ	Probability of mutating an allele in the offspring
$\theta_{\text{del}}$	Deletion threshold If the experience of a classifier is greater than $\theta_{\text{del}}$ its fitness may be considered in its probability of deletion
δ	Mean fitness in [P] below which the fitness of a classifier may be considered in its probability of deletion
$\theta_{\text{sub}}$	Subsumption threshold – the experience of a classifier must be greater than $\theta_\text{sub}$ in order to be able to subsume another classifier
	7

**Advanced Topics:** Learning Parameters {2 of 2}

Symbol	Meaning
P#	Probability of using a # in one attribute in C when covering
$p_I\epsilon_IF_I$	Initial Values in new classifiers
p <sub>explr</sub>	Probability during action selection of choosing the action uniform randomly
$\theta_{mna}$	Minimal number of actions that must be present in a match set [M] or else covering will occur
doGASumput subsumption	ion is a Boolean parameter that specifies if offspring are to be tested for possible logical by parents.
doActionSetS classifiers.	subsumption is a boolean parameter that specifies if action sets are to be tested for subsuming







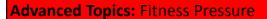
## **Advanced Topics:** Over-generals

- Over-generals are undesired, inaccurate rules that typically match many instances.
- When additional reward offsets any additional penalty
- Strength-based fitness is more prone to overgenerals
- Accuracy-based fitness is less prediction orientated

Want 10011###1:1 get 10011###:1, where 10011###0:0

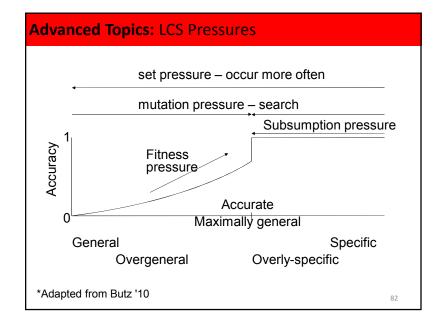
\* Can occur in unbalanced datasets or where the error tolerance  $\epsilon_0$  is set too high.

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- Fitness pressure is fundamental to evolutionary computation: "survival of the fittest"
- Fitter rules assumed to include better genetic material,
- Fitter rules are proportionately more likely to be selected for mating,
- Genetic material hypothesised to improve each generation.
- Fitness measures based on error or accuracy drive the population to rules that don't make mistakes
- Favours specific rules (cover less domain)
- Fitness measures based on reward trade mistakes for more reward
- Favours general rules (cover more domain)

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#### **Advanced Topics:** Set Pressure

- Set pressure is related to the opportunity to breed,
- Does not occur in panmictic rule selection
- Need Niching through [M] or [A] rule discovery
- Class imbalance affects set pressure
- Set pressure is more effective when replacing 'weaker' rules
- Often panmictic deletion, thus one action can replace a different action
- To prevent an action type disappearing, relative fitness is used (rare rules have high relative fitness and so breed)
- Rules that occur in more sets have more opportunity to be selected from mating
- · Favours general rules

#### **Advanced Topics:** Mutation Pressure

- ❖ Genotypically change the specificity-generality balance
- Mutation can

Randomise:

Generalise:

Specialise:

 $0 \leftarrow 1 \text{ or } #$  $1 \leftarrow 0 \text{ or } #$ 

0 · #

 $\begin{array}{ccc} 0 & \leftarrow & 0 \\ 1 & \leftarrow & 1 \end{array}$ 

 $\# \leftarrow 0 \text{ or } 1$ 

# ←

# ← 0 or 1

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# **Advanced Topics:** Complete vs. Best Action Mapping

- ❖ Should LCS discover:
  - The most optimum action in a niche
  - The predicted payoff for all actions in a niche
     X x A => P (cf Q-Learning)
- \* The danger with optimum action only:
  - If a suboptimal rule is converged upon ... difficult to discover and switch policy (CF path habits)
- The problem with predicting all actions:
  - · Memory and time intensive
  - Identifies and keeps consistently incorrect action (100% accurate prediction) rules
  - · Harder to interpret rule base

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#### **Advanced Topics:** LCS Scalability

- What is scalability?
  - Maintaining algorithm tractability as problem scale increases.
  - ❖ Problem scale increases can include...
    - Higher pattern dimensionality
    - Larger-scale datasets with
      - ❖Increased number of potentially predictive attributes.
      - Increased number of training instances.
- Strategies for improving LCS scalability.
  - ♦ More efficient rule representations [18,28] (Pittsburgh and Michigan)
  - Windowing [36] (Pittsburgh)
  - Computational Parallelization (GPGPUs) [22]
  - ❖ Ensemble learning with available attributes partitioned into subsets [27]
  - Expert knowledge guided GA [25]
  - ❖Rule Specificity Limit [28]

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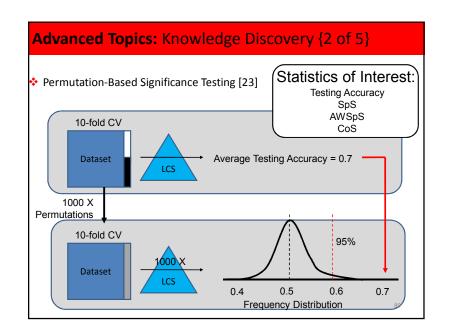
# **Advanced Topics:** Knowledge Discovery {1 of 5}

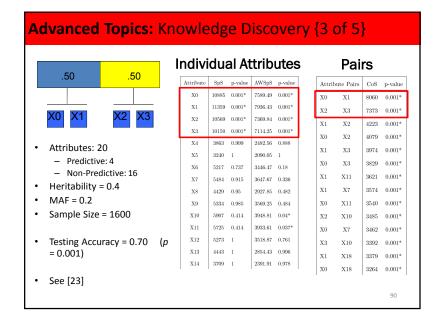
Description of global summary statistics for [P] (SpS, AWSpS) [23]

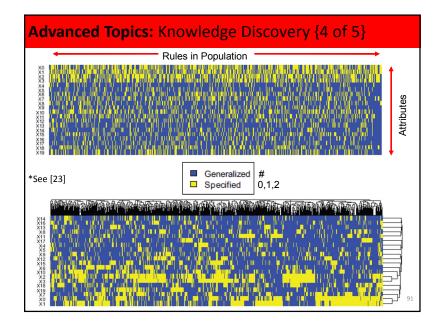
Attribute	X1	X2	X3	X4	Class	Numerosi	ty Accuracy
R1	X	#	#	X	0	5	0.73
R2	#	X	#	X	1	1	0.51
R3	X	X	#	X	0	2	0.88
R4	#	X	X	#	1	1	0.62
SpS	7	4	1	8			
AWSpS	5.41	2.89	0.62	5.92			

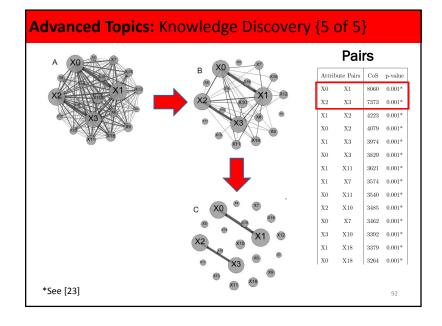
SpS (X1) = 
$$5 + 2 = 7$$

AWSpS (X1) = (0.73) \* 5 + (0.88) \* 2 = 5.41

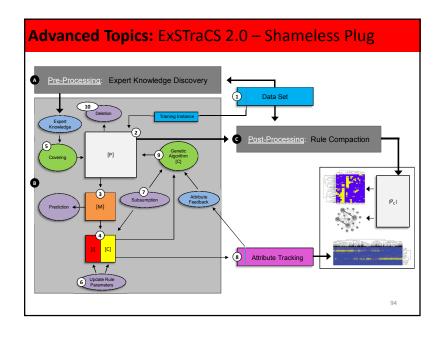


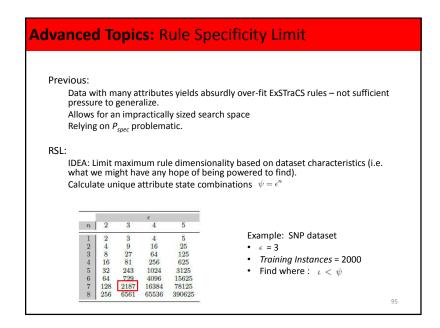


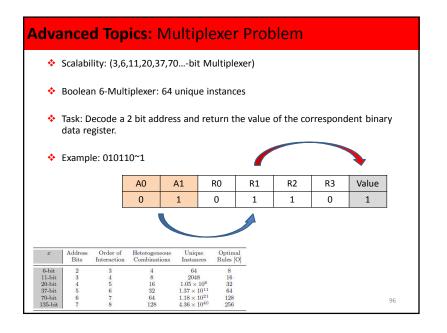




# An extension to the LCS algorithm that allows for the explicit characterization of heterogeneity, and allows for the identification of heterogeneous subject groups. Akin to long-term memory. Experiential knowledge stored separately from the rule population that is never lost. Relies on learning that is both incremental and supervised. Stored knowledge may be fed back into LCS during learning.







# Advanced Topics: ExSTraCS Results — 70 & 135-bit Multiplexer Problem 70-bis(2000);Tain 70-bis(2000);Tain 70-bis(2000);Tain 70-bis(5000);Tain 70-bis(5000);



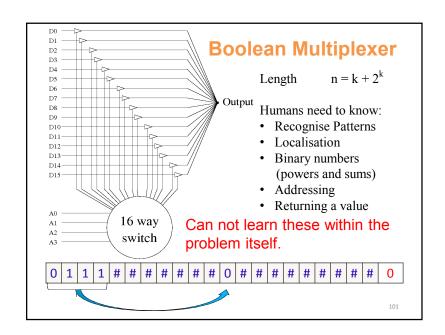
# **CF Hypotheses**

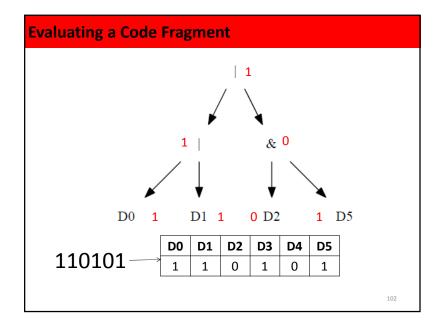
- Different problems in the same domain are likely to contain common patterns
- Patterns in one domain are useful in related domains

This Statement is False

**Abstracted Rules** 'if side guide setting < width, then poor quality product e.g. Abstraction checks for patterns in the base rules and crates and abstracted rules for each discovered pattern Base rules e.g. if side-guide-setting = 80, width = 82 then poor quality product if side-guide-setting = 79, width = 80 then poor quality product Learning system Raw Data https://youtu.be/\_MBKVZjB9Io e.g. Features 'side-guide setting', 'width' : 'product quality' 81 poor 79 80 poor 78 76 good

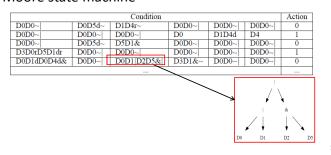
**Abstracted Rules** 

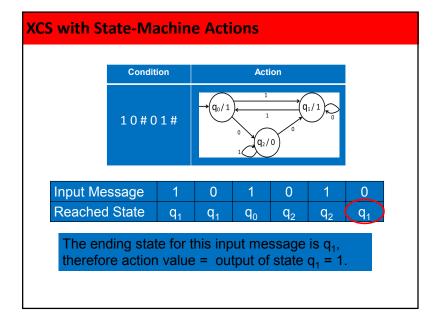


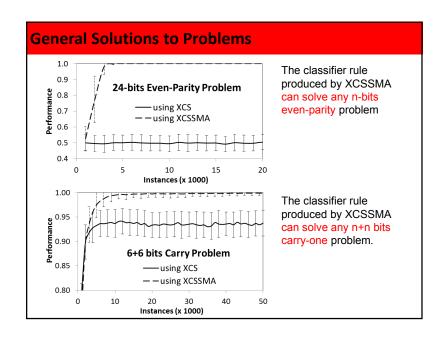


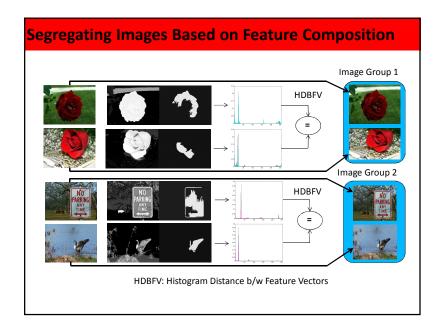
#### **CF Systems**

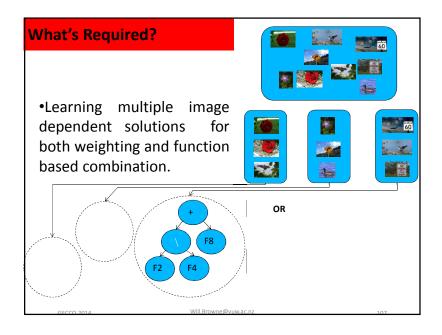
- XCSCFC CF in the condition part
- XCSCFA CF in the action part
- XCSRCFA Real coded, CF in the action part
- XCSSMA Replaced the static binary action with a Moore state machine

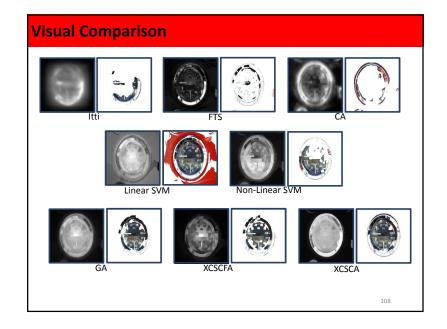


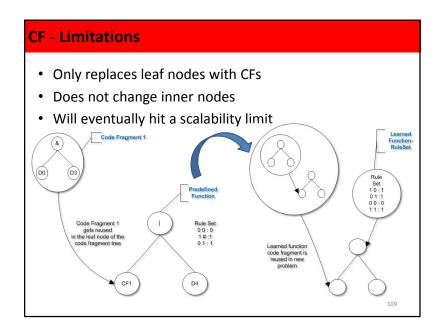


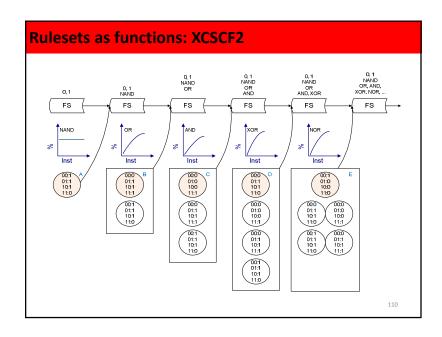


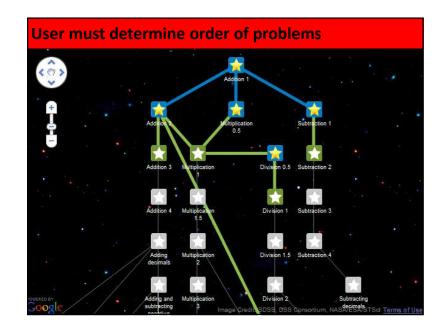


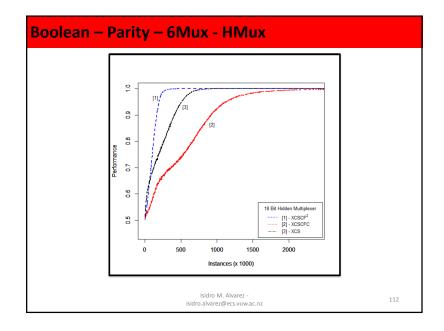












#### **Resources** – Additional Information

- Additional Information :
  - Keep up to date with the latest LCS research
  - . Get in contact with an LCS researcher
  - Contribute to the LCS community research and discussions
- Active Websites:
  - GBML Central <a href="http://gbml.org/">http://gbml.org/</a>
  - Illinois GA Lab <a href="http://www.illigal.org">http://www.illigal.org</a>
- \* LCS Researcher Webpages:
  - Urbanowicz, Ryan <a href="http://www.ryanurbanowicz.com/">http://www.ryanurbanowicz.com/</a>
  - Browne, Will <a href="http://ecs.victoria.ac.nz/Main/WillBrowne">http://ecs.victoria.ac.nz/Main/WillBrowne</a>
  - Lanzi, Pier Luca <a href="http://www.pierlucalanzi.net/">http://www.pierlucalanzi.net/</a>
  - Wilson, Stewart <a href="https://www.eskimo.com/~wilson/">https://www.eskimo.com/~wilson/</a>
  - Bacardit, Jaume http://homepages.cs.ncl.ac.uk/jaume.bacardit/
  - Holmes, John <a href="http://www.med.upenn.edu/apps/faculty/index.php/g359/c1807/p19936">http://www.med.upenn.edu/apps/faculty/index.php/g359/c1807/p19936</a>
  - Kovacs, Tim <a href="http://www.cs.bris.ac.uk/home/kovacs/">http://www.cs.bris.ac.uk/home/kovacs/</a>
  - Bull, Larry http://www.cems.uwe.ac.uk/~lbull/
- International Workshop Learning Classifier Systems (IWLCS) held annually at GECCO
  - Renamed for GECCO '15 Evolutionary Rule-based Machine Learning
- Other:
  - Mailing List:: Yahoo Group: lcs-and-gbml @ Yahoo
  - Proceedings of IWLCS
  - Annual Special Issue of Learning Classifier Systems published by Evolutionary Intelligence
    - NEW ISSUE THEME: 20 Years of XCS!!! Dedicated to Stewart Wilson

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#### **Resources** – LCS Review Papers & Books

- Select Review Papers:
  - Bull, Larry. "A brief history of learning classifier systems: from CS-1 to XCS and its variants." Evolutionary Intelligence (2015): 1-16.
  - Bacardit, Jaume, and Xavier Llorà. "Large-scale data mining using genetics-based machine learning." Wiley Interdisciplinary Reviews: Data Mining and Knowledge Discovery 3.1 (2013): 37-61.
  - Urbanowicz, Ryan J., and Jason H. Moore. "Learning classifier systems: a complete introduction, review, and roadmap." Journal of Artificial Evolution and Applications 2009 (2009): 1.
  - Sigaud, Olivier, and Stewart W. Wilson. "Learning classifier systems: a survey." Soft Computing 11.11 (2007): 1065-1078.
  - Holland, John H., et al. "What is a learning classifier system?." Learning Classifier Systems. Springer Berlin Heidelberg, 2000. 3-32.
  - Lanzi, Pier Luca, and Rick L. Riolo. "A roadmap to the last decade of learning classifier system research (from 1989 to 1999)." Learning Classifier Systems. Springer Berlin Heidelberg, 2000. 33-61.
- Books:
  - NOTE: Brown & Urbanowicz are preparing an <u>Introductory LCS Textbook</u> hopefully available this year. (Springer)
  - Drugowitsch, J., (2008) <u>Design and Analysis of Learning Classifier Systems: A Probabilistic Approach.</u>
     Springer-Verlag.
  - Bull, L., Bernado-Mansilla, E., Holmes, J. (Eds.) (2008) Learning Classifier Systems in Data Mining. Springer
  - Butz, M (2006) Rule-based evolutionary online learning systems: A principled approach to LCS analysis and design. Studies in Fuzziness and Soft Computing Series, Springer.
  - Bull, L., Kovacs, T. (Eds.) (2005) Foundations of learning classifier systems. Springer.
  - \* Kovacs, T. (2004) Strength or accuracy: Credit assignment in learning classifier systems. Springer.
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  - Lanzi, P.L., Stolzmann, W., Wilson, S., (Eds.) (2000). <u>Learning classifier systems: From foundations to applications</u> (LNAI 1813). Springer.
  - Holland, J. H. (1975). Adaptation in natural and artificial systems. University of Michigan Press.

**Resources** - Software

- Educational LCS (eLCS) in Python.
  - http://sourceforge.net/projects/educationallcs/
  - Simple Michigan-style LCS for learning how they work and how they are implemented.
  - Code intended to be paired with first LCS introductory textbook by Brown/Urbanowicz.
- ExSTraCS 2.0 Extended Supervised Learning LCS in Python
  - http://sourceforge.net/projects/exstracs/
  - For prediction, classification, data mining, knowledge discovery in complex, noisy, epistatic, or heterogeneous problems.
- BioHEL Bioinformatics-oriented Hierarchical Evolutionary Learning in C++
  - http://ico2s.org/software/biohel.html
  - GAssist also available through this link.
- XCS & ACS (by Butz in C and Java) & XCSLib (XCS and XCSF) (by Lanzi in C++)
  - http://www.illigal.org
- XCSF with function approximation visualization in Java
  - http://medal.cs.umsl.edu/files/XCSFJava1.1.zip
- EpiXCS

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#### Conclusion

- ❖What and Why
  - Many branches of RBML, e.g. ARM, AIS, LCS
  - ❖ Powerful, human interpretable, learning algorithms
- Driving Mechanisms
  - Discovery
  - Learning
- ❖How?
  - LCS Algorithm Walk-Through
  - Flexible and robust methods developed
- Multiple styles
- Advanced methods: solutions to complex & real-world problems
- Many Resources Available

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- 23) Urbanowicz, Ryan J., Ambrose Granizo-Mackenzie, and Jason H. Moore. "An analysis pipeline with statistical and visualization-guided knowledge discovery for michigan-style learning classifier systems." Computational Intelligence Magazine, IEEE 7.4 (2012): 35-45.
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