Introducing Rule-Based Machine Learning: Capturing Complexity

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Instructor

Ryan Urbanowicz is a post-doctoral research associate at the University of Pennsylvania in the Pearlman School of Medicine. He completed a Bachelors and Masters degree in Biological Engineering at Cornell University (2004 & 2005) and a Ph.D in Genetics at Dartmouth College (2012). His research focuses on the methodological development and application of learning classifier systems to complex, heterogeneous problems in bioinformatics, genetics, and epidemiology.



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Bladder Cancer Study: Clinical Variable Analysis-Survivorship

Course Agenda

- Introduction (What and Why?)
 - LCS Applications
 - Distinguishing Features of an LCS
 - Historical Perspective
- Driving Mechanisms
 - Discovery
 - Learning
- LCS Algorithm Walk-Through (How?)
 - * Rule Population
 - Set Formation
 - Covering
 - Prediction/Action Selection
 - Parameter Updates/Credit Assignment
 - Subsumption
 - Genetic Algorithm
 - Deletion
- Michigan vs. Pittsburgh-style
- Advanced Topics
- Resources

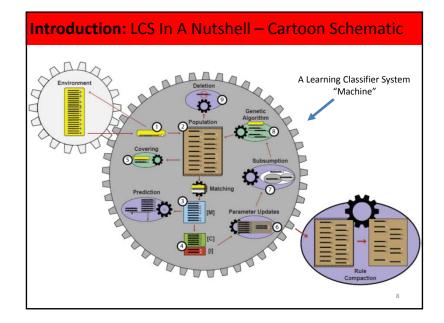
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Introduction: What is Rule-Based Machine Learning?

- Rule Based Machine Learning (RBML)
- What types of algorithms fall under this label?
 - Learning Classifier Systems (LCS)*
 - Michigan-style LCS
 - Pittsburgh-style LCS
 - * Association Rule Mining
 - * Related Algorithms
 - Artificial Immune Systems
- Rule-Based The solution/model/output is collectively comprised of individual rules typically of the form (IF: THEN).
- Machine Learning "A subfield of computer science that evolved from the study of pattern recognition and computational learning theory in artificial intelligence. Explores the construction and study of algorithms that can learn from and make predictions on data." – Wikipedia
- * Keep in mind that machine learning algorithms exist across a continuum.
 - Hybrid Systems
 - Conceptual overlaps in addressing different types of problem domains.

* LCS algorithms are the focus of this tutorial.

Introduction: LCS In A Nutshell – A Classic Schematic **INPUT** One Training Instance Deletion Data Set Genetic Covering [P] Algorithm 8 **ENVIRONMENT** 3 Prediction Subsumption 7 Rule Compaction [1] [C] [P.] Update Rule Parameters OUTPUT **Learning Cycle**



Introduction: Comparison of RBML Algorithms

Learning Classifier Systems (LCS)

- Developed primarily for modeling, sequential decision making, classification, and prediction in complex adaptive system.
- ◆ IF:THEN rules link independent variable states to dependent variable states. e.g. {V₁, V₂, V₃} → Class/Action

* Association Rule Mining (ARM)

- Developed primarily for discovering interesting relations between variables in large datasets.
- F:THEN rules link independent variable(s) to some other independent variable e.g. {V₁, V₂, V₃} → V₄

Artificial Immune Systems (AIS)

- Developed primarily for anomaly detection (i.e. differentiating between self vs. not-self)
- Multiple 'Antibodies' (i.e. detectors) are learned which collectively characterize 'self' or "not-self' based on an affinity threshold.

What's in common?

- In each case, the solution or output is determined piece-wise by a set of `rules' that each cover part of the problem at hand. No single, 'model' expression is output that seeks to describe the underlying pattern(s).
- This tutorial will focus on LCS algorithms, and approach them initially from a supervised learning perspective (for simplicity).

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Introduction: Why LCS Algorithms? {2 of 3}

Other Advantages

- Applicable to single-step or multi-step problems.
- Representation Flexibility: Can accommodate discrete or continuous-valued endpoints* and attributes (i.e. Dependent or Independent Variables)
- Can learn in clean or very noisy problem environments.
- Accommodates missing data (i.e. missing attribute values within training instances).
- * Classifies binary or multi-class discrete endpoints (classification).
- Can accommodate balanced or imbalanced datasets (classification).

* We use the term `endpoints' to generally refer to dependent variables .

Introduction: Why LCS Algorithms? {1 of 3}

- Adaptive Accommodate a changing environment. Relevant parts of solution can evolve/update to accommodate changes in problem space.
- ❖ Model Free Limited assumptions about the environment*
 - Can accommodate complex, epistatic, heterogeneous, or distributed underlying patterns.
 - No assumptions about the number of predictive vs. non-predictive attributes (feature selection).
- Ensemble Learner (unofficial) No single model is applied to a given instance to yield a prediction. Instead a set of relevant rules contribute a 'vote'.
- Stochastic Learner Non-deterministic learning is advantageous in large-scale or high complexity problems, where deterministic learning becomes intractable.
- Multi-objective (Implicitly) Rules evolved towards accuracy and generality/simplicity.
- Interpretable (Data Mining/Knowledge Discovery) Depending on rule representation, individual rules are logical and human readable IF:THEN statements. Strategies have been proposed for global knowledge discovery over the rule population solution [23].
- * The term `environment' refers to the source of training instances for a problem/task. 10

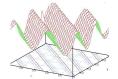
Introduction: Why LCS Algorithms? {3 of 3} LCS Algorithms: One concept, many components, infinite combinations. Rule Representations Learning Strategy Discovery Mechanisms Selection Mechanisms Prediction Strategy Fitness Function Supplemental Heuristics Many Application Domains Cognitive Modeling Complex Adaptive Systems Reinforcement Learning Supervised Learning Unsupervised Learning (rare) Metaheuristics Data Mining ***** ... 12 *Slide adapted from Lanzi Tutorial: GECCO 2014

Introduction: LCS Applications - General

- Categorized by the type of learning and the nature of the endpoint predictions.
- Supervised Learning:
 - Classification / Data Mining Problems: (Label
 - Find a compact set of rules that classify all
 - Function Approximation Problems & Regression: (Numerical prediction)
 - Find an accurate function approximation represented by a partially overlapping set of approximation rules.
- Reinforcement Learning Problems & Sequential Decision Making
 - Find an optimal behavioral policy represented by a compact set of rules.









Introduction: LCS Applications – Uniquely Suited

- Uniquely Suited To Problems with...
 - Dvnamic environments
 - Perpetually novel events accompanied by large amounts of noisy or irrelevant data.
 - Continual, often real-time, requirements for actions.
 - Implicitly or inexactly defined goals.
 - Sparse payoff or reinforcement obtainable only through long action sequences [Booker 89].
- And those that have...
 - High Dimensionality
 - Noise
 - Multiple Classes
 - Epistasis
 - Heterogeneity
 - Hierarchical dependencies
 - Unknown underlying complexity or dynamics

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Introduction: LCS Applications – Specific Examples

Search

Medical Diagnosis

Design

Optimisation

Modelling

Scheduling

Routing

Adaptive-control

Knowledge-Handling

Prediction

Visualisation

Feature Selection

Querving

Image classification

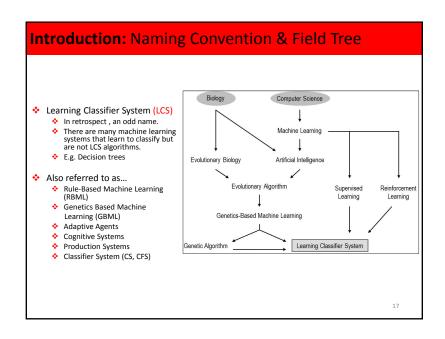
Game-playing

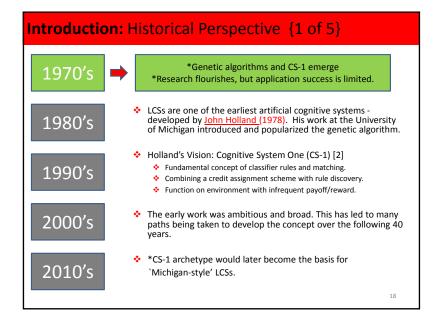
Navigation

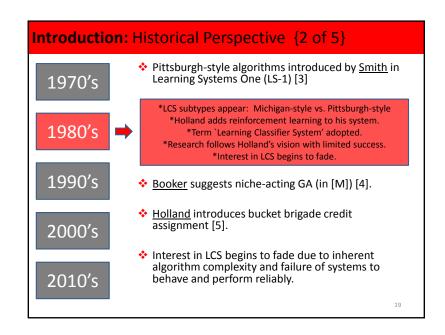
Rule-Induction Data-mining

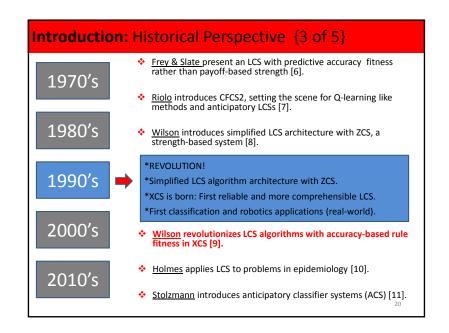
Introduction: Distinguishing Features of an LCS

- Learning Classifier Systems typically combine:
 - Global search of evolutionary computing (e.g. Genetic Algorithm)
 - Local optimization of machine learning (supervised or reinforcement) THINK: Trial and error meets neo-Darwinian evolution.
- Solution/output is given by a set of IF:THEN rules.
 - Learned patterns are distributed over this set.
 - Output is a distributed and generalized probabilistic prediction
 - ❖ IF:THEN rules can specify any subset of the attributes available in the
 - IF:THEN rules are only applicable to a subset of possible instances.
 - ❖ IF:THEN rules have their own parameters (e.g. accuracy, fitness) that reflect performance on the instances they match.
 - Rules with parameters are termed 'classifiers.
- Incremental Learning (Michigan-style LCS)
 - Rules are evaluated and evolved one instance from the environment
- Online or Offline Learning (Based on nature of environment)









Introduction: Historical Perspective {4 of 5} Wilson introduces XCSF for function approximation [12]. * Koyacs explores a number of practical and theoretical LCS 1970's questions [13,14]. Bernado-Mansilla introduce UCS for supervised learning [15]. Bull explores LCS theory in simple systems [16]. Bacardit introduces two Pittsburgh-style LCS systems GAssist and 1980's BioHEL with emphasis on data mining and improved scalability to larger datasets[17,18]. Holmes introduces EpiXCS for epidemiological learning. Paired with the first LCS graphical user interface to promote accessibility and ease of use [19]. 1990's Butz introduces first online learning visualization for function approximation [20]. Lanzi & Loiacono explore computed actions [21]. *LCS algorithm specializing in supervised learning and data 2000's mining start appearing. *LCS scalability becomes a central research theme. *Increasing interest in epidemiological and bioinformatics. 2010's *Facet-wise theory and applications

Introduction: Historical Perspective {5 of 5} Franco & Bacardit explored GPU parallelization of LCS for scalability [22]. Urbanowicz & Moore introduced statistical and visualization strategies for 1970's knowledge discovery in an LCS [23]. Also explored use of 'expert knowledge' to efficiently guide GA [24], introduced attribute tracking for explicitly characterizing heterogeneous patterns [25]. Browne and Iqbal explore new concepts in reusing building blocks (i.e., code 1980's fragments). Solved the 135-bit multiplexer reusing building blocks from simpler multiplexer problems [26]. Bacardit successfully applied BioHEL to large-scale bioinformatics problems also exploring visualization strategies for knowledge discovery [27]. 1990's Urbanowicz introduced ExSTraCS for supervised learning [28]. Applied ExSTraCS to solve the 135-bit multiplexer directly. *Increased interest in supervised learning applications persists. 2000's *Emphasis on solution interpretability and knowledge discovery. *Scalability improving - 135-bit multiplexer solved! *GPU interest for computational parallelization. 2010's *Broadening research interest from American & European to include Australasian & Asian.

Introduction: Historical Perspective - Summary 1970's ❖~40 years of research on LCS has... 1980's Clarified understanding. Produced algorithmic descriptions. Determined 'sweet spots' for run parameters. 1990's Delivered understandable 'out of the box' code. ❖Demonstrated LCS algorithms to be... Flexible ❖Widely applicable 2000's Uniquely functional on particularly complex problems. 2010's 23

Driving Mechanisms

Two mechanisms are primarily responsible for driving LCS algorithms.

Discovery

- Refers to "rule discovery".
- * Traditionally performed by a genetic algorithm (GA).
- Can use any directed method to find new rules.

Learning

- The improvement of performance in some environment through the acquisition of knowledge resulting from experience in that environment.
- Learning is constructing or modifying representations of what is being experienced.
- AKA: Credit Assignment
- LCSs traditionally utilized reinforcement learning (RL).
- Many different RL schemes have been applied as well as much simpler supervised learning schemes.

Driving Mechanisms: LCS Rule Discovery {1 of 2}

- Create hypothesised better rules from existing rules & genetic material.
 - Genetic algorithm
 - · Original and most common method
 - Well studied
 - Stochastic process
 - · The GA used in LCS is most similar to niching GAs
 - Estimation of distribution algorithms
 - Sample the probability distribution, rather than mutation or crossover to create new rules
 - · Exploits genetic material
 - Bayesian optimisation algorithm
 - · Use Bayesian networks
 - · Model-based learning

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Driving Mechanisms: LCS Rule Discovery {2 of 2}

When to learn

Too frequent: unsettled [P]

Too infrequent: inefficient training



What to learn

Most frequent niches or...

Underrepresented niches

How much to learn

How many good rules to keep (elitism)

Size of niche

Driving Mechanisms: Genetic Algorithm (GA)

- ❖ Inspired by the neo-Darwinist theory of natural selection, the evolution of rules is modeled after the evolution of organisms using four biological analogies.
 - ❖ Genome → Coded Rule (Condition)

Example Rules (Ternary Representation)

❖ Phenotype → Class (Action)

Condition ~ Action

❖ Survival of the Fittest → Rule Competition

#101# ~ 1

❖ Genetic Operators → Rule Discovery

#10## ~ 0 00#1# ~ 0

1#011 ~ 1

Elitism (Essential to LCS)

- LCS preserves the majority of top rules each learning iteration.
- Rules are only deleted to maintain a maximum rule population size (N).

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Driving Mechanisms: GA – Mutation Operator

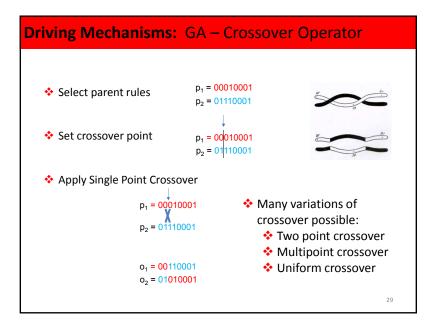
Select parent rule

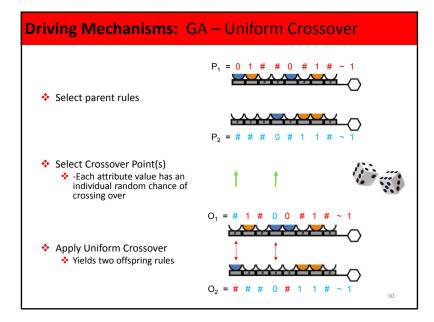
 $r_1 = 01110001$

Randomly select bit to mutate $r_1 = 0.1110001$

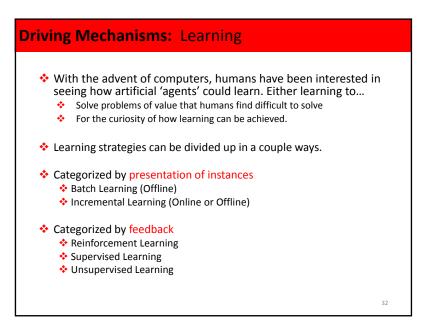
Apply mutation

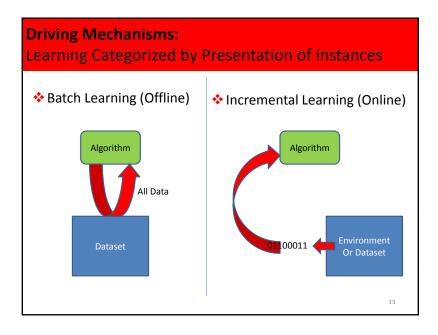
 $r_1 = 01100001$





Driving Mechanisms Two mechanisms are primarily responsible for driving LCS algorithms. Discovery * Refers to "rule discovery" Traditionally performed by a genetic algorithm (GA) Can use any directed method to find new rules Learning ❖ The improvement of performance in some environment through the acquisition of knowledge resulting from experience in that environment. Learning is constructing or modifying representations of what is being experienced. * AKA: Credit Assignment LCSs traditionally utilized reinforcement learning (RL). ❖ Many different RL schemes have been applied as well as much simpler supervised learning (SL) schemes. 31





Driving Mechanisms: Learning Categorized by Feedback

Supervised learning: The environment contains a teacher that directly provides the correct response for environmental states.

Unsupervised learning:

The learning system has an internally defined teacher with a prescribed goal that does not need utility feedback of any kind.

Reinforcement learning: The environment does not directly indicate what the correct response should have been. Instead, it only provides reward or punishment to indicate the utility of actions that were actually taken by the system.

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Driving Mechanisms: LCS Learning

- LCS learning primarily involves the update of various rule parameters such as...
 - Reward prediction (RL only)
 - Error
 - Fitness
- Many different learning strategies have been applied within LCS algorithms.
 - Bucket Brigade [5]
 - Implicit Bucket Brigade
 - One-Step Payoff-Penalty
 - Symmetrical Payoff Penalty
 - Multi-Objective Learning
 - Latent Learning
 - Widrow-Hoff [8]
 - Supervised Learning Accuracy Update [15]
 - Q-Learning-Like [9]
- Fitness Sharing
 - Give rule fitness some context within niches.

Driving Mechanisms: Assumptions for Learning

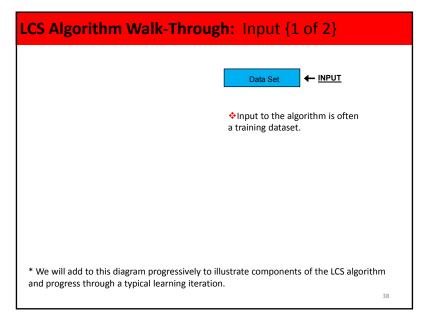
- In order for artificial learning to occur data containing the patterns to learn is needed.
- This can be through recorded past experiences or interactive with current events.
- ❖ If there are no clear patterns in the data, then LCSs will not learn.

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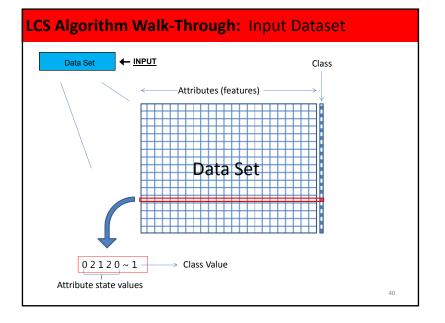
LCS Algorithm Walk-Through

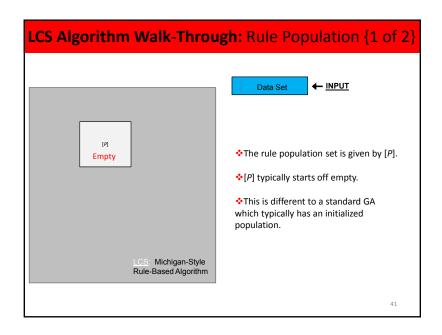
- Demonstrate how a fairly typical modern Michigan-style LCS algorithm...
 - is structured,
 - is trained on a problem environment,
 - * makes predictions within that environment
- We use as an example, an LCS architecture most similar to UCS [15], a supervised learning LCS.
- We assume that it is learning to perform a classification/prediction task on a training dataset with discrete-valued attributes, and a binary endpoint.
- We provide discussion and examples beyond the UCS architecture throughout this walk-through to illustrate the diversity of system architectures available.

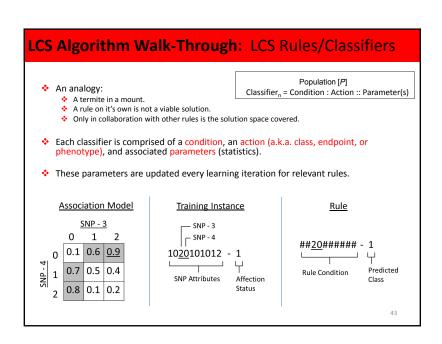
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LCS Algorithm Walk-Through: Input {2 of 2} Detectors Sense the current state of the environment and encode it as a formatted data instance. Detectors Grab the next instance from a finite training dataset. Effectors Translate action messages into performed actions that Environment modify the state of the environment The learning capabilities of LCS rely on and are Effectors constrained by the way the agent perceives the environment, e.g., by the detectors the system employs. Input data may be binary, integer, real-valued, or some other custom representation, assuming the LCS algorithm has been coded to handle it. 39







LCS Algorithm Walk-Through: Rule Population {2 of 2} ❖ A finite set of rules [P] which collectively explore the 'search Every valid rule can be thought of as part of a candidate solution (may or may not be good) The space of all candidate solutions is termed the 'search' space'. [P] The size of the search space is determined by both the encoding of the LCS itself and the problem itself. The maximum population size (N) is one of the most critical run parameters. User specified N = 200 to 20000 rules but success depends on dataset dimensions and problem complexity. ❖ Too small → Solution may not be found ❖ Too large → Run time or memory limits too extreme.

. CS Algorithm Walk-Through: Rule Re ^T ernary	
 LCSs can use many different representation schemes. Also referred to as `encodings' 	(Ternary Representation) Condition ~ Class
Suited to binary input or	#101# ~ 1
Suited to real-valued inputs and so forth	#10## ~ 0
 Ternary Encoding – traditionally most commonly used 	00#1# ~ 0
The ternary alphabet matches binary input	1#011 ~ 1
A attribute in the condition that we don't care about is given t symbol '#' (wild card)	he
 For example, 	
101~1 - the Boolean states 'on off on' has action 'or	n'
 001~1 - the Boolean states 'off off on' has action 'o 	n'
 Can be encoded as 	
#01~1 - the Boolean states 'either off on' has action	n 'on'
In many binary instances, # acts as an OR function on {0,1}	
, , , , , , , , , , , , , , , , , , , ,	44

LCS Algorithm Walk-Through: Rule Representation – Other {1 of 4}

- Quaternary Encoding [29]
 - ❖ 3 possible attribute states {0,1,2} plus '#'.
 - For a specific application in genetics.
- Real-valued interval (XCSR [30])
 - Interval is encoded with two variables: center and spread
 - ❖ i.e. [center,spread] → [center-spread, center+spread]
 - i.e. [0.125,0.023] → [0.097, 0.222]
- Real-valued interval (UBR [31])
 - Interval is encoded with two variables: lower and upper bound
 - i.e. [lower, upper]
 - i.e. [0.097, 0.222]
- Messy Encoding (Gassist, BIOHel, ExSTraCS [17,18,28])
 - * Attribute-List Knowledge Representation (ALKR) [33]
 - ❖ 11##0:1 shorten to 110:1 with reference encoding
 - Improves transparency, reduces memory and speeds processing

4.5

Predicted

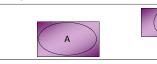
(Quaternary Encoding)

##20##### - 1

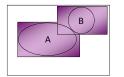
Rule Condition

LCS Algorithm Walk-Through: Rule Representation – Other {2 of 4}

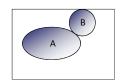
- We have a search space with two classes to identify [A.B]
- Attributes are real numbered so we decide to use bounds:
 - e.g. $0 \le x \le 10$, which works fine in this case...



- We form Hypercubes with the number of dimensions = the number of conditions/attributes.
- In the second example A & B are harder to separate with this encoding, so use Hyperellipsoids instead.



Vs.



Income range of applicant?

Years in present job?

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LCS Algorithm Walk-Through: Rule Representation – Other {3 of 4}

- Mixed Discrete-Continuous ALKR [28]
 - Useful for big and data with multiple attribute types
 - Discrete (Binary, Integer, String)
 - Continuous (Real-Valued)
 - Similar to ALKR (Attribute List Knowledge Representation): [Bacardit et al. 09]
 - Intervals used for continuous attributes and direct encoding used for discrete.



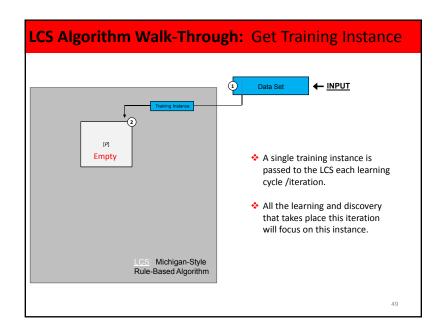


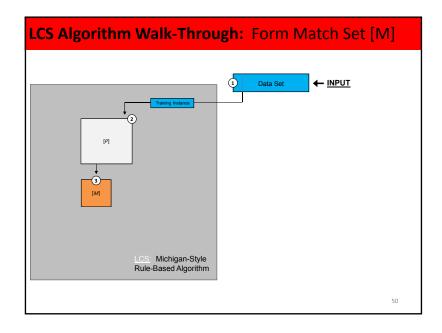
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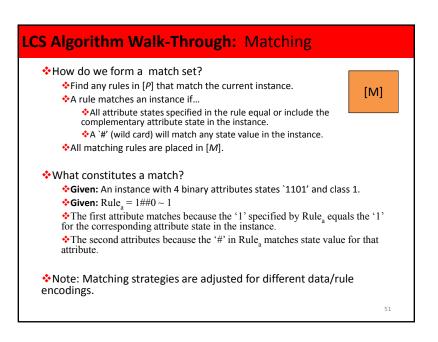
Classification

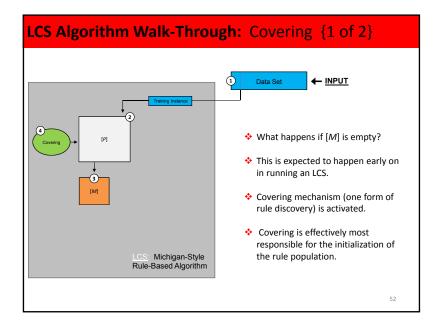
LCS Algorithm Walk-Through: Rule Representation – Other {4 of 4}

- Decision trees [32]
- Code Fragments [26]
- Artificial neural network
- Fuzzy logic/sets
- Horn clauses and logic
- S-expressions, GP-like trees and code fragments.
- NOTE Alternative action encodings also utilized
 - Computed actions replaces action value with a function [21]









LCS Algorithm Walk-Through: Covering {2 of 2}

- Covering initializes a rule by generalizing an instance.
 - Condition: Generalization of instance attribute states.
 - Class:
 - If supervised learning: Assigned correct class
 - ❖ If reinforcement learning: Assigned random class/action
- Covering adds #'s to a new rule with probability of generalization (P_w) of 0.33 - 0.5 (common settings).
- New rule is assigned initial rule parameter values.
- NOTE: Covering will only add rules to the population that match at least one data instance.
 - * This avoids searching irrelevant parts of the search space.

(New Rule)

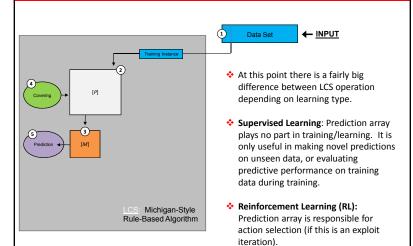
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LCS Algorithm Walk-Through: Special Cases for Matching and Covering

- Matching:
 - Continuous-valued attributes: Specified attribute interval in rule must include instance value for attribute. E.g. [0.2, 0.5] includes 0.34.
 - Alternate strategy-
 - Partial match of rule is acceptable (e.g. 3/4 states). Might be useful in high dimensional problem spaces.
- Covering:
 - For supervised learning also activated if no rules are found for [C]
 - Alternate activation strategies-
 - * Having an insufficient number of matching classifiers for:
 - Given class (Good for best action mapping)
 - All possible classes (Good for complete action mapping and reinforcement learning)
 - Alternate rule generation-
 - * Rule specificity limit covering [28]:
 - Removes need for P_{#.}, useful/critical for problems with many attributes or high dimensionality.
 - Picks some number of attributes from the instance to specify up to a datasetdependent maximum.

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LCS Algorithm Walk-Through: Prediction Array {1 of 3}



LCS Algorithm Walk-Through:Prediction Array {2 of 3}

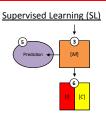
- Rules in [M] advocate for different classes!
- Want to predict a class (known as action selection in RL).
- In SL, prediction array just makes prediction.
- In RL, prediction array choses predicted action during exploit phase. A random action is chosen for explore phases. This action is sent out into the environment. All rules in [M] with this chosen action forms the action set [A].
- Consider the fitness (F) of the rules in an SL example.

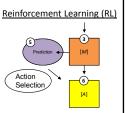
Rule_a $1##101 \sim 1$ F = 0.8,

Rule, $1\#0\#1 \sim 0 \quad F = 0.3$,

Rule_o $1##1#1 \sim 0$ F = 0.4, ...

- Class/Action can be selected:
 - Deterministically Class of classifier with best F in [M].
 - Probabilistically Class with best average F across rules in [M], i.e. Classifiers vote for the best class.

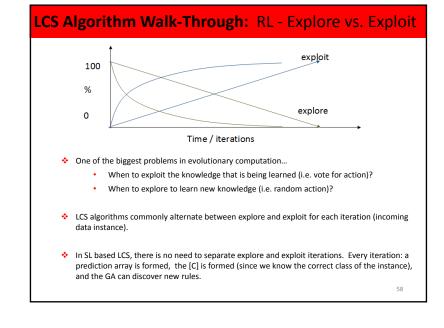


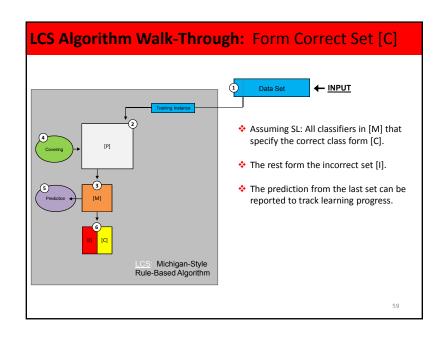


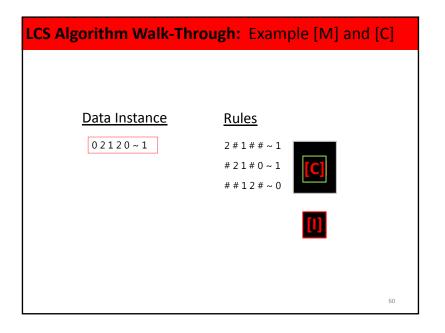
LCS Algorithm Walk-Through: Prediction Array {3 of 3} Prediction Arrays in Reinforcement Learning: Prediction vote can be based on different metrics * Total predicted payoff - MCS [16] In RL, prediction array choses predicted action during exploit phase. A random action is chosen for explore phases. This action is sent out into the environment. All rules in [M] with this chosen action forms the action set [A]. . Consider the fitness (F) of the rules in an SL example. $1##101 \sim 1$ F = 0.8, Rule Reinforcement Learning (RL) $1#0##1 \sim 0$ F = 0.3, $1##1#1 \sim 0$ F = 0.4, ...Class/Action can be selected: ❖ <u>Deterministically</u> – Class of classifier with best F in [M]. Selection

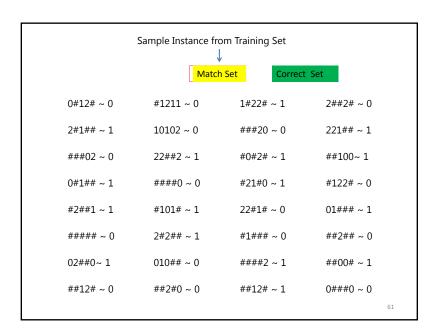
Probabilistically - Class with best average F across

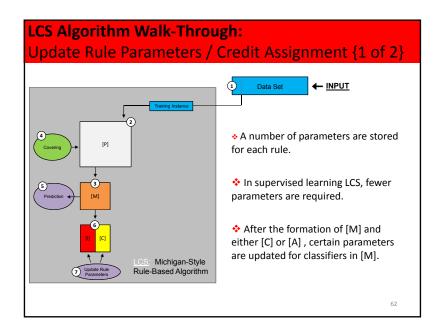
rules in [M], i.e. Classifiers vote for the best class.











LCS Algorithm Walk-Through: Update Rule Parameters / Credit Assignment {2 of 2} ❖ An action/class has been chosen and passed to the environment.

❖ Supervised Learning:

Update Rule Parameters

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- ❖ Parameter Updates:
 - ❖Rules in [C] get boost in accuracy.
 - ❖Rules in [M] that didn't make it to [C] get decreased in accuracy.
- * Reinforcement Learning:
 - ❖ A reward may be returned from the environment
 - *RL parameters are updated for rules in [M] and/or [A]

LCS Algorithm Walk-Through: Credit Assignment for Reinforcement Learning Reinforcement Learning (RL) LCS algorithms were originally all designed with RL in mind. Credit traditionally took the form of classifier strength The cumulative credit coming from reward feedback from the environment . This reflects the reward the system can expect if that rule is fired. Two examples of strength-based credit assignment/fitness: ZCS – Zeroth-Level Classifier System [8] Implicit Bucket Brigade back-propagation of strength (deferred reward) Fraction (β) of strength of all rules in [A] is placed in a common 'bucket'. If an immediate reward (r_{imm}) is received from environment all rules in [A] add (β r_{imm}) Classifiers in the action set of the previous time-step [A]_{.1} receive a discounted (γ) distribution of the strength put in the 'bucket' (back-propagation) Total strength of members of [A] $S_{[A]} \leftarrow S_{[A]} - \beta S_{[A]} + \beta r_{imm} + \beta \gamma S_{[A]}$ Action Set [A] MCS – Minimal Classifying System [16] Widrow-Hoff delta rule with learning rate 8 value_{new} = value + β x (signal - value) Filters the 'noise' in the reward signal β = 1 the new value is signal, β = 0 then old value kept Learning Strategy Credit Assignment • $f_i < f_i + \beta ((P/|[A]|) - f_i)$

LCS Algorithm Walk-Through: Fitness Sharing

- Fitness sharing takes the strength/payoff and updates a fitness so that the strength of a classifier is considered relative to the strengths of other classifiers in the action set.
- This pressures the classifiers with the best strength relative to their niche to have the highest fitness. This helps eliminate the takeover effect of 'strong' classifiers from one particular niche.
- Niche: A set of environmental states each of which is matched by approximately the same set of classifiers.
- We will detail fitness sharing in the context of XCS and accuracy-based fitness.

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LCS Algorithm Walk-Through:

Why not Strength vs. Accuracy-based Fitness in RL?

- Different niches of the environment usually have different payoff levels.
- In fitness sharing classifier's strength no longer correctly predicts payoff Fitness sharing prevents takeover
- Fitness sharing does not prevent more renumerative niches gaining more classifiers -Niche rule discovery helps
- Rule discovery cannot distinguish an accurate classifier with moderate payoff from an overly general classifier having the same payoff on average – Over-generals proliferate
- No reason for accurate generalizations to evolve
- ZCS -> XCS: "Wilson's intuition was the prediction should estimate how much reward might result from a certain action but that the evolution learning should be focused on the most reliable classifiers, that is, classifiers that give a more precise (accurate) prediction)"

LCS Algorithm Walk-Through:

XCS Accuracy-Based Fitness + Fitness Sharing

- Classifier considered accurate if:
 - Error < tolerance, otherwise scaled.

$$\varepsilon \leftarrow \varepsilon + \beta (|R - p| - \varepsilon),$$

$$\kappa = \begin{cases} 1 & \text{if } \varepsilon < \varepsilon_0 \\ \varepsilon < \varepsilon_0 \end{cases}$$

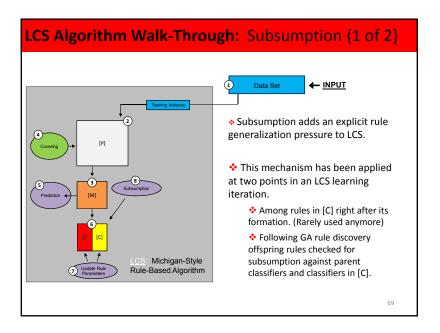
Accuracy relative to action set

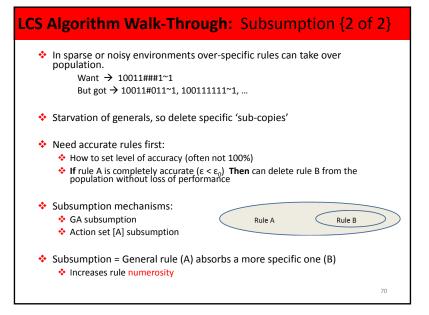
$$\kappa' = \frac{\kappa}{\sum_{x \in [A]} \kappa_x}$$

Fitness based on relative accuracy, e.g. XCS $F \leftarrow F + \beta(\kappa' - F)$

 $p \leftarrow p + \beta (R - p)$

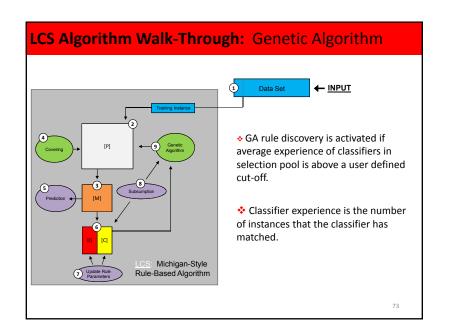
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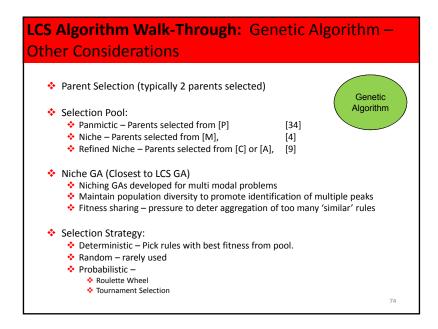


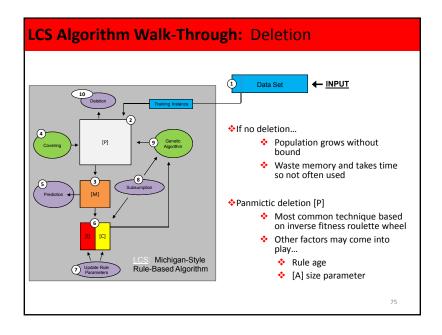


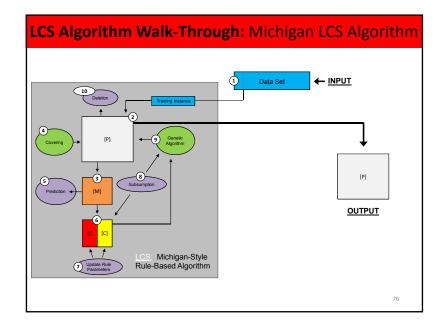
**Numerosity is a useful concept (trick): **Reduces memory usage * Instead of population carrying multiple copies of the same classifier it just carries one copy. * Each rule has a numerosity value (initialised as 1) * Protects rule from deletion * Stabilises rule population * Numerosity is increased by 1 * When subsumes another rule * When RD makes a copy * Numerosity is decreased by 1 * Rule is selected for deletion

CS Algorithm Walk-Through: Numerosity {2 of 2} Numerosity (n) affects action selection and update procedures: The fitness sums take numerosity into account: Terminology: Macroclassifiers: all unique classifiers n ≥ 1 Microclassifiers: all individual classifiers (n copies of macroclassifiers) Ratio of macroclassifiers to microclassifiers often used as a measure of training progress. Numerosity is also often applied as a `best-available' strategy to ranking rules for manual rule inspection (i.e. knowledge discovery).









Break – 5 min

- Michigan vs. Pittsburgh LCS
- Advanced Topics,
- and Available Resources to Follow

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Michigan vs. Pittsburgh-Style LCSs: Major Variations

Michigan-Style LCS Rule string / chaosifer Pittsbur

Pittsburgh-Style LCS

- Entire population is the solution
- Single rule-set is the solution
- Learns iteratively
- Learns batch-wise
- GA operates between individual rules
- GA operates between rule-sets

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Michigan vs. Pittsburgh-Style LCSs: Implementations

Michigan Style LCS

- ZCS (Strength Based)
- XCS (Accuracy Based Most popular)
- UCS (Supervised Learning)
- ❖ ACS (Anticipatory)
- ❖ ExSTraCS (Extended Supervised Tracking and Learning)

Pittsburgh Style LCS

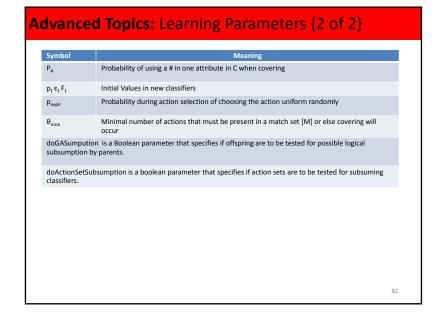
- ❖ GALE (Spatial Rule Population)
- GAssist (Data mining Pitt Style Archetype)
- ❖ BIOHEL (Focused on Biological Problems and Scalability)
- Other Hybrid Styles also exist!

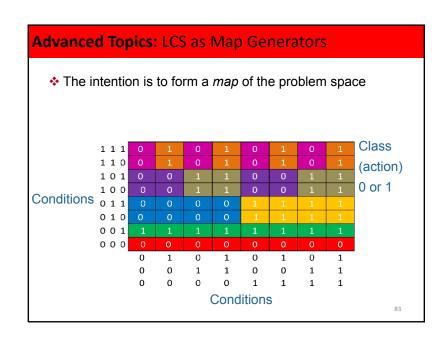
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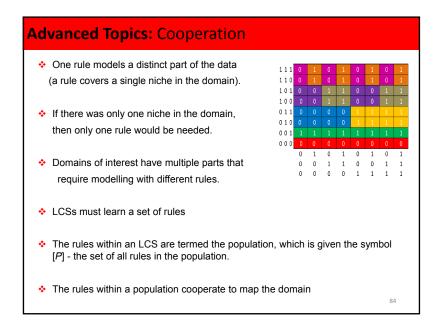
LCS Disadvantages

- Not widely known.
- * Relatively limited software accessibility.
- Rule population interpretation and knowledge extraction can be challenging.
- Can suffer from overfitting, despite explicit and implicit pressures to generalize rules.
- * Relatively little theoretical work or convergence proofs.
- Many run parameters to consider/optimize.

Symbol	Meaning
N	Maximum size of the population (In micro-classifiers, N is the number sum of the classifier numerosities)
β	Learning rate for p, ϵ , f, and as
α, ε ₀ , ν	Used in calculating the fitness of a classifier
γ	Discount factor used (in multi-step problems) in updating classifier predictions
θ_{GA}	GA threshold The GA is applied when the average time since the last GA in the lest is greater than the threshold.
χ	Probability of applying crossover in GA
μ	Probability of mutating an allele in the offspring
θ_{del}	Deletion threshold If the experience of a classifier is greater than $\theta_{\text{del}\prime}$ its fitness may be considered in its probability of deletion
δ	Mean fitness in [P] below which the fitness of a classifier may be considered in its probability of deletion
θ_{sub}	Subsumption threshold – the experience of a classifier must be greater than θ_{sub} in order to be able to subsume another classifier



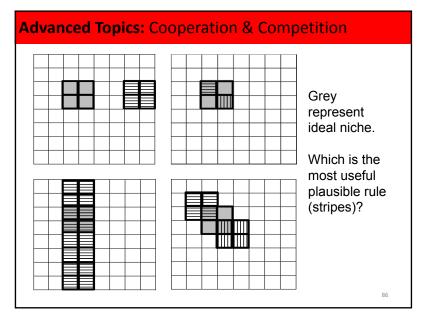




Advanced Topics: Competition

- Ideally, there would only be one unique and correct rule for each niche
- Number of rules would equal number of niches
- No prior knowledge, so each rule must be learnt.
- LCSs allow multiple, slightly different rules per niche Multiple hypotheses are available to find the optimum rule
- * Each rule 'covers', i.e. describes, its part of the search space.
- The rules within a niche compete to map the domain.

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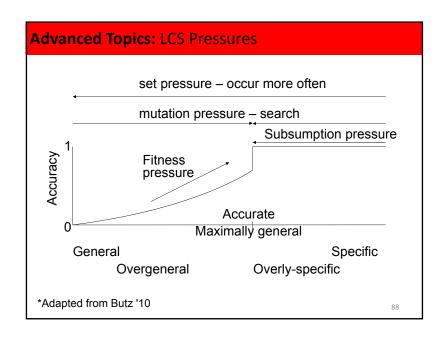
Advanced Topics: Over-generals

- Over-generals are undesired, inaccurate rules that typically match many instances
- When additional reward offsets any additional penalty
- Strength-based fitness is more prone to overgenerals
- Accuracy-based fitness is less prediction orientated

Want 10011###1:1 get 10011###:1, where 10011###0:0

* Can occur in unbalanced datasets or where the error tolerance ϵ_0 is set too high.





Advanced Topics: Fitness Pressure

- Fitness pressure is fundamental to evolutionary computation: "survival of the fittest"
- Fitter rules assumed to include better genetic material,
- Fitter rules are proportionately more likely to be selected for mating,
- Genetic material hypothesised to improve each generation.
- Fitness measures based on error or accuracy drive the population to rules that don't make mistakes
- Favours specific rules (cover less domain)
- Fitness measures based on reward trade mistakes for more reward
- Favours general rules (cover more domain)

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- 1

Advanced Topics: Set Pressure

- Set pressure is related to the opportunity to breed,
- Does not occur in panmictic rule selection
- Need Niching through [M] or [A] rule discovery
- Class imbalance affects set pressure
- Set pressure is more effective when replacing 'weaker' rules
- Often panmictic deletion, thus one action can replace a different action
- To prevent an action type disappearing, relative fitness is used (rare rules have high relative fitness and so breed)
- Rules that occur in more sets have more opportunity to be selected from mating
- · Favours general rules

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Advanced Topics: Mutation Pressure

- Genotypically change the specificity-generality balance
- Mutation can

Randomise:

Generalise:

Specialise:

0 ← 1 or # 1 ← 0 or #

0 ← #

0 ←

← 0 or 1

.

← 0 or 1

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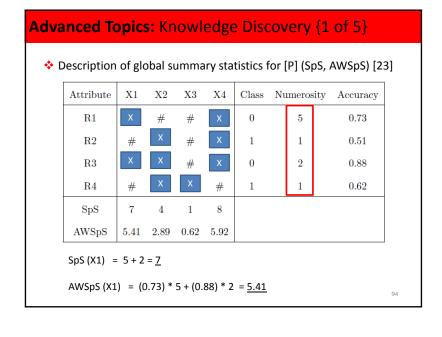
Advanced Topics: Complete vs. Best Action Mapping

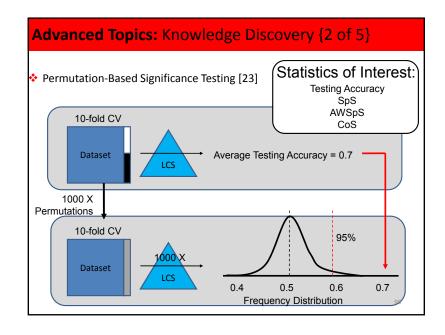
- Should LCS discover:
 - The most optimum action in a niche
 - The predicted payoff for all actions in a niche

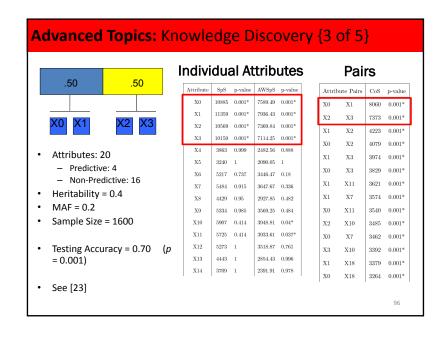
 $X \times A => P$ (cf Q-Learning)

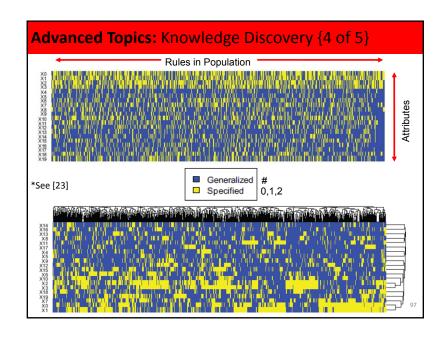
- The danger with optimum action only:
 - If a suboptimal rule is converged upon ... difficult to discover and switch policy (CF path habits)
- The problem with predicting all actions:
 - · Memory and time intensive
 - Identifies and keeps consistently incorrect action (100% accurate prediction) rules
 - · Harder to interpret rule base

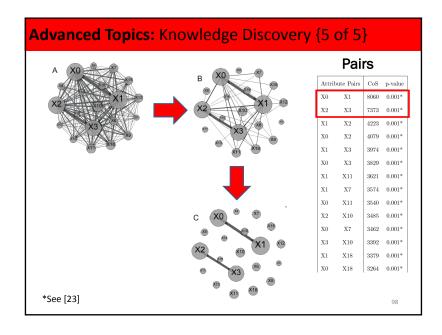
Advanced Topics: LCS Scalability What is scalability? Maintaining algorithm tractability as problem scale increases. ❖Problem scale increases can include... Higher pattern dimensionality Larger-scale datasets with Increased number of potentially predictive attributes. Increased number of training instances. Strategies for improving LCS scalability. ❖More efficient rule representations [18,28] (Pittsburgh and Michigan) Windowing [36] (Pittsburgh) Computational Parallelization (GPGPUs) [22] ❖Ensemble learning with available attributes partitioned into subsets [27] ◆Expert knowledge guided GA [25] ❖Rule Specificity Limit [28] 93

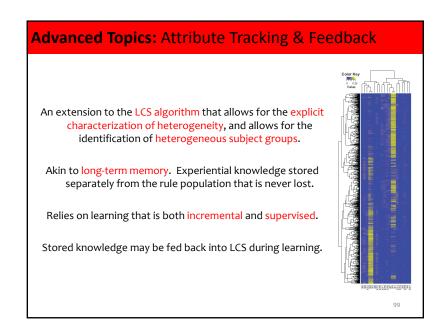


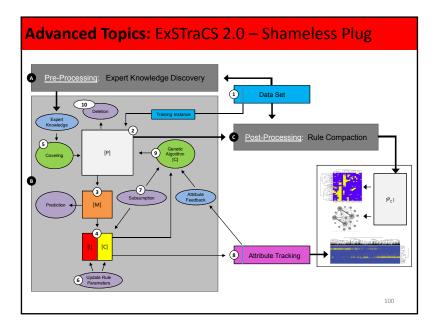




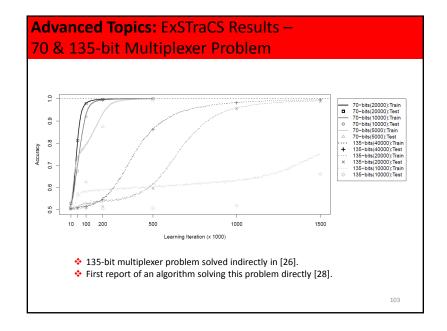


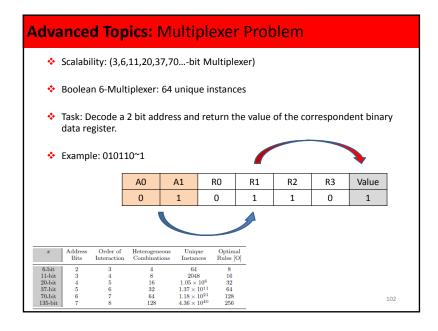


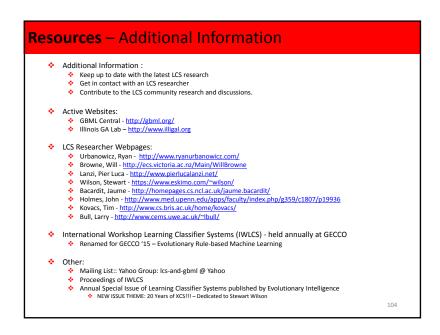




Advanced Topics: Rule Specificity Limit Previous: Data with many attributes yields absurdly over-fit ExSTraCS rules – not sufficient pressure to generalize. Allows for an impractically sized search space Relying on P_{spec} problematic. IDEA: Limit maximum rule dimensionality based on dataset characteristics (i.e. what we might have any hope of being powered to find). Calculate unique attribute state combinations $\psi = \epsilon^n$ Example: SNP dataset 16 • *\(\epsilon \)* = 3 8 16 32 64 128 • Training Instances = 2000 256 1024 • Find where : $\iota < \psi$ 4096 2187 16384 78125 65536 390625 101







Resources - Software

- Educational LCS (eLCS) in Python.
 - http://sourceforge.net/projects/educationallcs/
 - Simple Michigan-style LCS for learning how they work and how they are implemented.
 - * Code intended to be paired with first LCS introductory textbook by Brown/Urbanowicz.
- ExSTraCS 2.0 Extended Supervised Learning LCS in Python
 - http://sourceforge.net/projects/exstracs/
 - For prediction, classification, data mining, knowledge discovery in complex, noisy, epistatic, or heterogeneous problems.
- ❖ BioHEL Bioinformatics-oriented Hierarchical Evolutionary Learning in C++
 - http://ico2s.org/software/biohel.html
 - GAssist also available through this link.
- XCS & ACS (by Butz in C and Java) & XCSLib (XCS and XCSF) (by Lanzi in C++)
 - http://www.illigal.org
- XCSF with function approximation visualization in Java
 - http://medal.cs.umsl.edu/files/XCSFJava1.1.zip
- EpiXCS

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Conclusion

- What and Why
 - ❖Many branches of RBML, e.g. ARM, AIS, LCS
 - ❖ Powerful, human interpretable, learning algorithms
- Driving Mechanisms
 - Discovery
 - Learning
- ❖How?
 - LCS Algorithm Walk-Through
 - Flexible and robust methods developed
- Multiple styles
- ❖ Advanced methods: solutions to complex & real-world problems
- Many Resources Available

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Resources – LCS Review Papers & Books

- Select Review Papers:
 - Bull, Larry. "A brief history of learning classifier systems: from CS-1 to XCS and its variants." Evolutionary Intelligence (2015): 1-16.
 - Bacardit, Jaume, and Xavier Llorà. "Large-scale data mining using genetics-based machine learning." Wiley Interdisciplinary Reviews: Data Mining and Knowledge Discovery 3.1 (2013): 37-61.
 - Urbanowicz, Ryan J., and Jason H. Moore. "Learning classifier systems: a complete introduction, review, and roadmap." Journal of Artificial Evolution and Applications 2009 (2009): 1.
 - Sigaud, Olivier, and Stewart W. Wilson. "<u>Learning classifier systems: a survey</u>." Soft Computing 11.11 (2007): 1065-1078.
 - Holland, John H., et al. "What is a learning classifier system?." Learning Classifier Systems. Springer Berlin Heidelberg, 2000. 3-32.
 - Lanzi, Pier Luca, and Rick L. Riolo. "A roadmap to the last decade of learning classifier system research (from 1989 to 1999)." Learning Classifier Systems. Springer Berlin Heidelberg, 2000. 33-61.

Books

- NOTE: Brown & Urbanowicz are preparing an <u>Introductory LCS Textbook</u> hopefully available this year. (Springer)
- Drugowitsch, J., (2008) <u>Design and Analysis of Learning Classifier Systems: A Probabilistic Approach</u>. Springer-Verlag.
- Bull, L., Bernado-Mansilla, E., Holmes, J. (Eds.) (2008) Learning Classifier Systems in Data Mining. Springer
- Butz, M (2006) Rule-based evolutionary online learning systems: A principled approach to LCS analysis and design. Studies in Fuzziness and Soft Computing Series, Springer.
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