

# A Practical Guide to Experimentation (and Benchmarking)

Nikolaus Hansen  
Inria  
Research Centre Saclay, CMAP, Ecole polytechnique

Permission to make digital or hard copies of part or all of this work for personal or classroom use is granted without fee provided that copies are not made or distributed for profit or commercial advantage and that copies bear this notice and the full citation on the first page. Copyrights for third-party components of this work must be honored. For all other uses, contact the Owner/Author.

GECCO '19 Companion, July 13–17, 2019, Prague, Czech Republic  
© 2019 Copyright is held by the owner/author(s).  
ACM ISBN 978-1-4503-6748-6/19/07.  
<https://doi.org/10.1145/3319619.3323397>

## Overview

- Scientific experimentation
- Invariance
- Statistical Analysis
- A practical experimentation session
- Approaching an unknown problem
- Performance Assessment
  - What to measure
  - How to display
  - Aggregation
  - Empirical distributions

Do not hesitate to ask questions!

## Why Experimentation?

- The behaviour of many if not most **interesting algorithms** is
  - not **amenable** to a (full) theoretical analysis even when applied to simple problems  
calling for an alternative to theory for investigation
  - not fully **comprehensible** or even predictable without (extensive) empirical examinations  
even on simple problems  
comprehension is the main driving force for scientific progress  
*If it disagrees with experiment, it's wrong. And that simple statement is the key to science.* — R. Feynman
- Virtually all algorithms have **parameters**  
like most (physical/biological/...) models in science  
we rarely have explicit knowledge about the “right” choice  
this is a *big* obstacle in designing and benchmarking algorithms
- We are interested in solving *black-box* optimisation problems  
which may be “arbitrarily” complex and (by definition) not well-understood

## Scientific Experimentation (dos and don'ts)

- What is the aim? *Answer a question*, ideally quickly and comprehensively  
consider in advance what the question is and in which way the experiment can answer the question

What are the dos and don'ts?

- what is most helpful to do?
- what is better to avoid?

## Scientific Experimentation (dos and don'ts)

- What is the aim? *Answer a question*, ideally quickly (minutes, seconds) and comprehensively  
consider in advance what the question is and in which way the experiment can answer the question
- do not (blindly) trust in what one needs to rely upon (code, claims, ...) without *good* reasons  
check/test "everything" yourself, practice stress testing (e.g. weird parameter setting) which also boosts understanding one key element for success  
interpreted/scripted languages have an advantage  
*Why Most Published Research Findings Are False* [Ioannidis 2005]
- practice to **make predictions** of the (possible/expected) outcome(s)  
to develop a mental model of the object of interest  
to practice being proven wrong, to overcome *confirmation bias*
- run *rather many than few experiments iteratively*, practice *online experimentation* (see demonstration)  
to run many experiments they must be *quick to implement and run*, ideally *seconds* rather than *minutes* (start with small dimension/budget)  
*develops a feeling for the effect of setup changes*

## Scientific Experimentation (dos and don'ts)

- run *rather many than few experiments iteratively*, practice *online experimentation* (see demonstration)  
to run many experiments they must be *quick to implement and run*, ideally *seconds* rather than *minutes* (start with small dimension/budget)  
*develops a feeling for the effect of setup changes*
- run any experiment at least **twice**  
assuming that the outcome is stochastic  
get an **estimator of variation/dispersion/variance**
- **display**: *the more* the better, *the better* the better  
figures are *intuition pumps* (not only for presentation or publication)  
it is hardly possible to overestimate the value of a good figure  
data is the only way experimentation can help to answer questions, therefore **look at them, study them carefully!**
- **don't** make **minimising CPU-time** a primary objective  
avoid spending time in implementation details to tweak performance  
prioritize code clarity (minimize time to *change* code, to debug code, to maintain code)  
yet code optimization may be necessary to run experiments efficiently

## Scientific Experimentation (dos and don'ts)

- **don't** make **minimising CPU-time** a primary objective  
avoid spending time in implementation details to tweak performance  
yet code optimization may be necessary to run experiments efficiently
- *Testing Heuristics: We Have it All Wrong* [Hooker 1995]  
*"The emphasis on competition is fundamentally anti-intellectual and does not build the sort of insight that in the long run is conducive to more effective algorithms"*
- It is usually (much) more important to **understand why** algorithm A performs badly on function  $f$ , than to make algorithm A faster for unknown, unclear or trivial reasons  
mainly because an algorithm is applied to *unknown* functions, not to  $f$ , and the "why" allows to predict the effect of design changes
- there are many **devils in the details**, results or their interpretation may crucially depend on simple or intricate bugs or subtleties  
yet another reason to run many (slightly) different experiments  
check limit settings to give consistent results

## Scientific Experimentation (dos and don'ts)

- there are many **devils in the details**, results or their interpretation may crucially depend on simple or intricate bugs or subtleties  
yet another reason to run many (slightly) different experiments  
check limit settings to give consistent results
- **Invariance** is a very powerful, almost indispensable tool

## Invariance: binary variables

Assigning 0/1 (for example minimize  $\sum_i x_i$  vs  $\sum_i 1 - x_i$ )

- is an “arbitrary” and “trivial” encoding choice and
- amounts to the affine linear transformation  $x_i \mapsto -x_i + 1$   
this transformation or the identity are the **coding choice in each variable**  
in continuous domain: norm-preserving (isotropic, “rigid”) transformation
- does not change the function “structure”
  - all level sets  $\{x \mid f(x) = \text{const}\}$  have the same size (number of elements, same volume)
  - the same neighbourhood
  - no variable dependencies are introduced (or removed)

Instead of 1 function, we now consider  **$2^{**n}$  different but equivalent functions**  
 $2^{**n}$  is non-trivial, it is the size of the search space itself

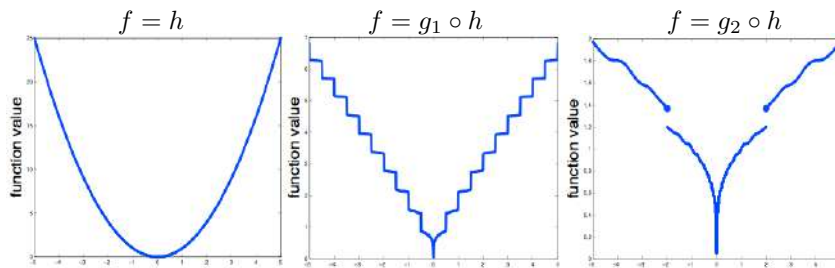
## Invariance: binary variables

Permutation of variables

- is another “arbitrary” and “trivial” encoding choice and
- is another norm-preserving transformation
- does not change the function “structure” (as above)
- may affect the neighbourhood depending on the operators (recombination, mutation)

Instead of 1 function, we now consider  **$n!$  different but equivalent functions**  
 $n! \gg 2^n$  is much larger than the size of the search space

## Invariance Under Order Preserving Transformations



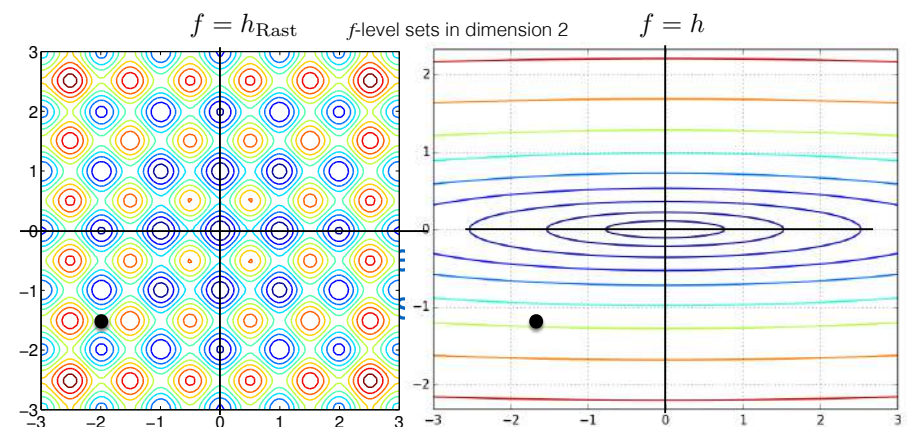
Three functions belonging to the same equivalence class

A **function-value free search algorithm** is invariant under the transformation with any **order preserving** (strictly increasing)  $g$ .

Invariances make

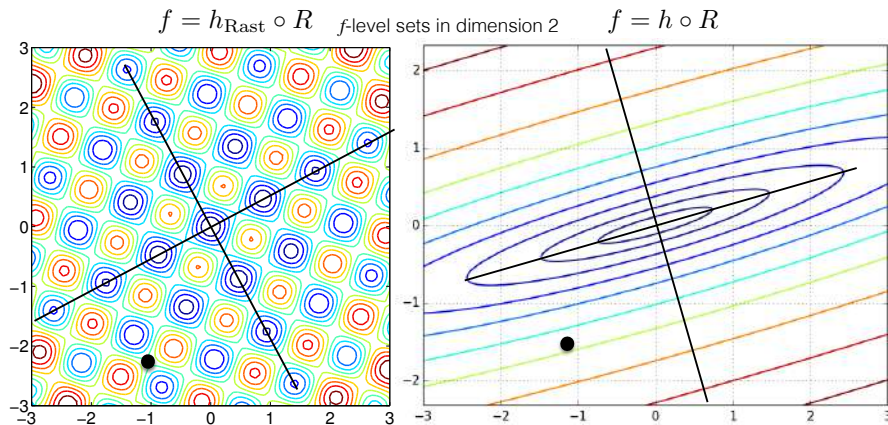
- observations meaningful **as a rigorous notion of generalization**
- algorithms predictable and/or “robust”

## Invariance Under Rigid Search Space Transformations



for example, invariance under search space rotation  
(**separable** vs non-separable)

## Invariance Under Rigid Search Space Transformations



for example, invariance under search space rotation  
(separable vs **non-separable**)

## Invariance

*The grand aim of all science is to cover the greatest number of empirical facts by logical deduction from the smallest number of hypotheses or axioms.*

— Albert Einstein

- Empirical performance results

- ▶ from benchmark functions
- ▶ from solved real world problems

are only useful if they do **generalize** to other problems

- **Invariance** is a strong **non-empirical** statement about generalization  
generalizing (identical) performance from a single function to a whole class of functions

Consequently, invariance is of greatest importance for the **assessment of search algorithms**.

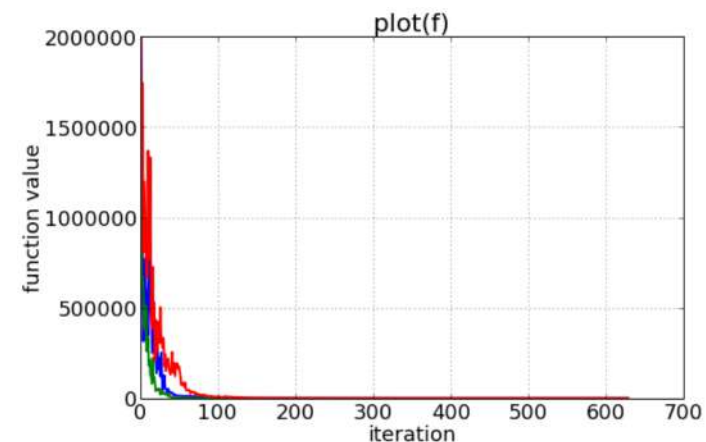
## Measuring Performance

Empirically

**convergence graphs** is all we have to start with

**the right presentation** is important!

## Displaying Three Runs

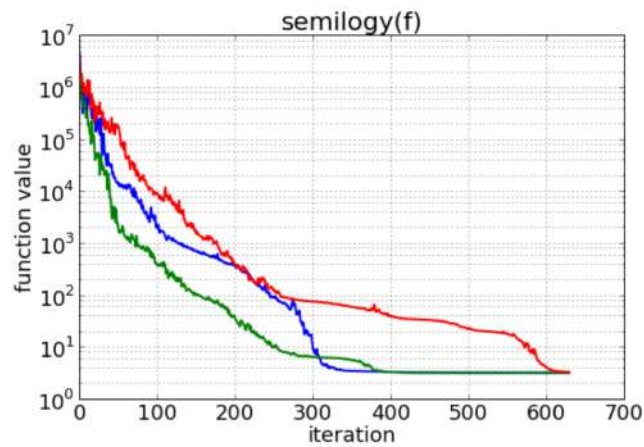


not like this (it's unfortunately not an uncommon picture)

why not, what's wrong with it?

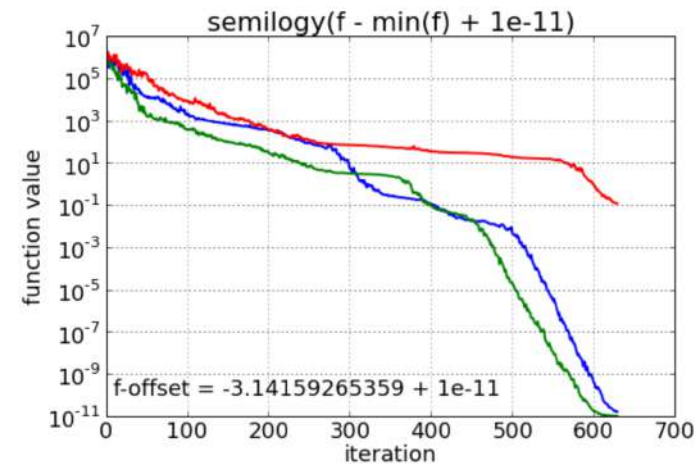


## Displaying Three Runs



better like this (shown are the same data),  
caveat: fails with negative f-values

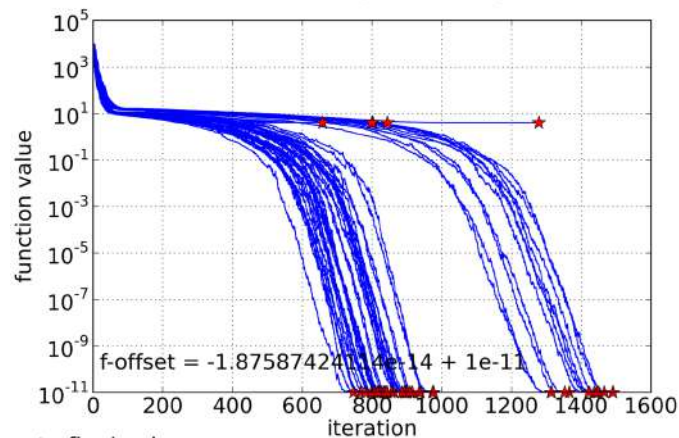
## Displaying Three Runs



even better like this: subtract minimum value over all runs

## Displaying 51 Runs

don't hesitate to display all data (the appendix is your friend)



★: final value

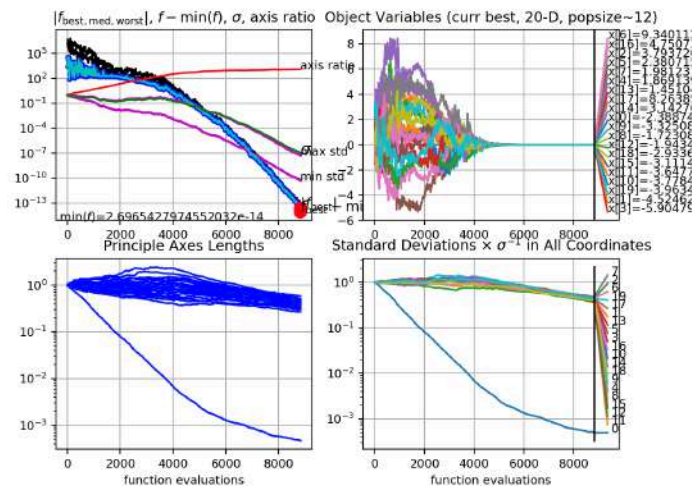
observation: three different "modes", which would be difficult to represent or recover in single statistics

4.04686177e-08 4.38294341e-08 4.65665203e-08 5.01580767e-08 ...]

There is more to display than convergence graphs

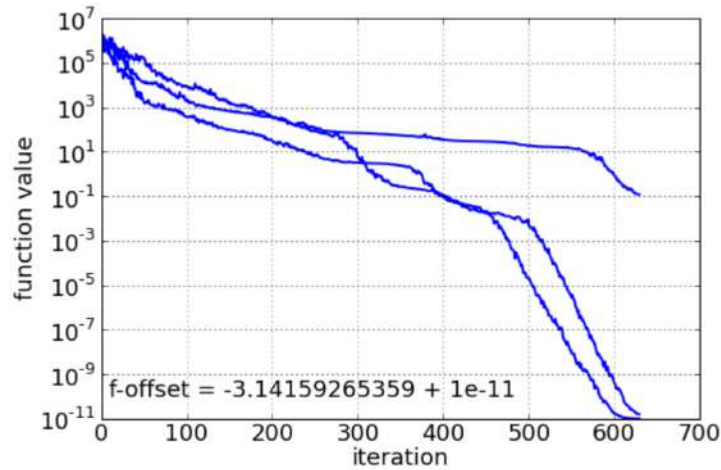
cma.plot()

Figure 328

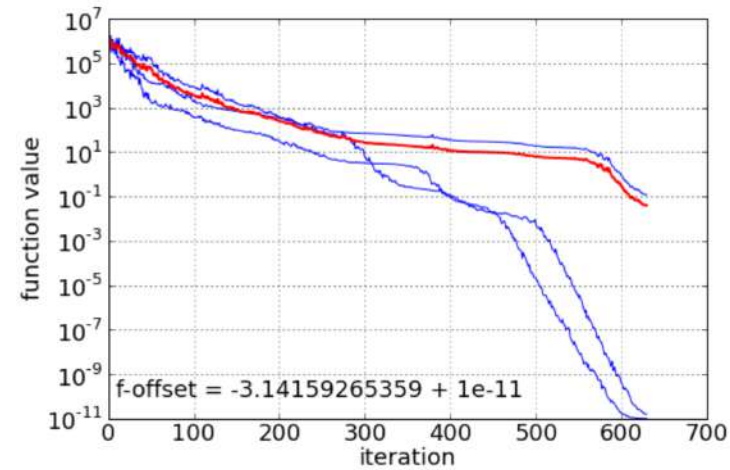


Navigation icons: back, forward, search, etc.

## Aggregation: Which Statistics?



## Aggregation: Which Statistics?



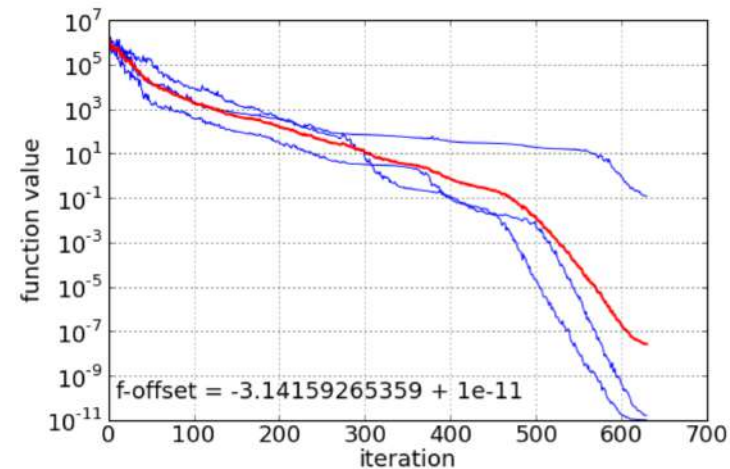
mean/average function value

- tends to emphasize large values

## More Caveats on Averages/Expectations

- to **reliably estimate an expectation** (from the *average*) we need to make **assumptions on the tail** of the underlying distribution
  - these can not be implied from the observed data
  - AKA: the average is well-known to be (highly) **sensitive to outliers** (extreme events)
- **rare events** can only be analyzed by collecting a *large enough number* of data

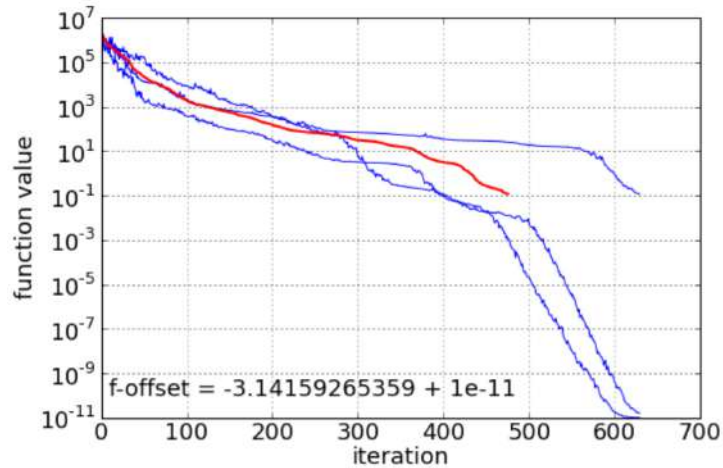
## Aggregation: Which Statistics?



geometric average function value  $\exp(\text{mean}_i(\log(f_i)))$

- reflects "visual" average
- depends on offset

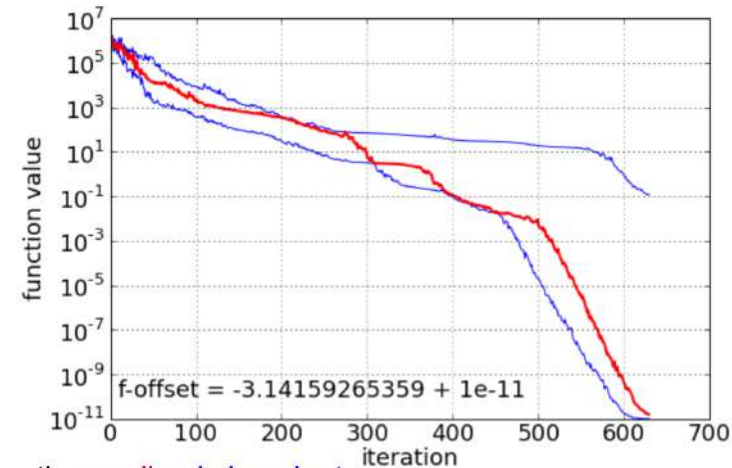
## Aggregation: Which Statistics?



### average iterations

- reflects "visual" average
- here: incomplete

## Aggregation: Which Statistics?



the **median** is **invariant**

- unique for uneven number of data
- independent of log-scale, offset...

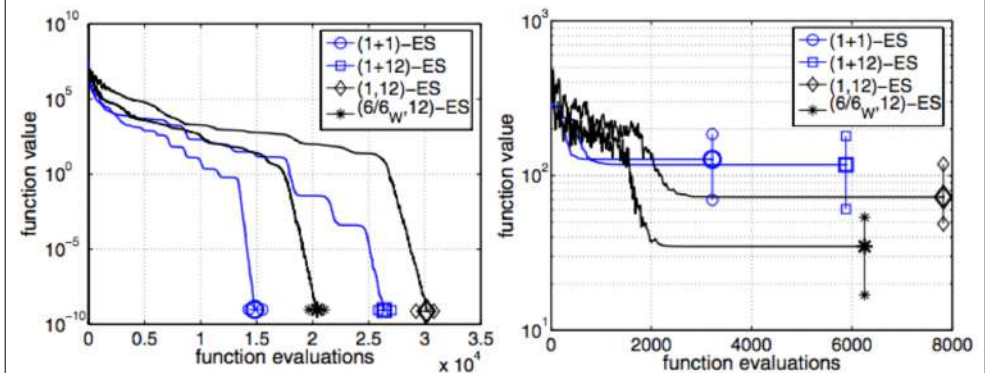
$$\text{median}(\log(\text{data})) = \log(\text{median}(\text{data}))$$

- same when taken over x- or y-direction

## Implications

- use the **median** as summary datum  
unless there are good reasons for a different statistics  
out of practicality: use an odd number of repetitions
- more general: use quantiles as summary data  
for example out of 15 data: 2nd, 8th, and 14th  
value represent the 10%, 50%, and 90%-tile

## Two More Examples



Comparison of 4 algorithms using the "median run" and the 90% central range of the final value on two different functions (Ellipsoid and Rastrigin)

caveat: this range display with simple error bars fails, if, e.g., 30% of all runs "converge"



## Statistical Analysis

“The first principle is that *you must not fool yourself*, and you are the easiest person to fool. So you have to be very careful about that. After you've not fooled yourself, it's easy not to fool other[ scientist]s. You just have to be honest in a conventional way after that. ”

— Richard P. Feynman

## Statistical Analysis

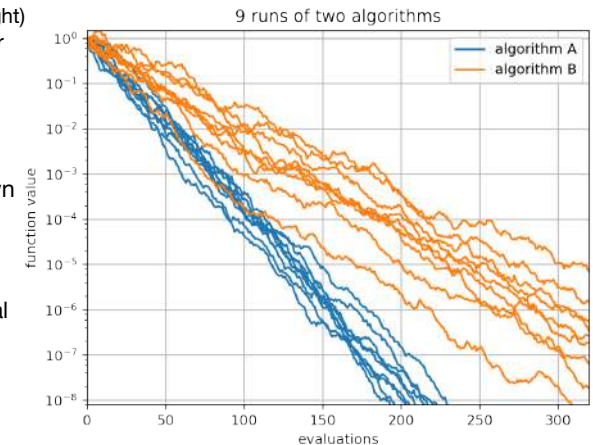
“experimental results lacking proper statistical analysis must be considered anecdotal at best, or even wholly inaccurate”

— M. Wineberg

Do you agree (sounds about right) or disagree (is taken a little over the top) with the quote?

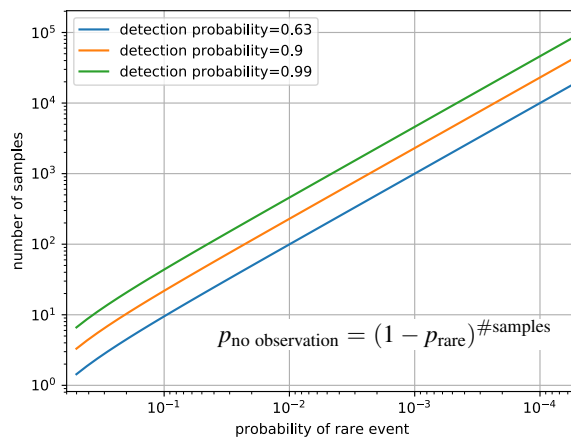
an experimental result (shown are *all data obtained*):

Do we (even) need a statistical analysis?



## Rare Events

- The obvious: if we consider rare events to be important, we have to sample many data



## Statistical Significance: General Procedure

- first, check the *relevance* of the result, for example of the difference which is to be tested for statistical significance  
this also means: do not *explorative testing* (e.g. test *all* pairwise combinations)  
any ever so small difference can be made *statistically* significant with a simple trick,  
but *not made* significant in the sense of *important* or *meaningful*
- prefer “nonparametric” methods  
*not* assuming that the data come from a *parametrised* family of probability distributions
- p-value** = significance level = probability of a false positive outcome, given  $H_0$  is true  
smaller p-values are better  
<0.1% or <1% or <5% is usually considered as *statistically significant*
- given a found/observed p-value, *fewer data are better*  
more data (almost inevitably) lead to smaller p-values, hence to achieve the same p-value with fewer data, the *between*-difference must be larger compared to the *within*-variation





## Statistical Significance: General Procedure

- first, check the *relevance* of the result, for example of the difference which is to be tested for statistical significance  
this also means: do not *explorative testing* (e.g. test *all* pairwise combinations) any ever so small difference can be made *statistically* significant with a simple trick, but *not made* significant in the sense of *important* or *meaningful*
- prefer “nonparametric” methods  
not assuming that the data come from a *parametrised* family of probability distributions
- **p-value** = significance level = probability of a false positive outcome, given  $H_0$  is true  
smaller p-values are better  
<0.1% or <1% or <5% is usually considered as *statistically significant*
- given a found/observed p-value, *fewer data are better*  
more data (almost inevitably) lead to smaller p-values, hence to achieve the same p-value with fewer data, the *between*-difference must be larger compared to the *within*-variation

## Statistical Significance: General Procedure

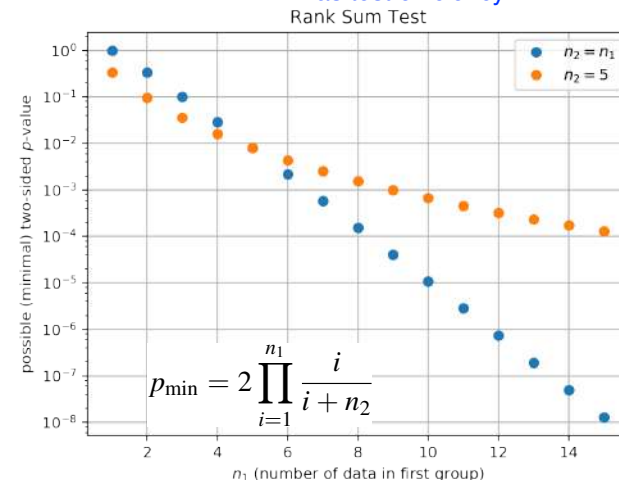
- first, check the *relevance* of the result, for example of the difference which is to be tested for statistical significance  
this also means: do not *explorative testing* (e.g. test *all* pairwise combinations) any ever so small difference can be made *statistically* significant with a simple trick, but *not made* significant in the sense of *important* or *meaningful*
- prefer “nonparametric” methods  
not assuming that the data come from a *parametrised* family of probability distributions
- **p-value** = significance level = probability of a false positive outcome, given  $H_0$  is true  
smaller p-values are better  
<0.1% or <1% or <5% is usually considered as *statistically significant*
- given a found/observed p-value, *fewer data are better*  
more data (almost inevitably) lead to smaller p-values, hence to achieve the same p-value with fewer data, the *between*-difference must be larger compared to the *within*-variation

## Statistical Significance: Methods

- use the **rank-sum** test (aka Wilcoxon or Mann-Whitney U test)
  - **Assumption:** all observations (data values) are obtained independently and no equal values are observed  
The “*lack*” of *necessary preconditions* is the main reason to use the rank-sum test. even a few equal values are not detrimental the rank-sum test is *nearly as efficient* as the t-test which requires normal distributions
  - **Null hypothesis** (nothing relevant is observed if):  $\Pr(x < y) = \Pr(y < x)$   
 $H_0$ : the probability to be greater or smaller (better or worse) is the same the aim is to be able to reject the null hypothesis
- Procedure: compute the sum of ranks in the ranking of all (combined) data values
- **Outcome:** a **p-value**  
the probability that the observed or a *more extreme* data set was generated under the null hypothesis; the probability to *mistakenly* reject the null hypothesis

## Statistical Significance: How many data do we need?

AKA as test efficiency

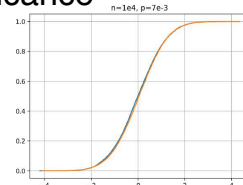


- assumption: data are fully “separated”, that is,  $\forall i, j : x_i < y_j$  or  $\forall i, j : x_i > y_j$  (two-sided)
- observation: adding 2 data points in each group gives about one additional order of magnitude
- use the **Bonferroni correction** for multiple tests

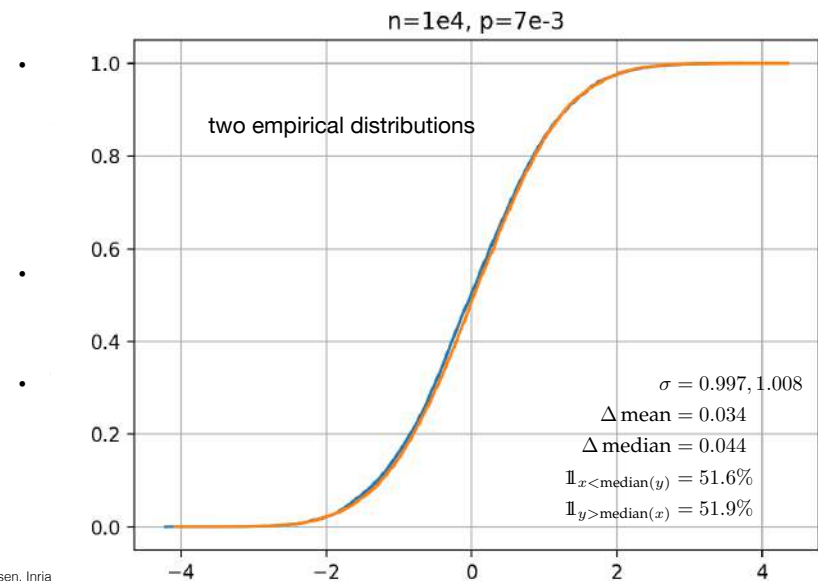
simple and conservative: multiply the computed p-value by the number of tests  
A practical guide to experimentation

## Statistical Significance: How many data do we need?

- In the best case: **at least ten** (two times five) and *two times nine is plenty*  
minimum number of data to possibly get two-sided  
 $p < 1\%$ : 5+5 or 4+6 or 3+9 or 2+19 or 1+200  
and  $p < 5\%$ : 4+4 or 3+5 or 2+8 or 1+40
- I often take two times **11 or 31 or 51**  
median, 5%-tile and 95%-tile are easily accessible  
with 11 or 31 or 51... data
- Too many data make statistical significance meaningless



## Statistical Significance: How many data do we need?



## Statistical Analysis

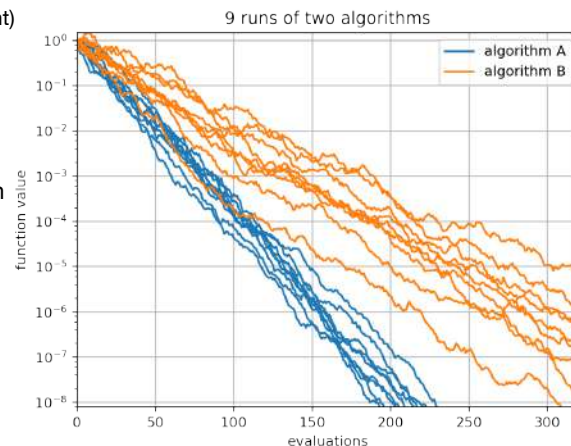
*“experimental results lacking proper statistical analysis must be considered anecdotal at best, or even wholly inaccurate”*

— M. Wineberg

Do you agree (sounds about right) or disagree (is taken a little over the top) with the quote?

an experimental result (shown are *all* data obtained):

Do we (even) need a statistical analysis?



## Jupyter IPython notebook

```
%pylab nbagg
import cma
cma.fmin(cma.ff.tablet, 20 * [1], 1);
```

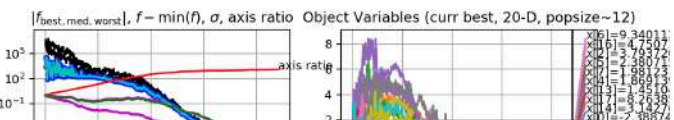
Populating the interactive namespace from numpy and matplotlib  
(6 w, 12) - aCMA-ES (mu\_w=3.7, w\_l=40%) in dimension 20 (seed=344737, Wed Jul 5 16:09:44 2017)

Iterat	#Evals	function value	axis ratio	sigma	min	max	std	t[mss]
1	12	2.637846492377813e+03	1.0e+00	9.49e-01	9e-01	1e+00	0:00.0	
2	24	3.858353384747645e+04	1.1e+00	9.13e-01	9e-01	9e-01	0:00.0	
3	36	1.589934793439056e+04	1.2e+00	8.94e-01	9e-01	9e-01	0:00.0	
100	1200	1.805167565570186e+02	6.6e+00	2.52e-01	6e-02	3e-01	0:00.1	
200	2400	9.260486860109009e+01	4.2e+01	2.79e-01	1e-02	4e-01	0:00.3	
300	3600	8.460045942108286e+00	2.0e+02	3.20e-01	4e-03	4e-01	0:00.4	
400	4800	5.352841113616880e-02	5.2e+02	4.71e-02	2e-04	5e-02	0:00.5	
500	6000	1.169838413517761e-04	8.7e+02	2.61e-03	3e-06	2e-03	0:00.7	
600	7200	2.232682824828931e-08	9.9e+02	5.00e-05	4e-08	3e-05	0:00.8	
700	8400	1.483610308401096e-12	1.2e+03	4.61e-07	3e-10	2e-07	0:00.9	
736	8832	2.696542797455203e-14	1.2e+03	1.03e-07	5e-11	5e-08	0:01.0	

termination on tolfun=1e-11 (Wed Jul 5 16:09:46 2017)  
final/bestever f-value = 1.422957e-14 1.422957e-14  
Incumbent solution: [-1.01044748e-11 -3.22608195e-08 -8.75163241e-10 -3.66834969e-08  
2.35485309e-08 -9.59521093e-10 4.23137381e-08 6.92049899e-09 ...]  
std deviations: [ 5.07976963e-11 4.52415829e-08 4.67529085e-08 4.36659472e-08  
4.04686177e-08 4.38294341e-08 4.65665203e-08 5.01580767e-08 ...]

```
cma.plot()
```

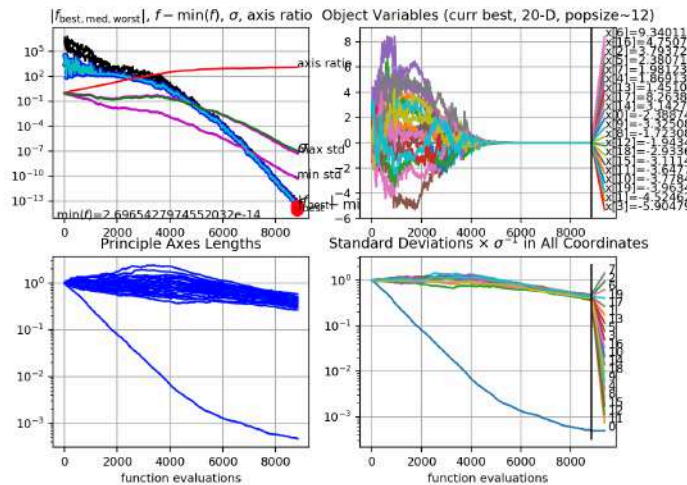
Figure 328



4.04686177e-08 4.38294341e-08 4.65665203e-08 5.01580767e-08 ...]

cma.plot()

Figure 328



Questions?

## Jupyter IPython notebook

```
# download&install anaconda python
# shell cmd "conda create" in case a different Python version is needed
# shell cmd "pip install cma" to install a CMA-ES module (or see github)
# shell cmd "jupyter-notebook" and click on compact-ga.ipynb
from __future__ import division, print_function
%pylab nbagg
```

Populating the interactive namespace from numpy and matplotlib

- See <https://github.com/nikohansen/GECCO-2019-experimentation-guide-notebooks>

- Demonstrations
  - A somewhat typical working mode
  - A parameter investigation

## Approaching an unknown problem

- Problem/variable **encoding**  
for example log scale vs linear scale vs quadratic transformation
- Fitness **formulation**  
for example  $\sum_i |x_i|$  and  $\sum_i x_i^2$  have the same optimal (minimal) solution but may be very differently "optimizable".
- Create **sections** plots (f vs x on a line)  
one-dimensional grid search is cheap
- Try to **locally improve** a given (good) solution
- Start local search from **different initial solutions**.  
Ending up always in different solutions? Or always in the same?
- Apply "global search" setting
- see also [http://cma.gforge.inria.fr/cmaes\\_sourcecode\\_page.html#practical](http://cma.gforge.inria.fr/cmaes_sourcecode_page.html#practical)

## Questions?

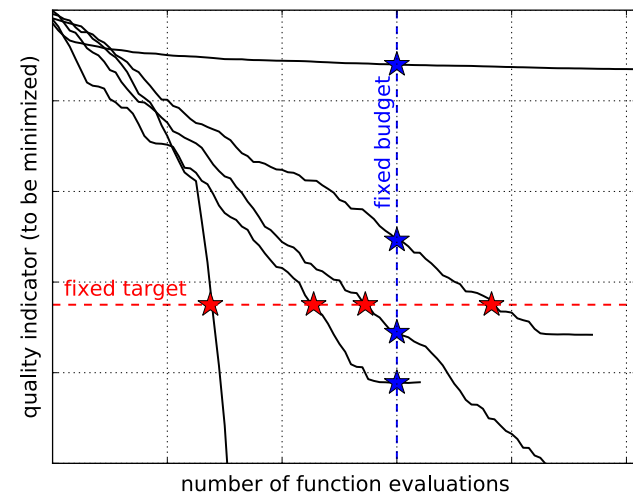
## Performance Assessment

- methodology: run an algorithm on a **set of test functions** and extract **performance measures** from the generated data  
choice of measure and aggregation
- display  
subtle display changes can make a huge difference
- there are surprisingly many devils in the details

## Why do we want to measure performance?

- compare algorithms and algorithm selection (the obvious)  
ideally we want standardized comparisons
- regression testing after (small) changes  
as we may expect (small) changes in behaviour, conventional regression testing may not work
- understanding of algorithms  
to improve algorithms  
non-standard experimentation is often preferable or necessary

## Aggregation: Fixed Budget vs Fixed Target



- for aggregation we need **comparable** data
- missing data: problematic when many runs lead to missing data
  - fixed target approach misses out on bad results (we may correct for this to some extent)
  - fixed budget approach misses out on good results



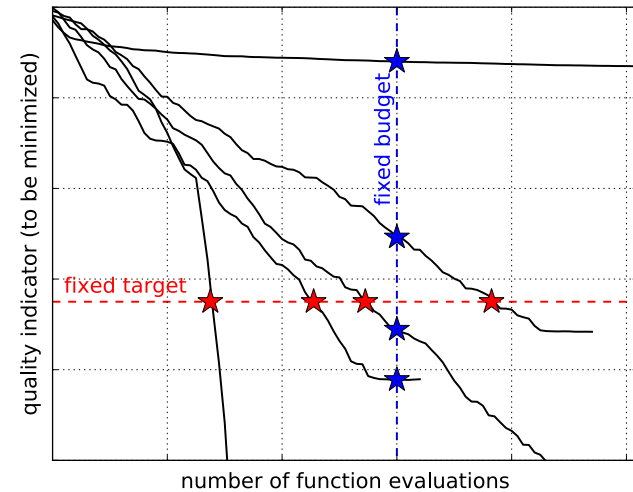
## Performance Measures for Evaluation

Generally, a performance measure should be

- **quantitative** on the ratio scale (highest possible)  
 “algorithm A is two *times* better than algorithm B”  
 as “performance(B) / performance(A) =  $1/2 = 0.5$ ”  
 should be meaningful statements
- assuming a wide range of values
- **meaningful (interpretable)** with regard to the real world  
 transfer the measure from benchmarking to real world

runtime or first hitting time is the prime candidate

## Aggregation: Fixed Budget vs Fixed Target



- for aggregation we need **comparable** data
- missing data: problematic when many runs lead to missing data
  - fixed target approach misses out on bad results (we may correct for this to some extent)
  - fixed budget approach misses out on good results

## Fixed Budget vs Fixed Target

Fixed budget => *measuring/display final/best f-values*

Fixed target => *measuring/display needed budgets (#evaluations)*

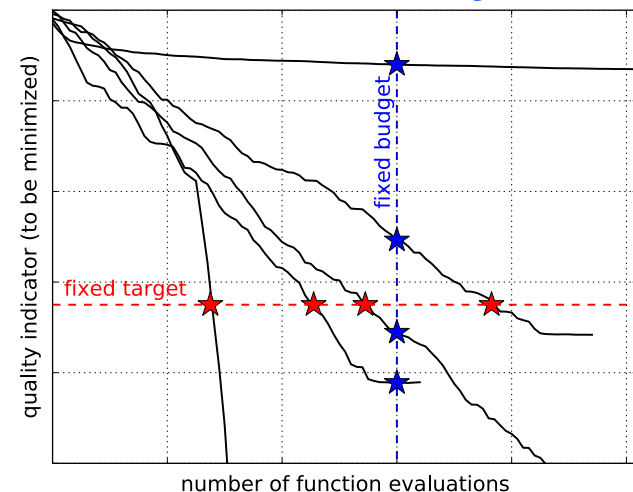
Number of function evaluations:

- are **quantitatively comparable** (on a ratio scale)  
 ratio scale: “A is 3.5 times faster than B”,  
 $A/B = 1/3.5$  is a meaningful notion
- the measurement itself is **interpretable independently of the function**  
 time remains the same time regardless of the underlying problem  
 3 times faster is 3 times faster is 3 times faster on every problem
- there is a clever way to account for **missing data**

via restarts

=> fixed target is (much) preferable

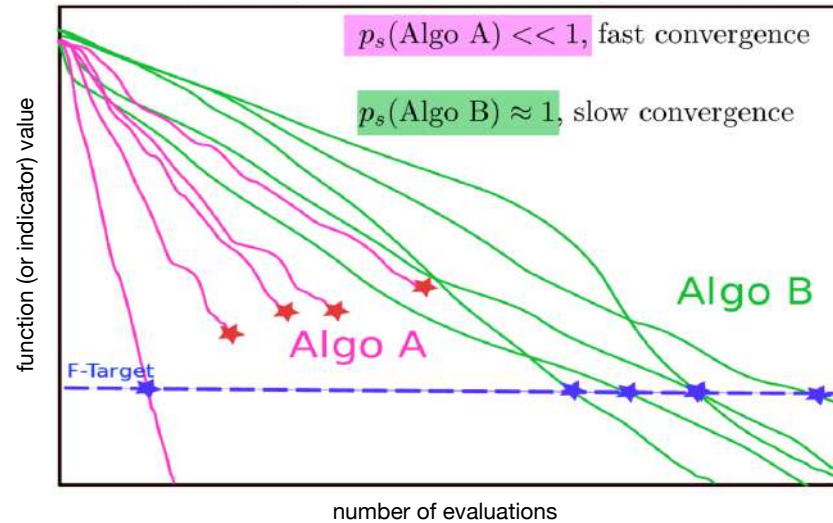
## The Problem of Missing Values



- for aggregation we need **comparable** data
- missing data: problematic when many runs lead to missing data
  - fixed target approach misses out on bad results (we may correct for this to some extent)
  - fixed budget approach misses out on good results

## The Problem of Missing Values

how can we compare the following two algorithms?



## The Problem of Missing Values

Consider simulated (artificial) restarts using the given independent runs

Algo Restart A:



$$p_s(\text{Algo Restart A}) = 1$$

Algo Restart B:



$$p_s(\text{Algo Restart B}) = 1$$

Caveat: the performance of algorithm A critically depends on termination methods (before to hit the target)

## The Problem of Missing Values

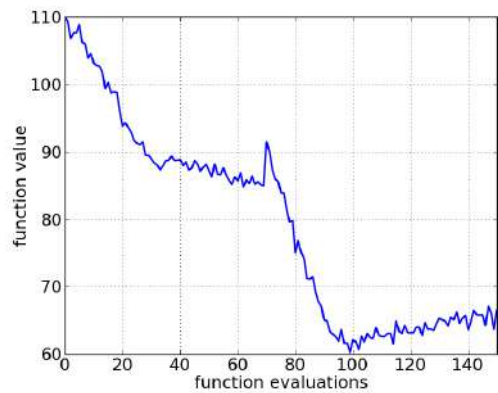
The **expected runtime** (ERT, aka SP2, aRT) to hit a target value in #evaluations is computed (estimated) as:

$$\begin{aligned} \text{ERT} &= \frac{\text{\#evaluations(until to hit the target)}}{\text{\#successes}} && \text{unsuccessful runs count (only) in the nominator} \\ &= \text{avg}(\text{evals}_{\text{succ}}) + \overbrace{\frac{N_{\text{unsucc}}}{N_{\text{succ}}}}^{\text{odds ratio}} \times \text{avg}(\text{evals}_{\text{unsucc}}) \\ &\approx \text{avg}(\text{evals}_{\text{succ}}) + \frac{N_{\text{unsucc}}}{N_{\text{succ}}} \times \text{avg}(\text{evals}_{\text{succ}}) \\ &= \frac{N_{\text{succ}} + N_{\text{unsucc}}}{N_{\text{succ}}} \times \text{avg}(\text{evals}_{\text{succ}}) \\ &= \frac{1}{\text{success rate}} \times \text{avg}(\text{evals}_{\text{succ}}) \end{aligned}$$

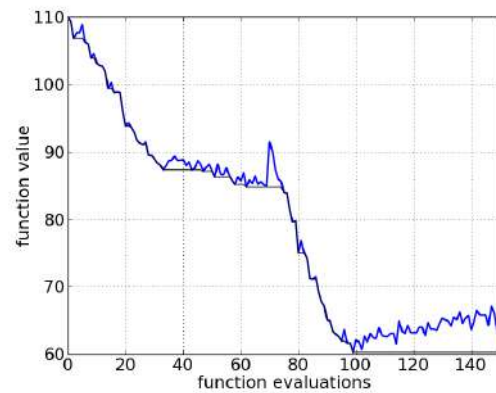
defined (only) for #successes > 0. The last three lines are aka Q-measure or SP1 (success performance).

## Empirical Distribution Functions

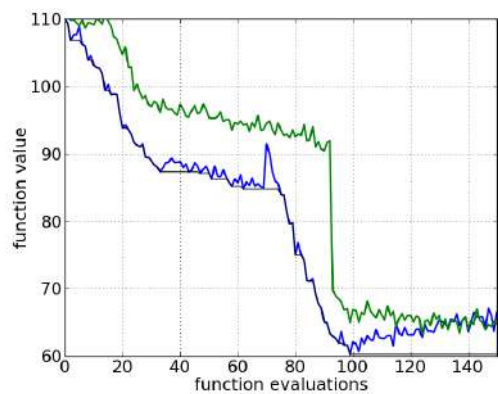
- **Empirical cumulative distribution functions** (ECDF, or in short, **empirical distributions**) are arguably the **single most powerful tool** to “aggregate” data in a display.



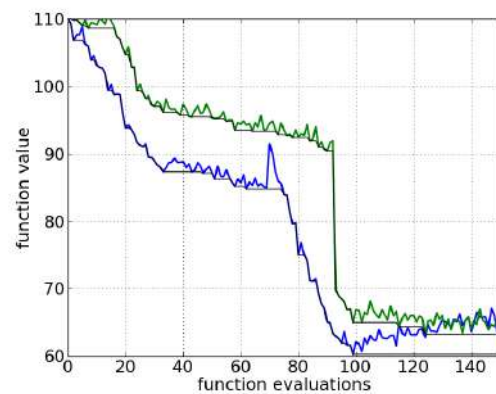
- a convergence graph



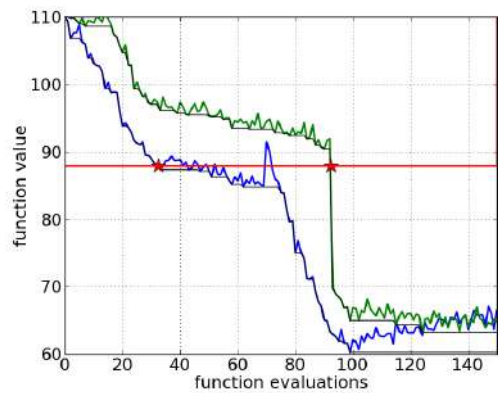
- a convergence graph
- first hitting time (black): lower envelope, a monotonous graph



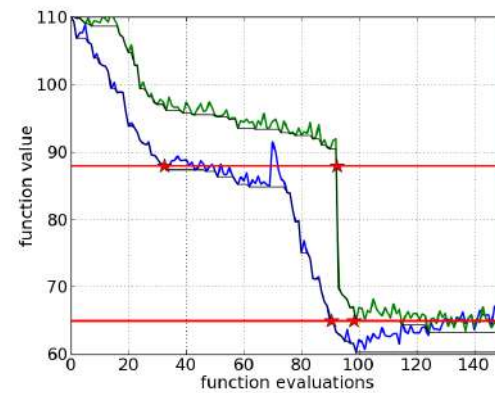
- another convergence graph



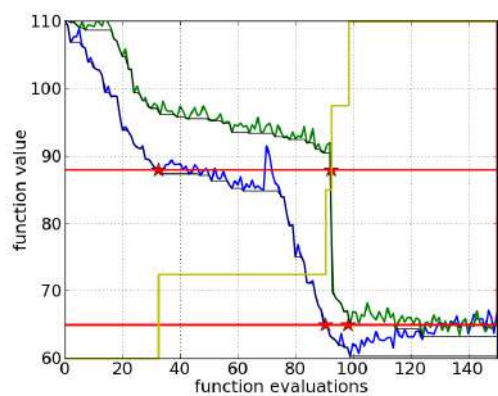
- another convergence graph with hitting time



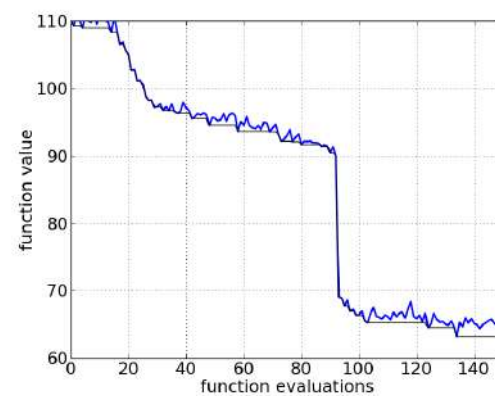
- a target value delivers two data points (or possibly missing values)



- another target value delivers two more data points

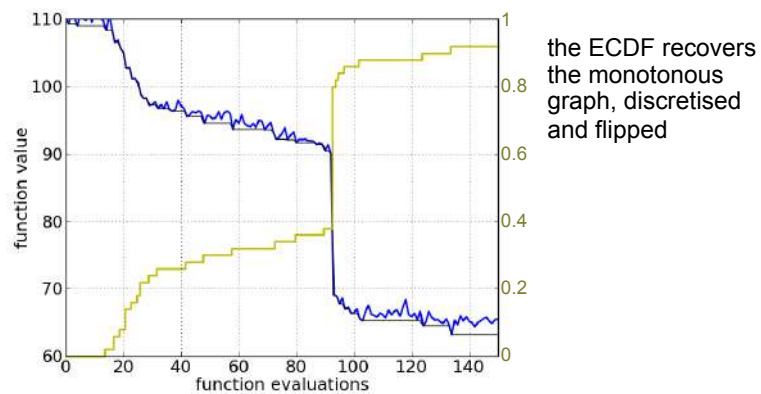
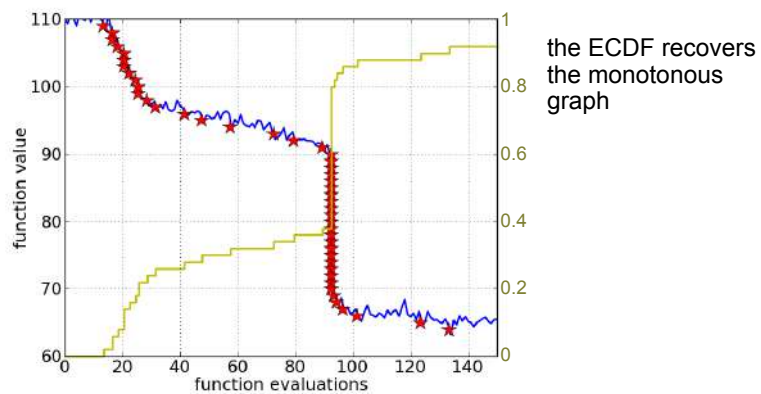
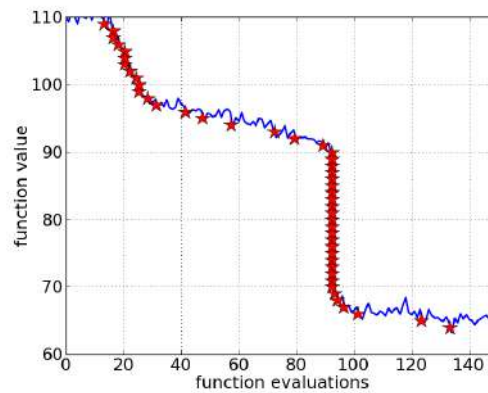
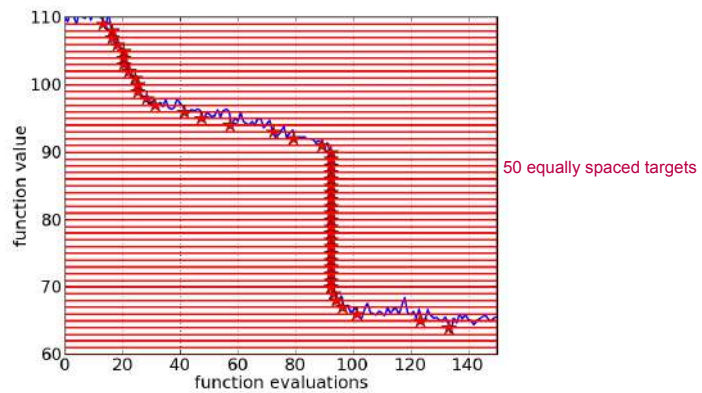


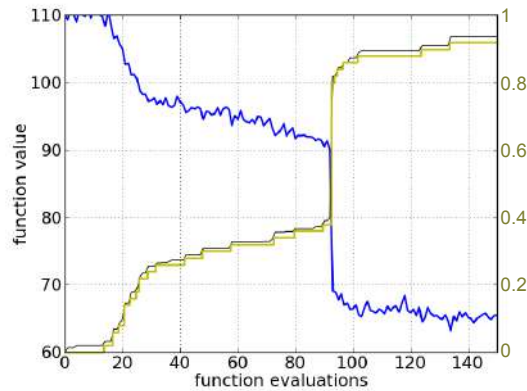
- the ECDF with four steps (between 0 and 1)



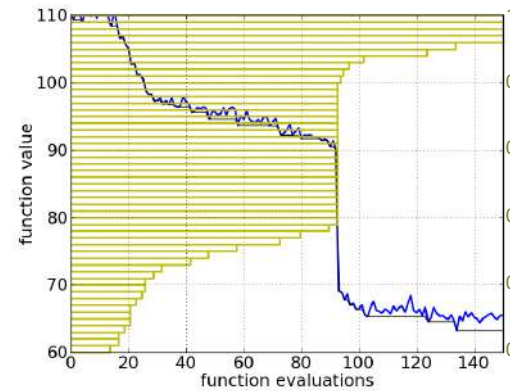
- reconstructing a single run







the ECDF recovers  
the monotonous  
graph, discretised  
and flipped



the ECDF recovers  
the monotonous  
graph, discretised  
and flipped

the area over the  
ECDF curve is the  
average runtime  
(the geometric  
average if the x-axis  
is in log scale)

## Data and Performance Profiles

- so-called *Data Profiles* (Moré and Wild 2009) are empirical distributions of runtimes [# evaluations] to achieve a given single target

usually divided by dimension + 1

- so-called *Performance profiles* (Dolan and Moré 2002) are empirical distributions of *relative* runtimes [# evaluations] to achieve a given single target

normalized by the runtime of the fastest algorithm  
on the respective problem

## Benchmarking with COCO

### COCO — Comparing Continuous Optimisers

- is a (software) platform for comparing continuous optimisers in a black-box scenario  
<https://github.com/numbbo/coco>
- automatises* the tedious and repetitive task of *benchmarking numerical optimisation algorithms in a black-box setting*
- advantage: saves time and *prevents* common (and not so common) *pitfalls*

### COCO provides

- experimental and measurement *methodology*  
main decision: what is the end point of measurement
- suites of benchmark functions  
single objective, bi-objective, noisy, constrained (in beta stage)
- data* of already benchmarked algorithms *to compare with*

## COCO: Installation and Benchmarking in Python

```
$ ## get and install the code
$ git clone https://github.com/numbbbo/coco.git # get coco using git
$ cd coco
$ python do.py run-python # install Python experimental module cocoex
$ python do.py install-postprocessing # install post-processing :-)
```

```
import os, webbrowser
from scipy.optimize import fmin
import cocoex, cocopp

# prepare
output_folder = "scipy-optimize-fmin"
suite = cocoex.Suite("bbob", "", "")
observer = cocoex.Observer("bbob", "result_folder: " + output_folder)

# run benchmarking
for problem in suite: # this loop will take several minutes
    observer.observe(problem) # generates the data for cocopp post-processing
    fmin(problem, problem.initial_solution)

# post-process and show data
cocopp.main(observer.result_folder) # re-run folders look like "...-001" etc
webbrowser.open("file://" + os.getcwd() + "/ppdata/index.html")
```

## Benchmark Functions

should be

- comprehensible
- difficult to defeat by “cheating”  
examples: optimum in zero, separable
- scalable with the input dimension
- reasonably quick to evaluate  
e.g. 12-36h for one full experiment
- reflect reality

specifically, we model well-identified difficulties encountered also in real-world problems

## The COCO Benchmarking Methodology

- budget-free  
larger budget means more data to investigate  
any budget is comparable  
termination and restarts are or become relevant
- using runtime as (almost) single performance measure  
measured in number of function evaluations
- runtimes are aggregated
- in empirical (cumulative) distribution functions
- by taking averages  
geometric average when aggregating over different problems

## Benchmarking Results for Algorithm ALG on the bboB Suite

[Home](#)

[Runtime distributions \(ECDFs\) per function](#)

[Runtime distributions \(ECDFs\) summary and function groups](#)

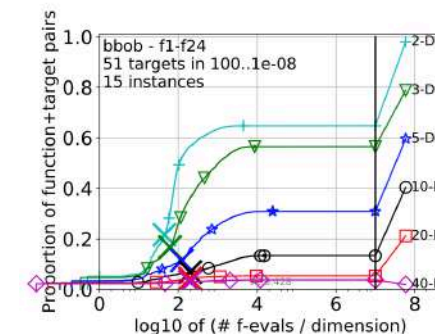
[Scaling with dimension for selected targets](#)

[Tables for selected targets](#)

[Runtime distribution for selected targets and f-distributions](#)

[Runtime loss ratios](#)

**Runtime distributions (ECDFs) over all targets**



## Using Theory

*“In the course of your work, you will from time to time encounter the situation where the facts and the theory do not coincide. In such circumstances, young gentlemen, it is my earnest advice to respect the facts.”*

— Igor Sikorsky, airplane and helicopter designer

## Using Theory in Experimentation

- shape our expectations and objectives
- debugging / consistency checks
  - theory may tell us what we *expect* to see
- knowing the limits (optimal bounds)
  - for example, we cannot converge faster than optimal
  - trying to improve is a waste of time
- utilize **invariance**
  - it may be possible to design a much simpler experiment and get to the same or stronger conclusion by invariance considerations
  - change of coordinate system is a powerful tool

FIN