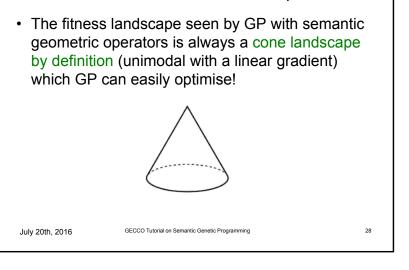


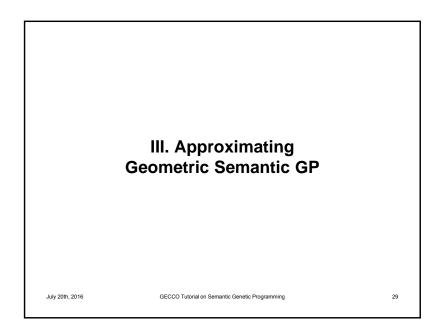
• Semantic geometric operators are geometric operators defined on the metric space of functions endowed with the semantic distance

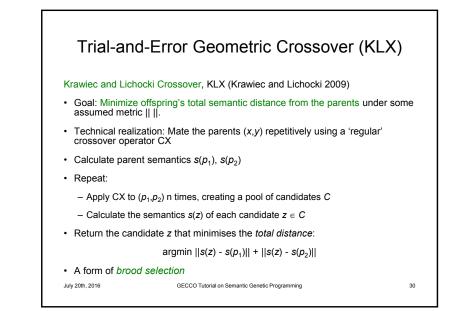
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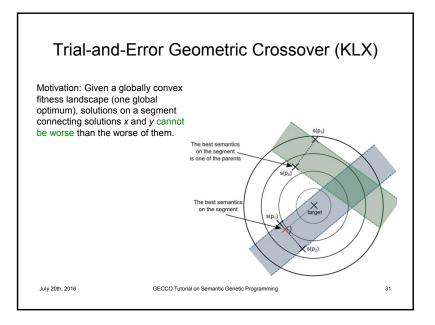
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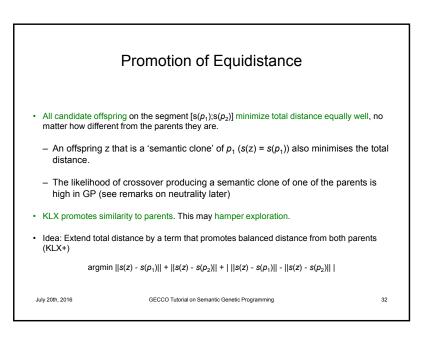


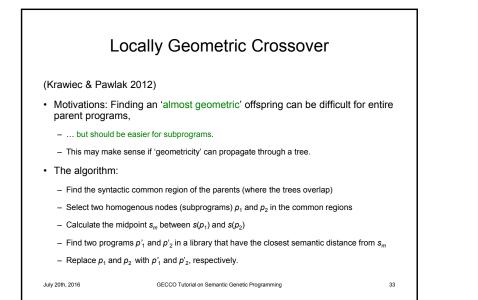
Semantic Fitness Landscape

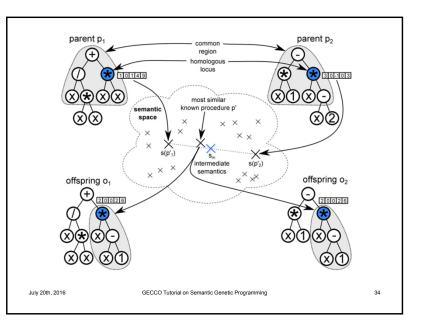


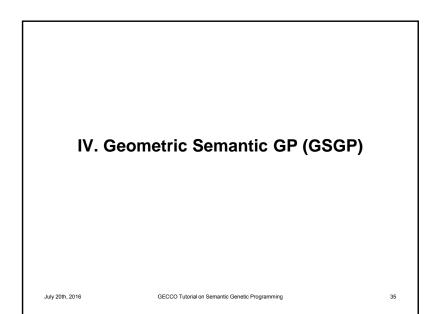












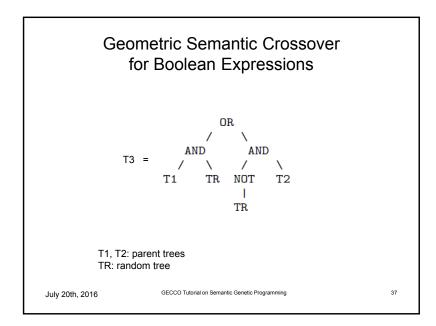
Geometric Semantic Operators Construction

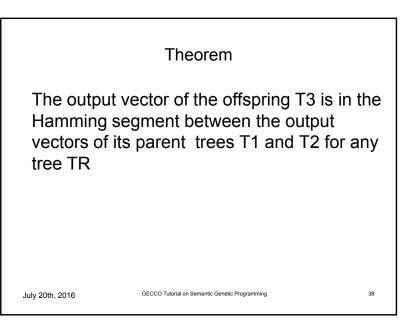
• By approximation:

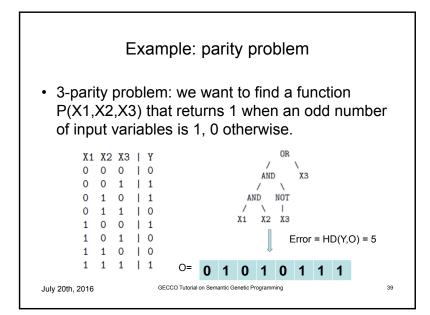
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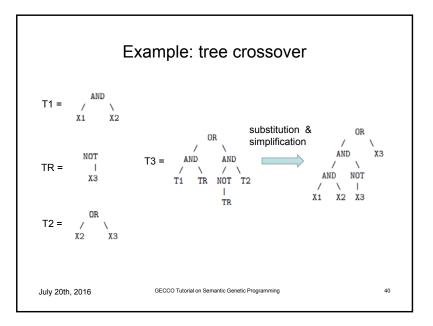
- Trial & Error is wasteful
- Offspring do not conform exactly to the semantic requirement
- By direct construction: Is it possible to find search operators that operate on syntax but that are guaranteed to respect geometric semantic criteria by direct construction?
- Due to the complexity of genotype-phenotype map in GP (Krawiec & Lichocki 2009) hypothesized that designing a crossover operator with such a guarantee is in general impossible. A pessimist? No, the established view until then...

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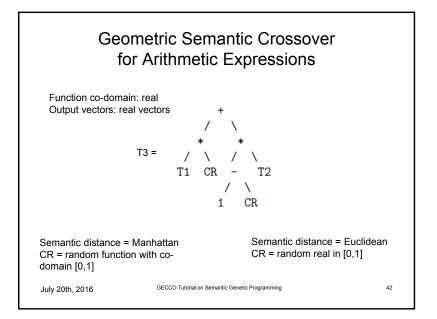


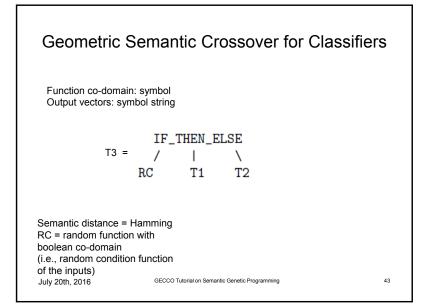


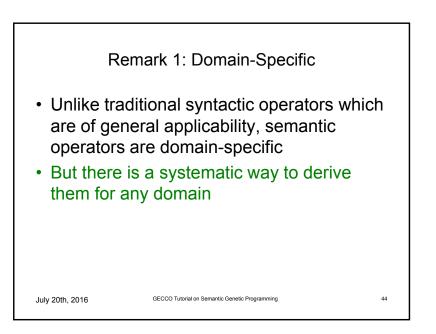




	Fxar	nn	le:	OI	uto	ม	tν	'e	cto	or	. CI	n	ssove	۶r	
		•	X2 X 0 0 1	3 0	Y 0		T1 0 0 0 0		T2 0 1 1		TR 1 0 1 0		T3 0 1 0		
		1 1	0 0 1	0	1 0	Ì	0 0	l I	0 1	I	1 0 1 0	I	0 1 1 1		
	 The output vector of TR acts as a crossover mask to recombine the output vectors of T1 and T2 to produce the output vector T3. 														
	 This is a geometric crossover on the semantic distance: output vector of T3 is in the Hamming segment between the output vectors of T1 and T2. 														
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Remark 2: Quick Growth

- Offspring grows in size very quickly, as the size of the offspring is larger than the sum of the sizes of its parents!
- To keep the size manageable we need to simplify the offspring without changing the computed function:
 - Boolean expressions: Boolean simplification
 - Math Formulas: algebraic simplification
- Programs: simplification by formal methods July 20th, 2016 GECCO Tutorial on Semantic Genetic Programming

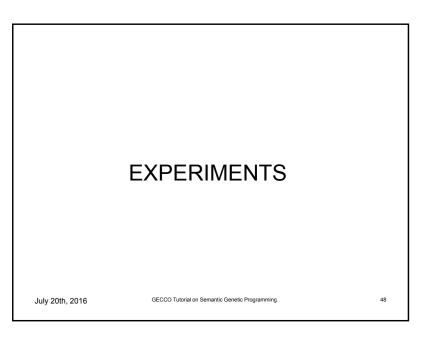
Remark 3: Syntax Does Not Matter! • The offspring is defined purely functionally, independently from how the parent functions and itself are actually represented (e.g., trees) • The genotype representation does not matter: solution can be represented using any genotype structure (trees, graphs, sequences)/language (Java, Lisp, Prolog) as long as the semantic operators can be described in that language

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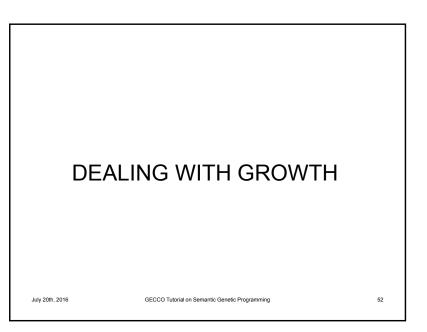
Semantic Mutations
It is possible to derive geometric semantic nutation operators.
They also have very simple forms for Boolean, Arithmetic and Program domains.

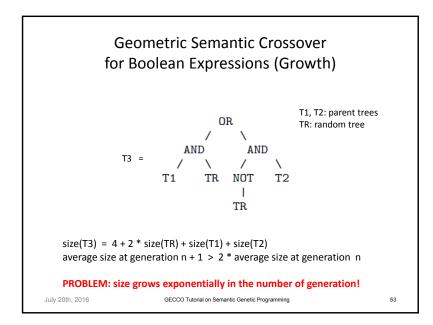


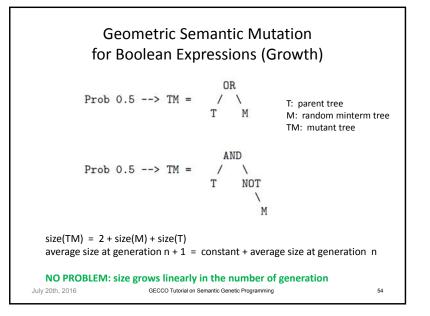
Boolean Problems									
Problem	Hits % Length								
	GP	GP GPt SSHC					-		
	avg sd	avg sd	avg so	avg s	i GP	GPt	SSHC	SGI	
Comparator6	80.2 3.8	90.9 3.5	99.8 0.5	99.5 0.	7 1.0	2.0	2.9	2.8	
Comparator8	80.3 2.8	94.9 2.4	100.0 0.0	99.9 0.	2 1.0	2.3	2.9	3.0	
Comparator10	82.3 4.3	95.3 0.9	100.0 0.0	100.0 0.	1 1.6	2.4	2.7	3.0	
Multiplexer6	70.8 3.3	94.7 5.8	99.8 0.5	99.5 0.	8 1.1	2.2	2.7	2.9	
Multiplexer11	76.4 7.9	88.8 3.4	100.0 0.0	99.90.	1 2.2	2.4	2.9	2.6	
Parity5	52.9 2.4	56.3 4.9	99.7 0.9	98.1 2.	1 1.4	1.7	2.9	2.9	
Parity6	50.5 0.7	55.4 5.1	99.7 0.6	98.8 1.	7 1.0	1.9	3.0	3.0	
Parity7	50.1 0.2	51.7 2.8	99.9 0.2	99.5 0.	6 1.0	1.7	3.0	3.1	
Parity8	50.1 0.2	50.6 0.9	100.0 0.0	99.7 0.	3 1.0	1.6	3.4	3.4	
Parity9	50.0 0.0	50.2 0.1	100.0 0.0	99.5 0.	3 1.0	1.3	3.8	3.8	
Parity10	50.0 0.0	50.0 0.0	100.0 0.0	99.4 0.	2 0.9	1.2	4.1	4.1	
Random5	82.2 6.6	90.9 6.0	99.5 1.2	98.8 2.	1 0.9	1.6	2.7	2.8	
Random6	83.6 6.6	93.0 4.1	99.9 0.4	99.2 1.	3 1.2	1.9	2.9	2.8	
Random7	85.1 5.3	92.9 3.8	99.9 0.2	99.8 0.	4 1.1	2.0	2.8	2.9	
Random8	89.6 5.3	93.7 2.4	100.0 0.1	99.9 0.	2 1.4	2.0	3.0	2.9	
Random9	93.1 3.7	95.4 2.3	100.0 0.1	100.0 0.	1 1.5	1.8	2.9	2.9	
Random10	95.3 2.3	96.2 2.0	100.0 0.0	100.0 0.	0 1.5	1.8	2.8	3.0	
Random11	96.6 1.6	97.3 1.5	100.0 0.0	100.0 0.	0 1.6	1.7	2.7	3.1	
True5	100.0 0.0	100.0 0.0	99.9 0.6	100.0 0.	0 1.1	1.3	2.0	2.4	
True6	100.0 0.0	100.0 0.0	99.8 0.6	100.0 0.	0 1.2	1.2	2.6	2.5	
True7		100.0 0.0					2.9	2.6	
True8	100.0 0.0	100.0 0.0	100.0 0.0	100.0 0.	1 1.2	1.4	3.3	2.9	

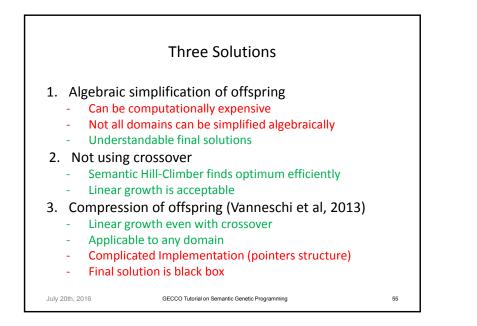
Polynomial Regression Problems											
Problem			\mathbf{Hits}	%							
	G	P	SSH	\mathbf{C}	SG	Р					
	avg	sd	avg	sd	avg	sd					
Polynomial3	79.9	23.1	100.0	0.0	99.5	1.5					
Polynomial4	60.5	27.6	99.9	0.9	99.9	0.9					
Polynomial5	40.7	21.6	100.0	0.0	99.5	2.0					
Polynomial6	37.5	23.4	100.0	0.0	98.9	3.1					
Polynomial7	30.7	18.5	100.0	0.0	99.9	0.9					
Polynomial8	34.7	16.0	99.5	2.0	99.7	1.3					
Polynomial9	20.7	13.2	100.0	0.0	98.5	4.9					
Polynomial10	25.7	16.7	99.4	1.7	99.9	0.9					
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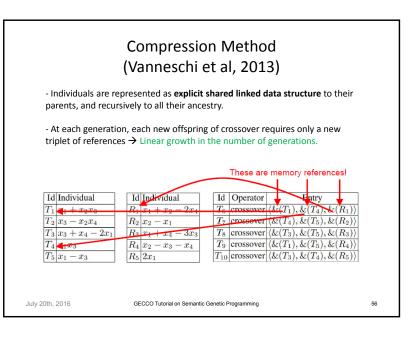
Classification Problems																
Problem Hits % Length																
			G	P	G	GPt SSHC				SGP						
n_v	n_c	n_{cl}	avg	sd	avg		avg	sd	avg	sd	GP	GPt	SSHC	SGF		
3	3	2	80.00	8.41	97.30	4.78	99.74	0.93	99.89	0.67	1.6	1.9	2.3	2.3		
3	3	4	49.15	9.96	78.89	8.93	99.89	0.67	99.00	1.63	1.6	2.1	2.3	2.3		
3	3	8	37.04	5.07	59.52	14.26	99.74	0.93	96.04	2.85	1.2	1.9	2.3	2.3		
3	4	2	67.92	7.05	93.80	-5.41	99.95	0.28	99.58	0.80	1.8	2.3	2.7	2.7		
3	4	4	39.11	7.02	68.48	8.66	99.84	0.47	98.08	1.64	1.7	2.3	2.7	2.7		
3	4	8	28.02	3.73	46.98	14.48	99.73	0.58	94.22	1.72	1.1	2.0	2.7	2.7		
4	3	2	88.31	6.98	98.89	2.89	99.96	0.22	100.00	0.00	1.6	1.9	2.9	2.9		
4	3	4	48.85	6.54	88.15	10.10	100.00	0.00	99.54	0.68	1.4	2.2	2.9	2.9		
4	3	8	36.54	9.01	60.37	17.14	100.00	0.00	96.63	1.23	1.0	1.9	2.9	2.9		
4	4	2	82.75	8.21	99.79	1.12	100.00	0.00	99.86	0.23	2.2	2.3	3.3	3.3		
4	4	4	44.13	8.75	77.55	6.30	100.00	0.00	99.68	0.29	2.0	2.4	3.3	3.3		
4	4	8	30.63	5.33	50.21	15.08	99.96	0.12	98.84	0.58	1.4	2.1	3.3	3.3		

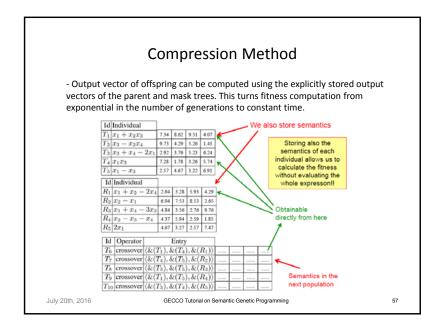


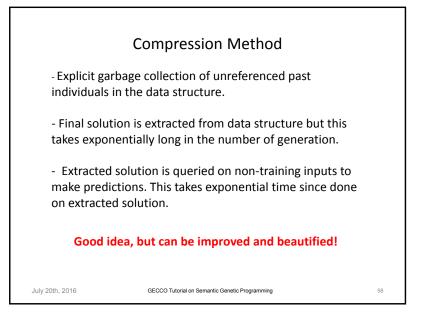


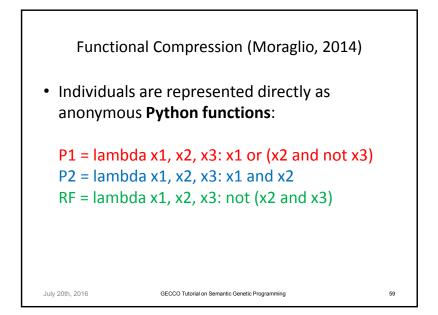


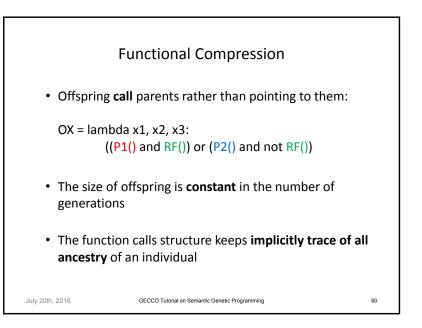












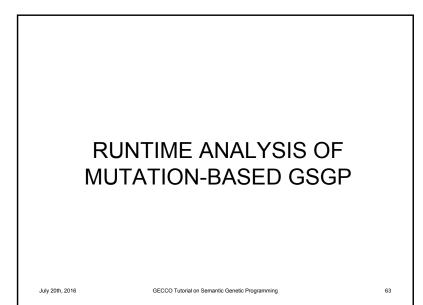
Functional Compression

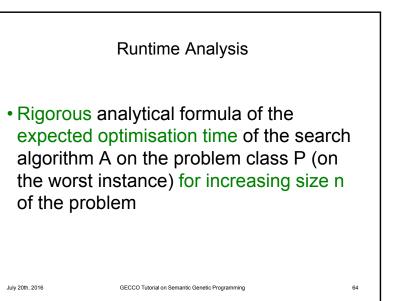
- All individuals are **momoized functions**: fitness of the offspring can be computed directly from stored output vectors of parents.
- **Garbage collection** of unreferenced past functions done automatically by the Python compiler.
- Final solution is a Python compiled function. The extracted solution is exponentially long.
- **But** the compiled final solution can be queried on nontraining inputs to make predictions in **linear time**.

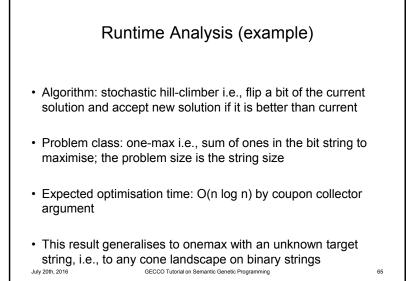
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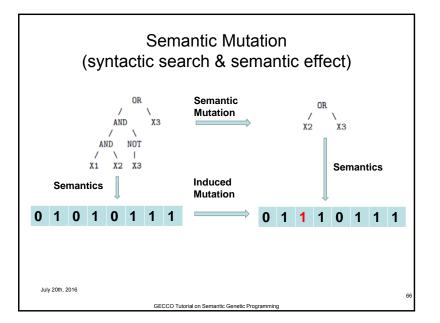
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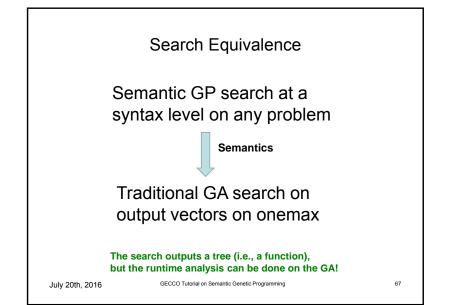
GSGP Implementations Original Mathematica implementation with algebraic simplification: https://github.com/amoraglio/GSGP Compression method (>2000 lines in C++): http://gsgp.sourceforge.net/ Functional compression (<100 lines in Python): http://gsgp.sourceforge.net/ Scala implementation using the ScaPS library: http://www.cs.put.poznan.pl/kkrawiec/wiki/?n=Site.Scaps

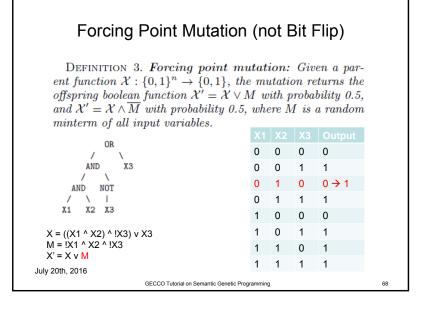


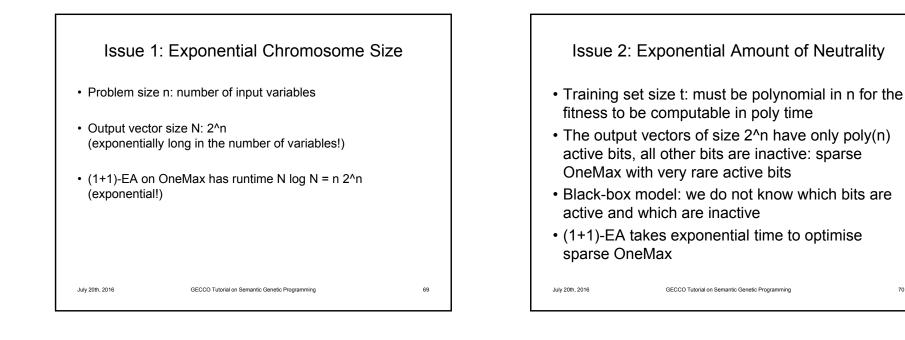


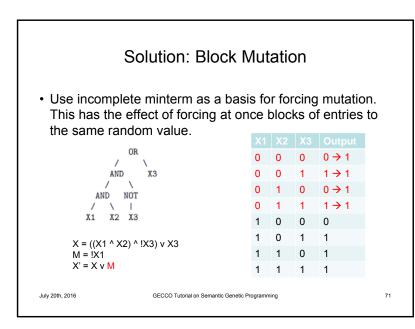


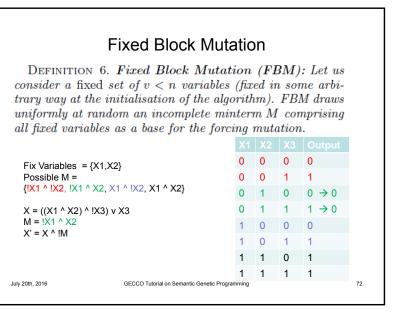












Polynomial Runtime with High Probability of Success on All Boolean Problems!

THEOREM 4. Let us assume that the size of the training set τ is a polynomial n^c in the number of input variables n, with c a positive constant. Let us choose the number of fixed variables v logarithmic in n such that $v > 2c \log_2(n)$. Then, semantic GP with FBM finds a function satisfying the training set in polynomial time with high probability of success, on any problem P, and training set T uniformly sampled from P.

Proof idea: choose v such that the number of partitions of the output vector is polynomial in n (so that the runtime is polynomial), and larger enough than the training set, so that each training example is in a single block w.h.p. (which guarantees that the optimum can be reached).

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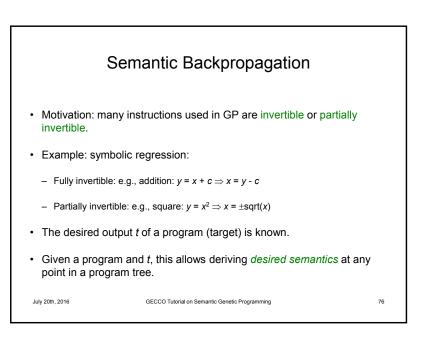
Lesson from Theory

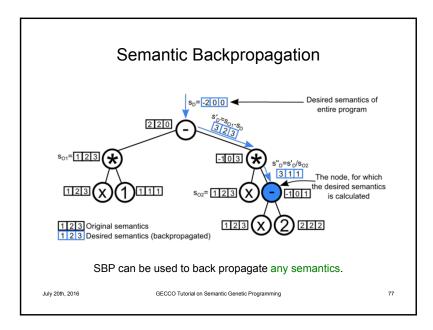
- Rigorous runtime analysis of GSGP on general classes of non-toy problems is possible as the landscape is always a cone
- There are issues with GSGP which require careful design of semantic mutations to obtain efficient search. Theory can guide the design of provably good semantic operators in terms of runtime
- Runtime analysis of GSGP with several other mutation operators for Boolean, arithmetic and classification domains have been done producing refined provably good semantic search operators

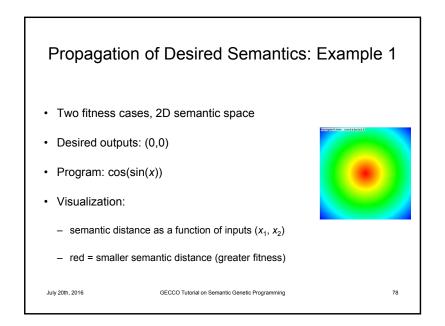
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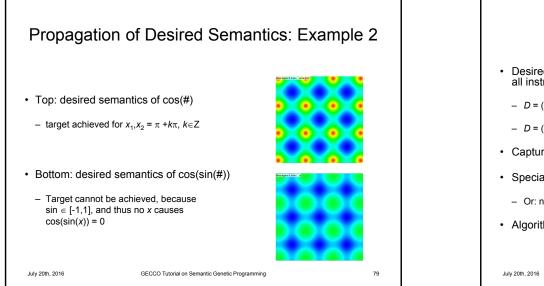
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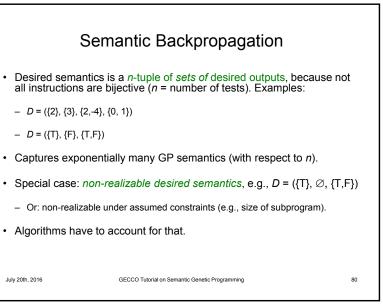


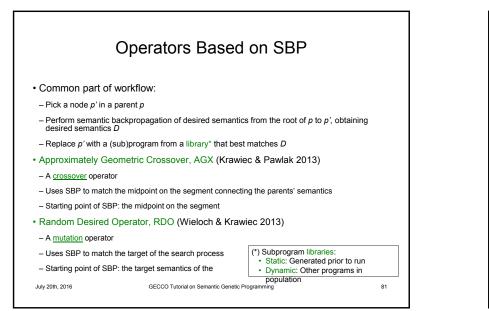


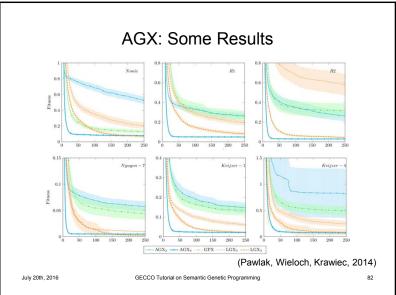












t3 t4

0 0

84

1 0 1

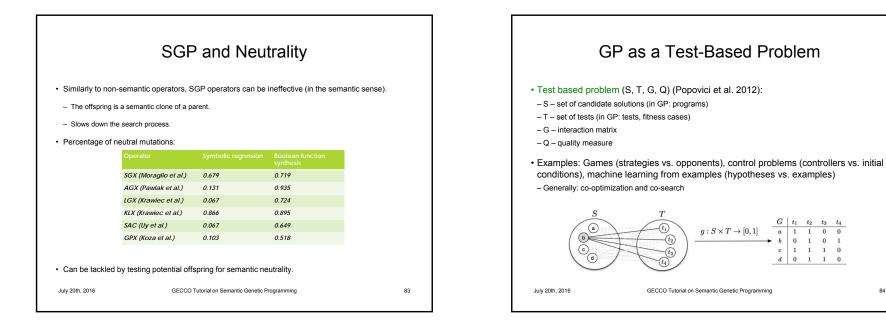
0 1 1 0

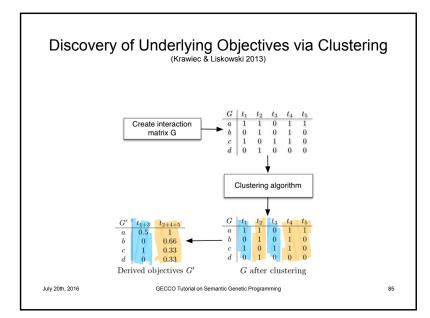
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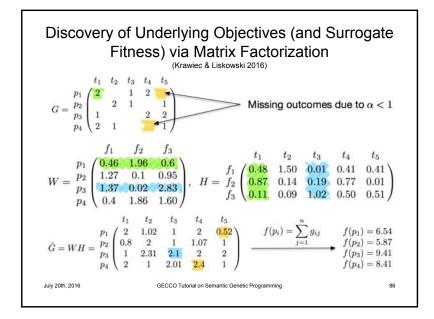
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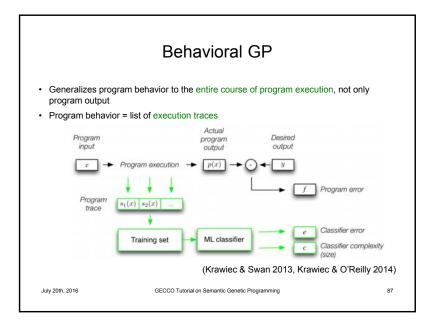
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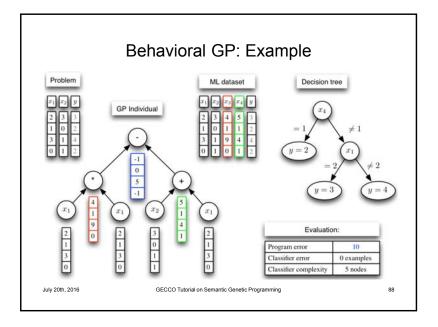
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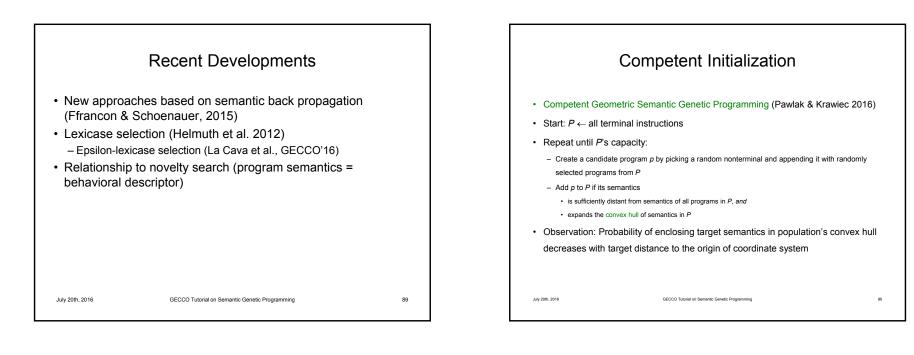


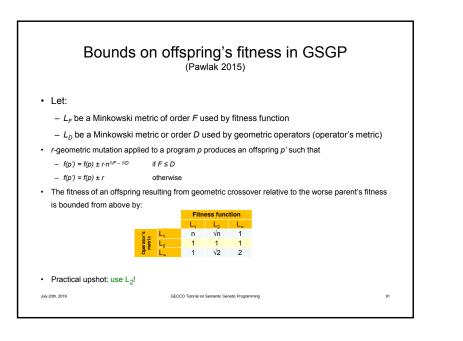


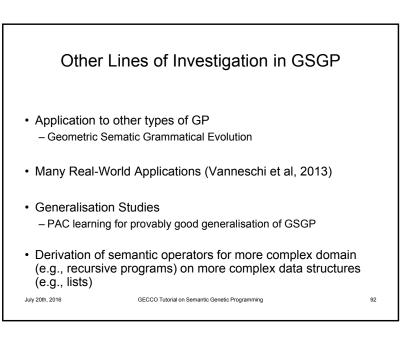












		References
Thank you!		 A. Moraglio, K. Krawiec, C. Johnson, Geometric Semantic Genetic Programming, PPSN XII, 2012. K. Krawiec, P. Lichocki, Approximating Geometric Crossover in Semantic Space, GECCO 2009. K. Krawiec, T. Pavida, Locally Geometric Semantic Crossover in Semantic Space, GECCO 2009. K. Krawiec, T. Pavida, E. Wieloch, K. Krawiec, Semantic Backpropagation for Designing Genetic Operators in Genetic Programming, IEEE Transactions on Evolutionary Computation, 2014. L. Beadle, C. Johnson, Semantically Driven Mutation in Genetic Programming, CEC 2008, L. Beadle, C. Johnson, Semantically Driven Mutation in Genetic Programming, CEC 2008, N.Q. Uy, N.X. Hoal, M. O'Nell, R. I. McKay, E. Galvan-Lopez, Semantical-based crossover in genetic programming: application to real-valued symbolic regression, Genetic Programming and Evolvable Machines, 2011, N.Q., Uy, Tofaol, M. O'Nell, R. J. McKay, D.N. Phong, D. Ne heroles of semantic locality in genetic programming, Information
Questions?		N.Q. Uv, N.X. Hoai, Michael O'Neill, Semantics based mutation in genetic programming: The case for real-valued symbolic regression, MeNDEL 2009, L Beadle, C. Johnson, Semantic analysis of program initialisation in genetic programming, Genetic Programming and Evolvable Machines, 2009, D. Jackson, Promoting Phenotypic Diversity in Genetic Programming, PPSN XI, 2010. Semantic selection:
		 E. Galvan-Lopez, B. Cody-Kenny, L. Trujillo, A. Kattan, Using Semantics in the Selection Mechanism in Genetic Programming: a Simple Hethod for Promoting Semantic Diversity, CEC 2013. R.E. Smith, S. Forrest, and A.S. Perelson. "Searching for diverse, coop- erative populations with genetic algorithms". In: Evolutionary Computation 12 (1993). Lasarczyk, C. W. G. & and Wolfgang Banzhaf, P. D. Dynamic Subset Selection Based on a Fitness Case Topology Evolutionary Computation, 2004, 12 (223-42). Nguyen Quang Uy, Nguyen Xuan Hoai, Michael O'Neill, R.I. McKay, and Dao Ngoc Phong. On the roles of semantic locality of crossover in genetic programming. Information Sciences, 235:195–213, 20 June 2013. Mauro Castelli, Leonardo Vanneschi, and Sara Silva. Semantic search-based genetic programming and the effect of intron deletion. IEEE Transactions on Cybernetics, 44(1):103–113, January 2014. Langdon, W. B. & Poli, R. Foundations of Genetic Programming Pervertag. 2002 McPhee, N.F., Drudations O, T., Semantic Building Biocks in Genetic Programming, Springer. 2008, 4971, 134-145
Credits: The authors thank Bartosz Wieloch and Tomasz F feedback on the slides of the tutorial. Other credits: \		 Langdon, W. B. & Poli, R. Foundations of Genetic Programming Springer-Verlag, 2002 McPhee, N. F. Ots, B. & Huchsion, T., Semantic Building Blocks in Genetic Programming, in O'Neill, M et al. (eds.) Proceedings of the 11th European Conference on Genetic Programming, EuroGP 2008, Springer, 2008, 4971, 134-145
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